Imaging, Deconvolution& Image Analysis

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Scientific Analysis of a mm Interferometer Output

mm interferometer output:

Calibrated visibilities in the uv plane (\simeq the Fourier plane).

2 possibilities:

- uv plane analysis (cf. Lecture by A. Castro-Carrizo):
 Always better . . . when possible!
 (in practice for "simple" sources as point sources or disks)
- Image plane analysis:
 - \Rightarrow Mathematical transforms to go from uv to image plane!

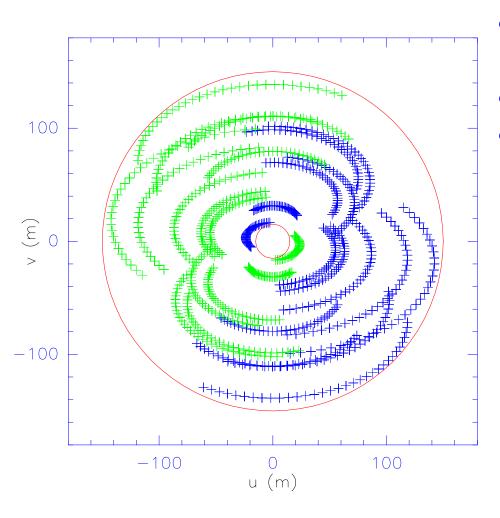
Goal: Understand effects of the imaging process on

- The resolution;
- The field of view (single pointing or mosaicing, cf. Lecture by F. Gueth);
- The reliability of the image;
- The noise level and repartition (cf. lecture by S.Guilloteau).

From Calibrated Visibilities to Images:

I. Comparison Visibilities/Source Fourier Transform

$$V_{ij}(b_{ij}) = 2D \text{ FT} \left\{ B_{\text{primary}}.I_{\text{source}} \right\} (b_{ij}) + N$$



- Primary Beam
 - ⇒ Distorted source information.
- Noise
 ⇒ Sensitivity problems.
- Irregular, limited sampling
 - ⇒ incomplete source information:
 - Support limited at:
 - * High spatial frequency
 - ⇒ limited resolution;
 - * Low spatial frequency ⇒ problem of wide field imaging;
 - Inside the support, incomplete (i.e. Nyquist's criterion not respected) sampling ⇒ lost of information.

From Calibrated Visibilities to Images: II. Effect of Irregular, Limited Sampling

Definitions:

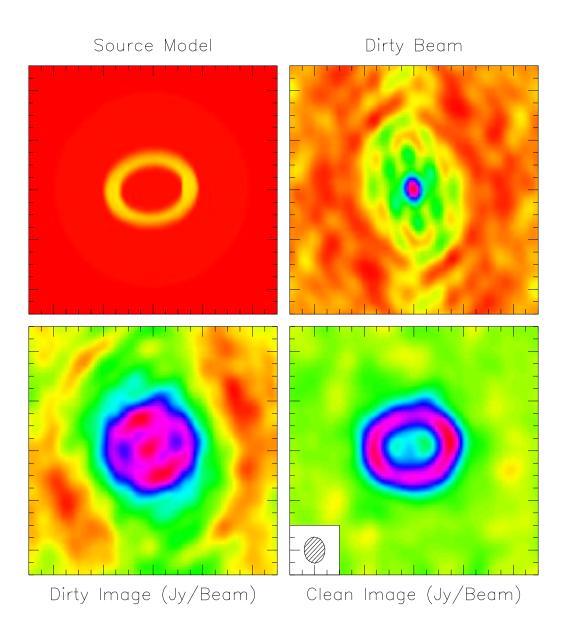
- $V = 2D \text{ FT } \{B_{\text{primary}}.I_{\text{source}}\};$
- Irregular, limited sampling function:
 - -S(u,v)=1 at (u,v) points where visibilities are measured;
 - -S(u,v)=0 elsewhere;
- $B_{\text{dirty}} = 2D \text{ FT}^{-1} \{S\};$
- $I_{\text{meas}} = 2D \text{ FT}^{-1} \{S.V\}.$

Fourier Transform Property #1:

$$I_{\text{meas}} = B_{\text{dirty}} * \{B_{\text{primary}}.I_{\text{source}}\}.$$

 B_{dirty} : Point Spread Function (PSF) of the interferometer (*i.e.* if the source is a point, then $I_{\text{meas}} = I_{\text{tot}}.B_{\text{dirty}}$).

From Calibrated Visibilities to Images: III. Why Deconvolving?



- Difficult to do science on dirty image.
- Deconvolution ⇒ a clean image compatible with the sky intensity distribution.

From Calibrated Visibilities to Images: IV. Summary

Fourier Transform and Deconvolution: The two key issues in imaging.

Stage	Implementation
Calibrated Visibilities	
↓ Fourier Transform	UV_STAT, UV_MAP
Dirty beam & image	
↓ Deconvolution	HOGBOM, CLARK
Clean beam & image	
↓ Visualization	GO BIT, GO VIEW
↓ Image analysis	GO NOISE, GO FLUX, GO MOMENTS
Physical information	
on your source	

Direct vs. Fast Fourier Transform

Direct FT:

- Advantage: Direct use of the irregular sampling;
- Inconvenient: Slow.

Fast FT:

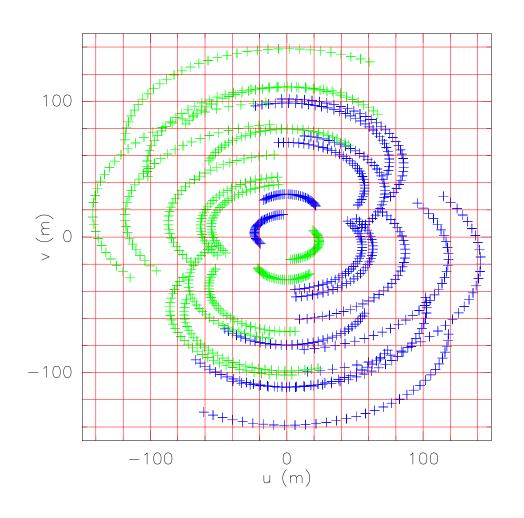
- Inconvenient: Needs a regular sampling ⇒ Gridding;
- Advantage: Quick for images of size $2^M \times 2^N$.
- \Rightarrow In practice, everybody use FFT.

From Calibrated Visibilities to Images: Summary

Fourier Transform and Deconvolution: The two key issues in imaging.

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Dirty beam & image	
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Physical information on your source	

Gridding: I. Interpolation Scheme



Convolution because:

- Visibilities = noisy samples of a smooth function.
 - \Rightarrow Some smoothing is desirable.
- Nearby visibilities are not independent.

-
$$V = 2D \text{ FT} \left\{ B_{\text{primary}}.I_{\text{source}} \right\}$$

= $\tilde{B}_{\text{primary}} * \tilde{I}_{\text{source}};$

- FWHM(convolution kernel)
 - $< \mathsf{FWHM}(\tilde{B}_{\mathsf{primary}})$
 - ⇒ No real information lost.

Gridding: II. Convolution Equation is Kept Through Gridding

Demonstration:

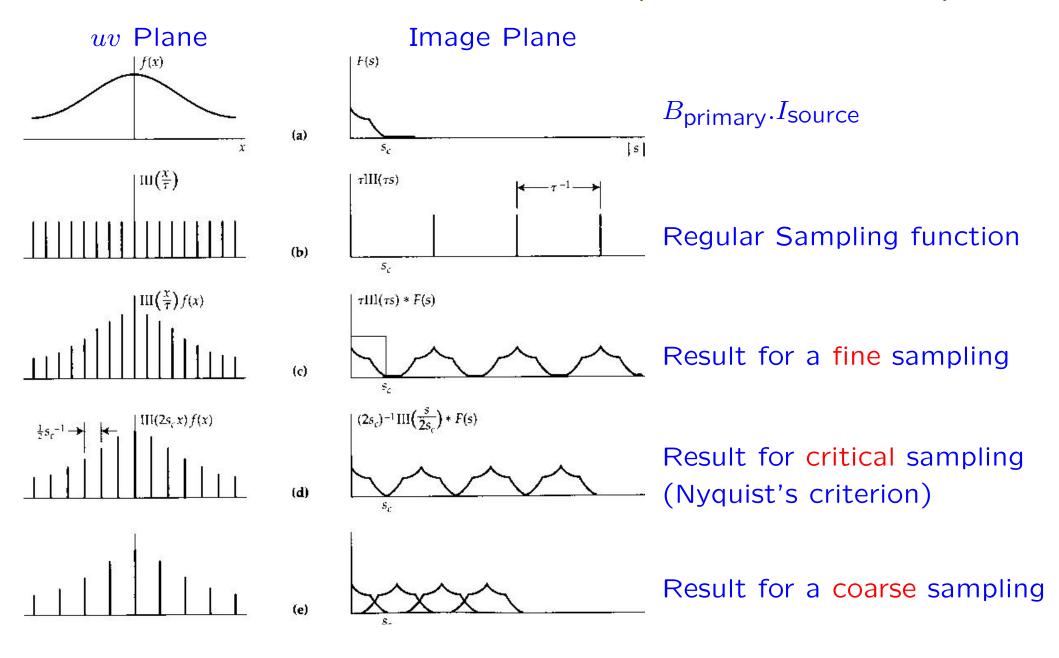
- $I_{\text{meas}}^{\text{grid}} \stackrel{\text{2D FT}}{\rightleftharpoons} G * (S.V)$ \Leftrightarrow $I_{\text{meas}}^{\text{grid}} = \tilde{G}.(\widetilde{S.V});$ • $B_{\text{dirty}}^{\text{grid}} \stackrel{\text{2D FT}}{\rightleftharpoons} G * S$ \Leftrightarrow $B_{\text{dirty}}^{\text{grid}} = \tilde{G}.\tilde{S};$
- \Rightarrow $I_{\text{meas}} = B_{\text{dirty}} * \left\{ B_{\text{primary}}.I_{\text{source}} \right\}$ with $I_{\text{meas}} = I_{\text{meas}}^{\text{grid}}/\tilde{G}$ and $B_{\text{dirty}} = B_{\text{dirty}}^{\text{grid}}/\tilde{G}$.

Remark: Gridding may be hidden in equations but it is still there.

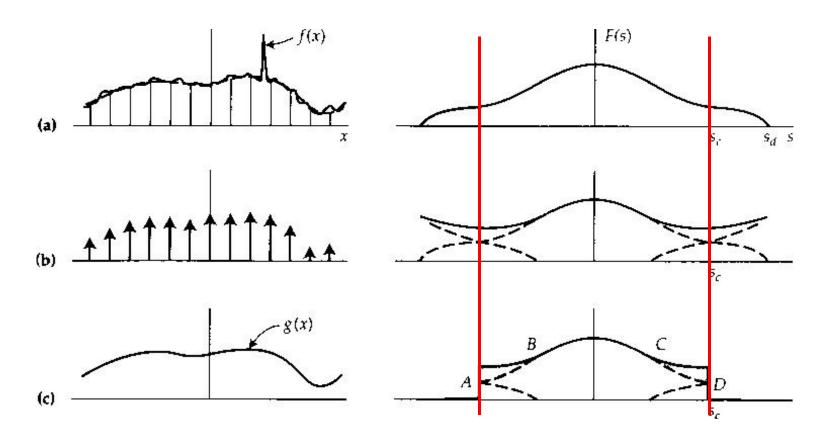
⇒ Artifacts due to gridding! (cf. next transparencies)

Gridding:

III. Effect of a Regular Sampling (Periodic Replication)



Gridding: III. Effect of a Regular Sampling (Aliasing)



Aliasing = Folding of intensity outside the image size into the image.

⇒ Image size must be large enough.

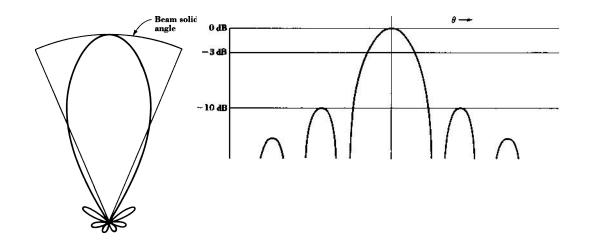
Gridding: IV. Pixel and Image Sizes

Pixel size: Between 1/3 and 1/4 of the synthesized beam size (*i.e.* more than the Nyquist's criterion in image plane to ease deconvolution).

Image size:

- = uv plane sampling rate (FT property # 2);
- ullet Natural resolution in the uv plane: $ilde{B}_{\mathsf{primary}}$ size;
- \Rightarrow At least twice the B_{primary} size (i.e. Nyquist's criterion in uv plane).

Gridding: V. Bright Sources in $B_{primary}$ Sidelobes



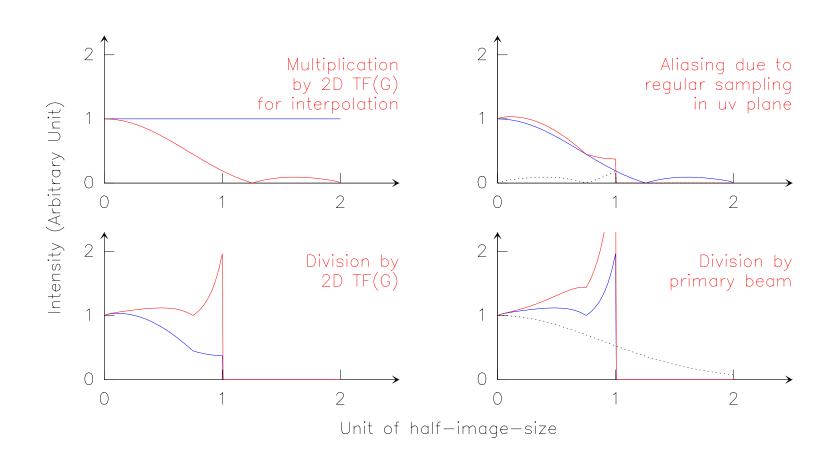
Bright Sources in B_{primary} sidelobes outside image size will be aliased into image.

⇒ Spurious source in your image!

Solution: Increase the image size.

(Be careful: only when needed for efficiency reasons!)

Gridding: VI. Noise Distribution



Gridding: VII. Choice of Gridding function

Gridding function must:

- Fall off quickly in image plane (to avoid noise aliasing);
- Fall off quickly in uv plane (to avoid too much smoothing).
- ⇒ Define a mathematical class of functions: Spheroidal functions.

GILDAS implementation: In UV_MAP

- Spheroidal functions = Default gridding function;
- Tabulated values are used for speed reasons.

Dirty Beam Shape and Image Quality

$$B_{\text{dirty}} = 2D \ \text{FT}^{-1} \{S\}.$$

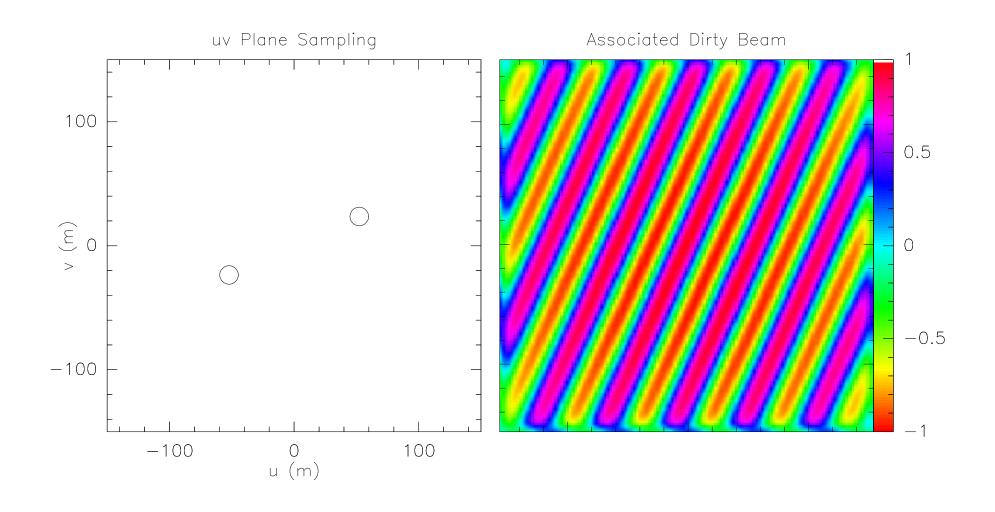
Importance of the Dirty Beam Shape:

- Deconvolving a dirty image is a delicate stage;
- The closest to a Gaussian $B_{\rm dirty}$ is, the easier the deconvolution;
- Extreme case: $B_{\text{dirty}} = \text{Gaussian} \Rightarrow \text{No deconvolution needed at all!}$

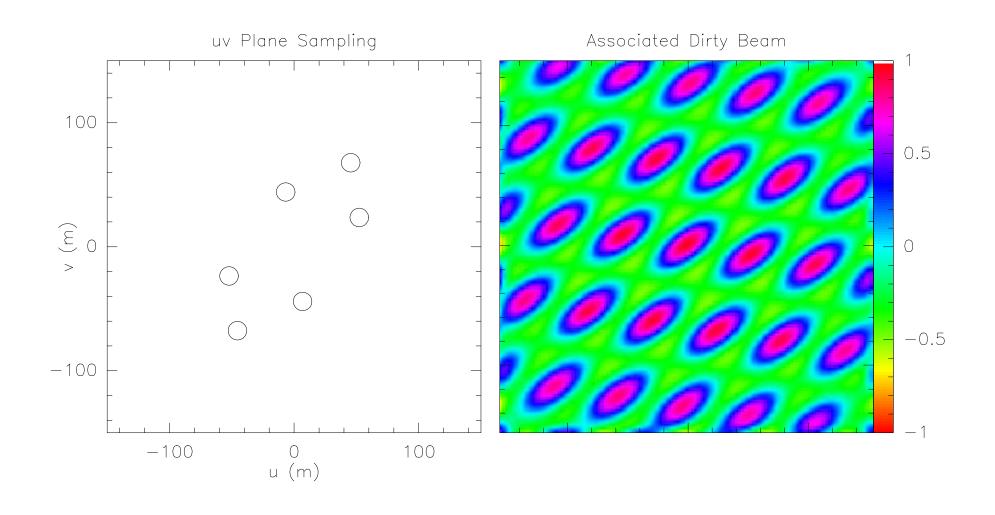
Ways to improve (at least change) B_{dirty} shape:

- Increase the number of antenna (costly).
- Change the antenna layout (technically difficult).
- Weight the irregular, limited sampling function S (the only thing you can do in practice).

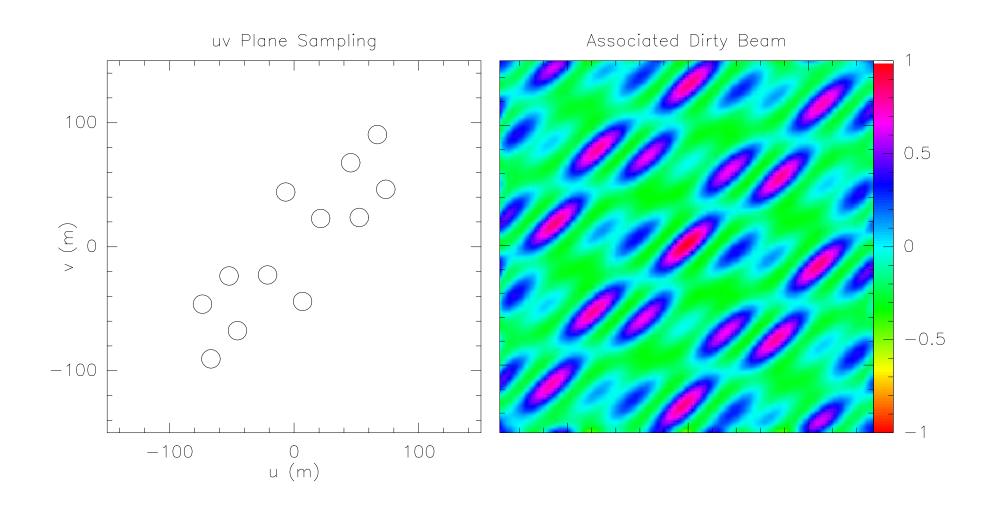
Dirty Beam Shape and Number of Antenna: 2 Antenna



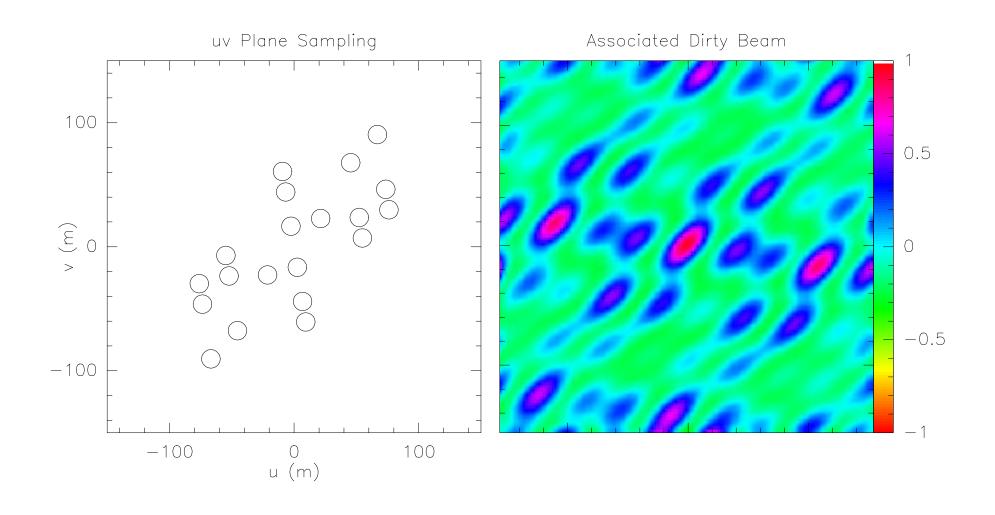
Dirty Beam Shape and Number of Antenna: 3 Antenna



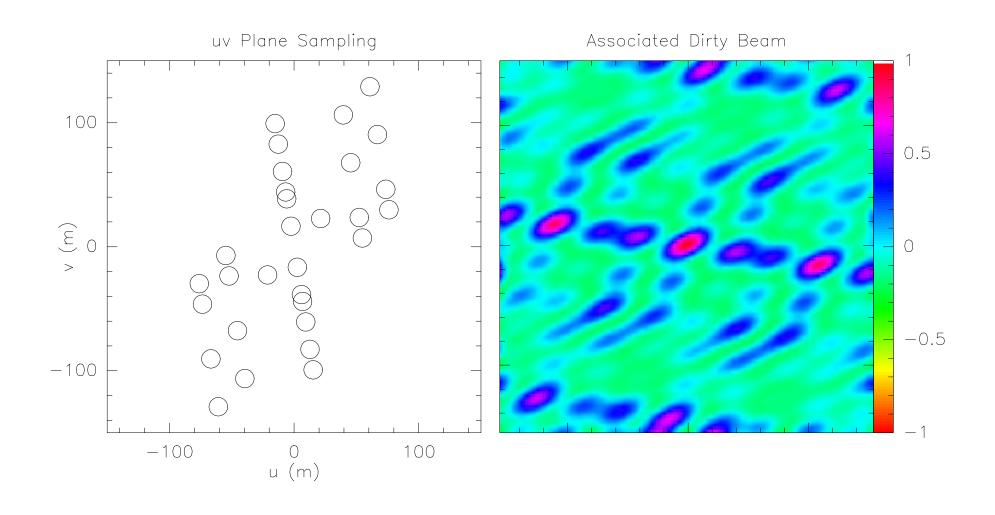
Dirty Beam Shape and Number of Antenna: 4 Antenna

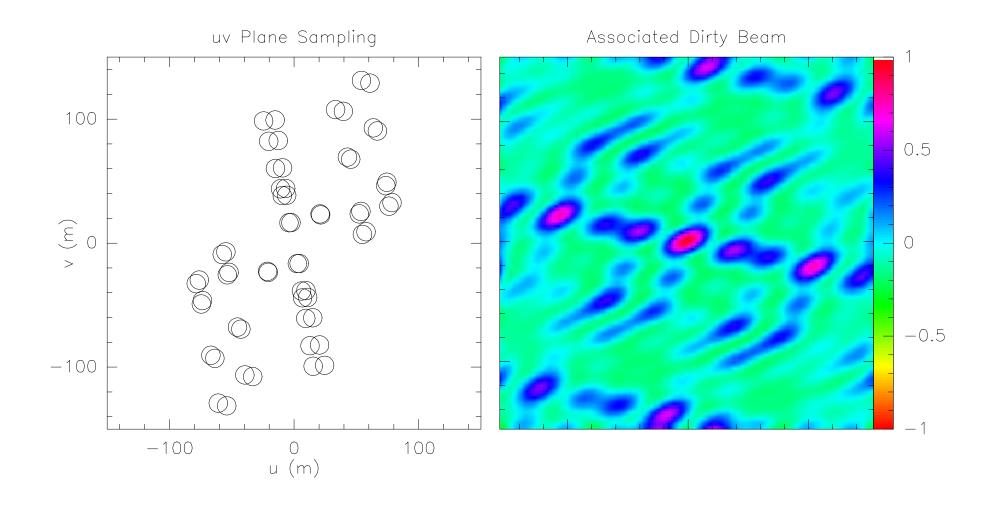


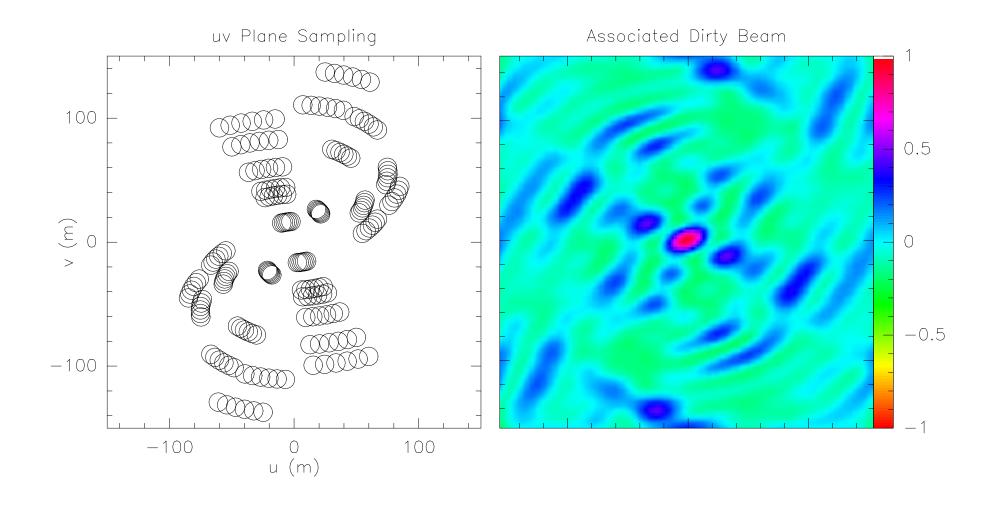
Dirty Beam Shape and Number of Antenna: 5 Antenna

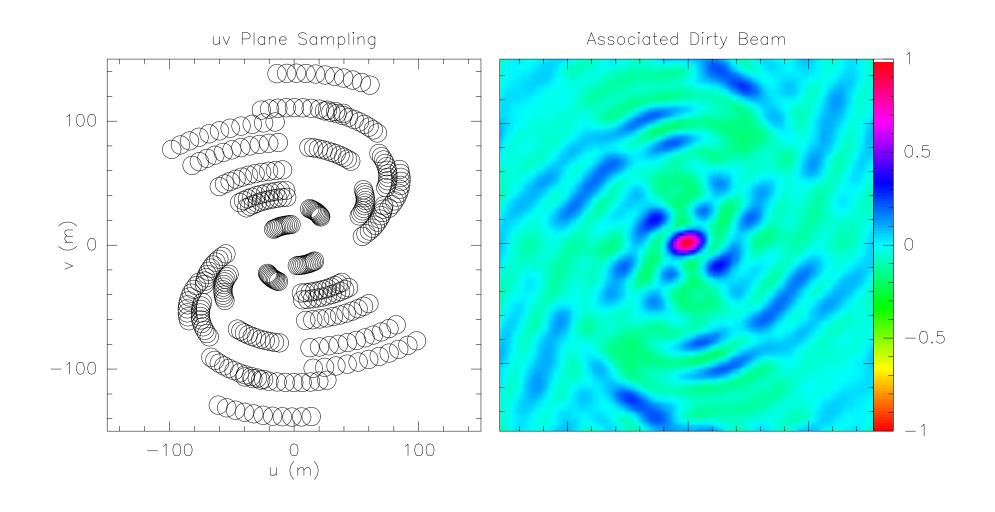


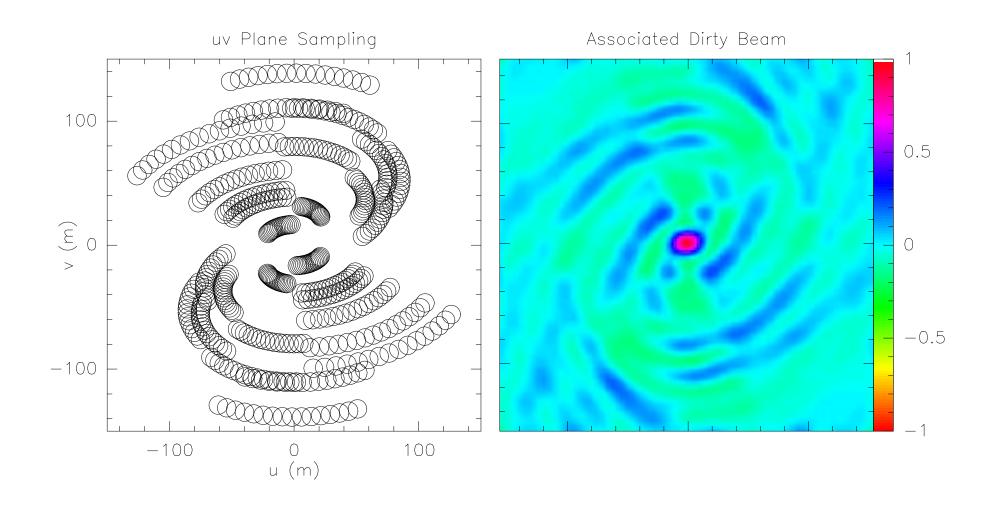
Dirty Beam Shape and Number of Antenna: 6 Antenna

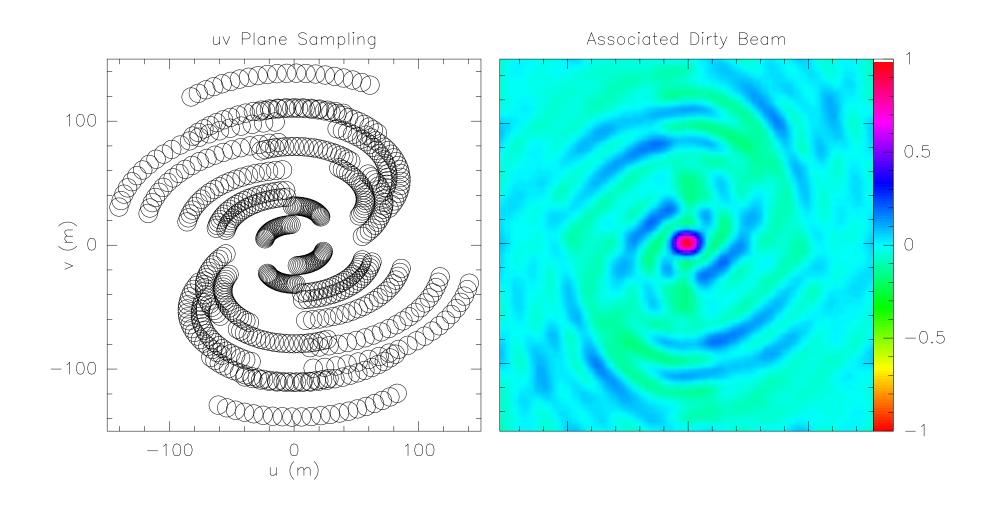


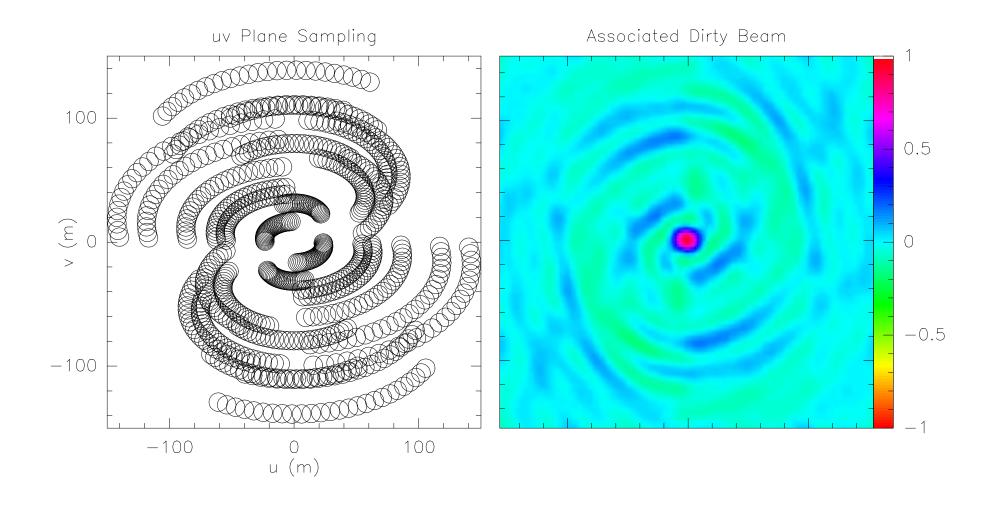


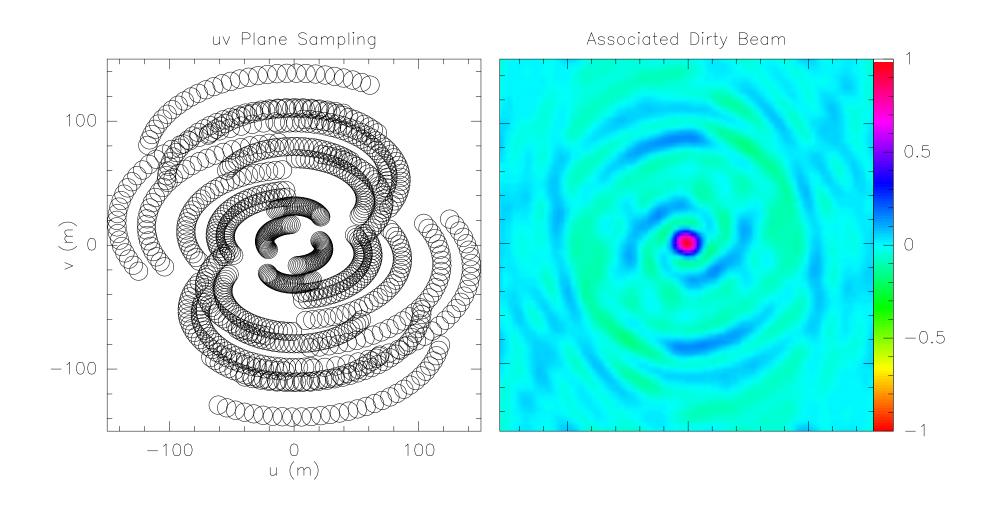


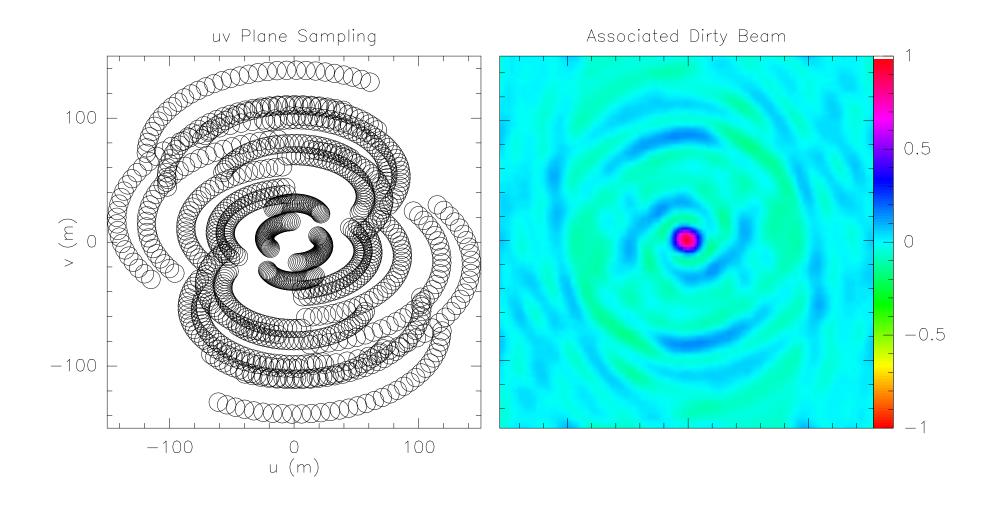












Dirty Beam Shape and Weighting

Natural Weighting: Default definition of the irregular sampling function at uv table creation.

- $S(u,v) = 1/\sigma^2$ at (u,v) points where visibilities are measured;
- S(u,v) = 0 elsewhere;

with $\sigma^2(u,v)$ the noise variance of the visibility.

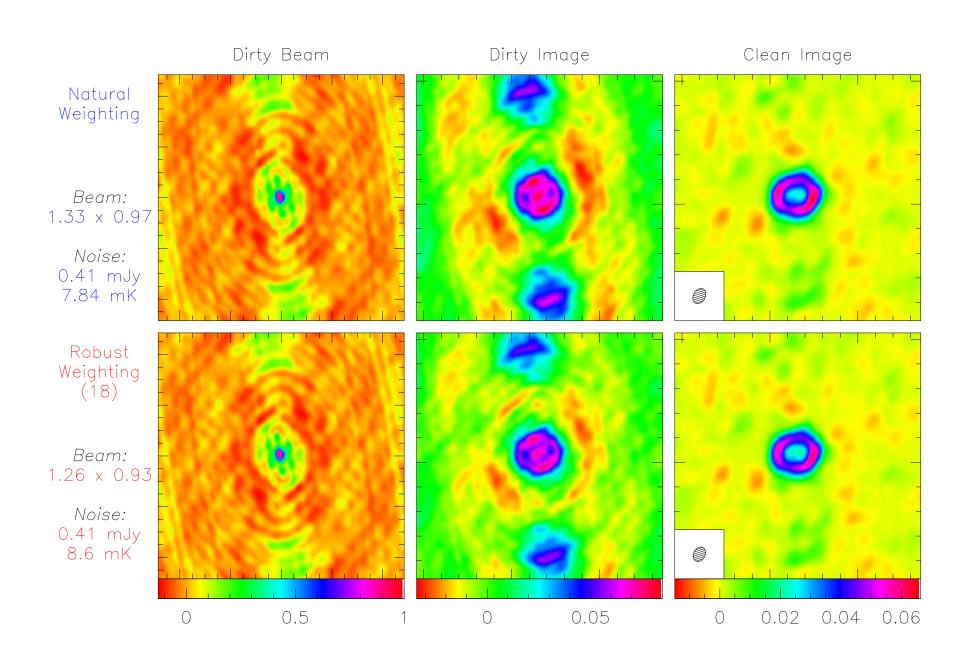
Introduction of a weighting function W(u, v):

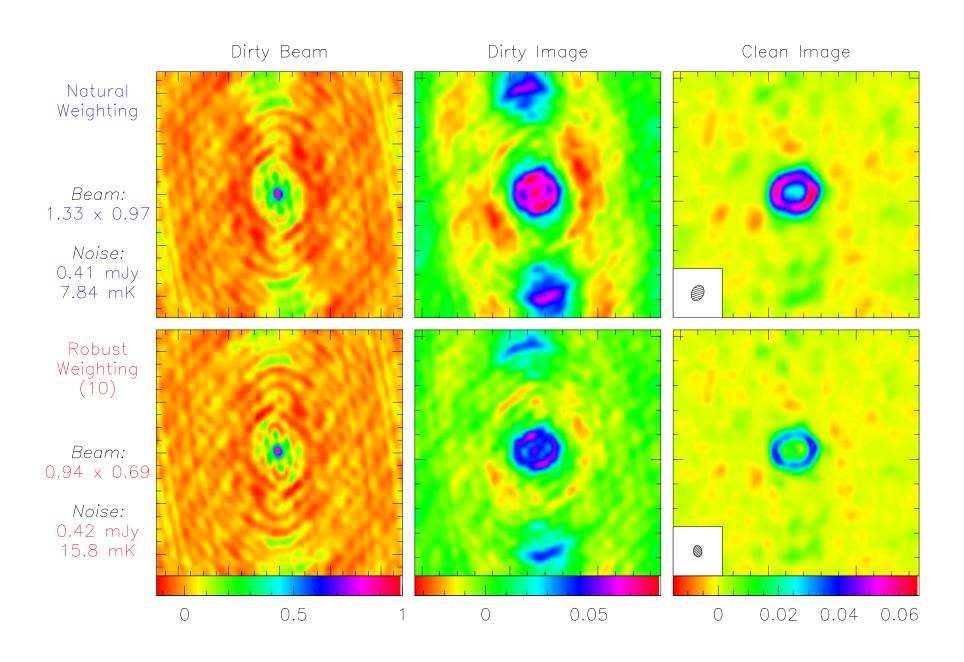
- $B_{\text{dirty}} = 2D \text{ FT}^{-1} \{W.S\};$
- Robust weighting: W enhance the large baseline contribution;
- Tapering: W enhance the small baseline contribution.

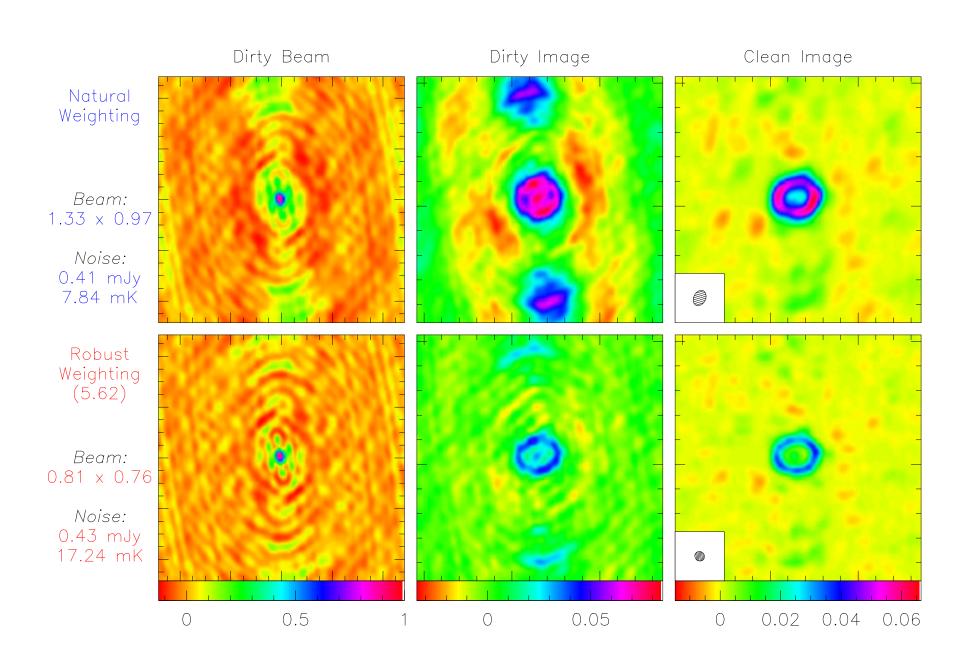
Robust Weighting: I. Definition

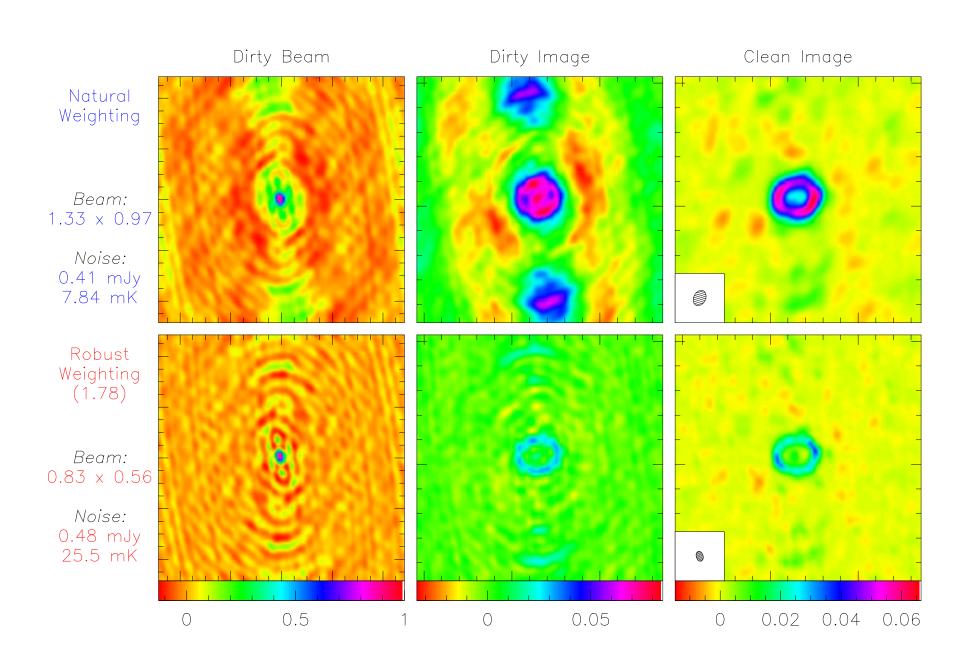
Definitions:

- Natural = $\sum_{(u,v) \in Cell} S$;
- $\sum_{(u,v) \in Cell} W.S = \begin{cases} Constant & \text{if (Natural} \ge Threshold); \\ Natural & \text{else;} \end{cases}$
- In practice, the cell size is 0.5D.









Robust Weighting: III. Definition and Properties

Definitions:

- Natural = $\sum_{(u,v) \in Cell} S$;
- $\sum_{(u,v) \in \text{Cell}} W.S = \begin{cases} \text{Constant if (Natural} \leq \text{Threshold)}; \\ \text{Natural else;} \end{cases}$
- In practice, the cell size is 0.5D.

Properties:

- Increase the resolution;
- Lower the sidelobes;
- Degrade point source sensitivity.

Unfortunately: GILDAS implementation gives it the name of "uniform" weighting!

Tapering: I Definition

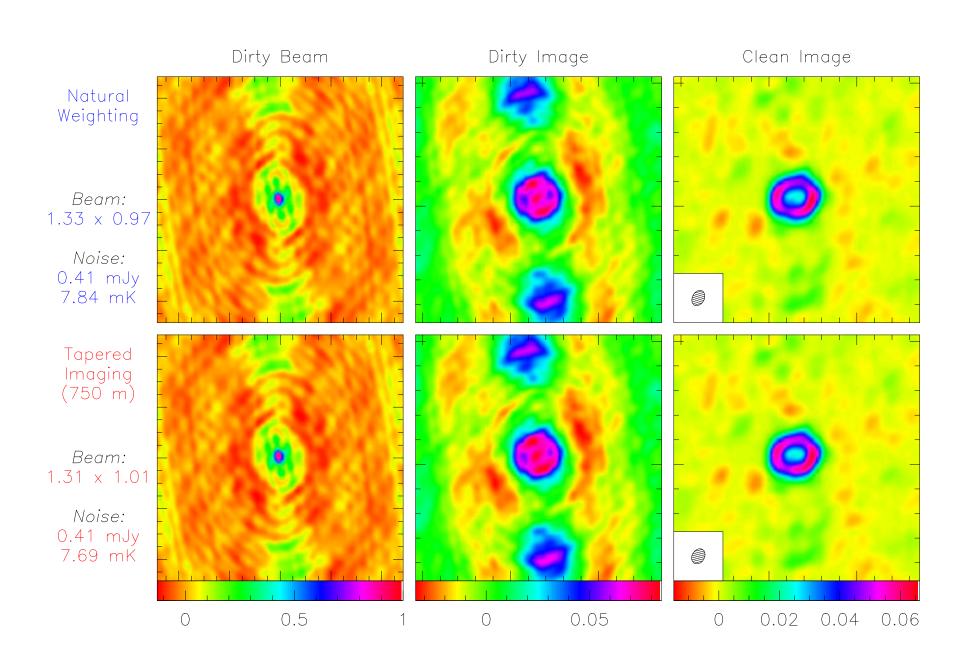
Definition:

ullet Apodization of the uv coverage in general by a Gaussian;

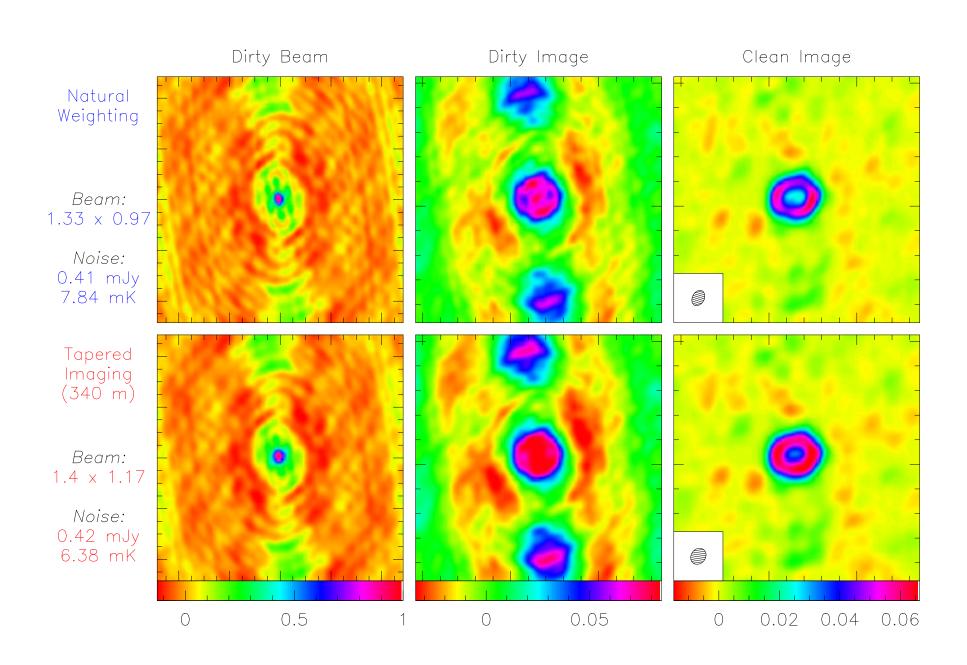
•
$$W = \exp\left\{-\frac{\left(u^2 + v^2\right)}{t^2}\right\}$$
 where $t =$ tapering distance.

 \Rightarrow Convolution (*i.e.* smoothing) of the image by a Gaussian.

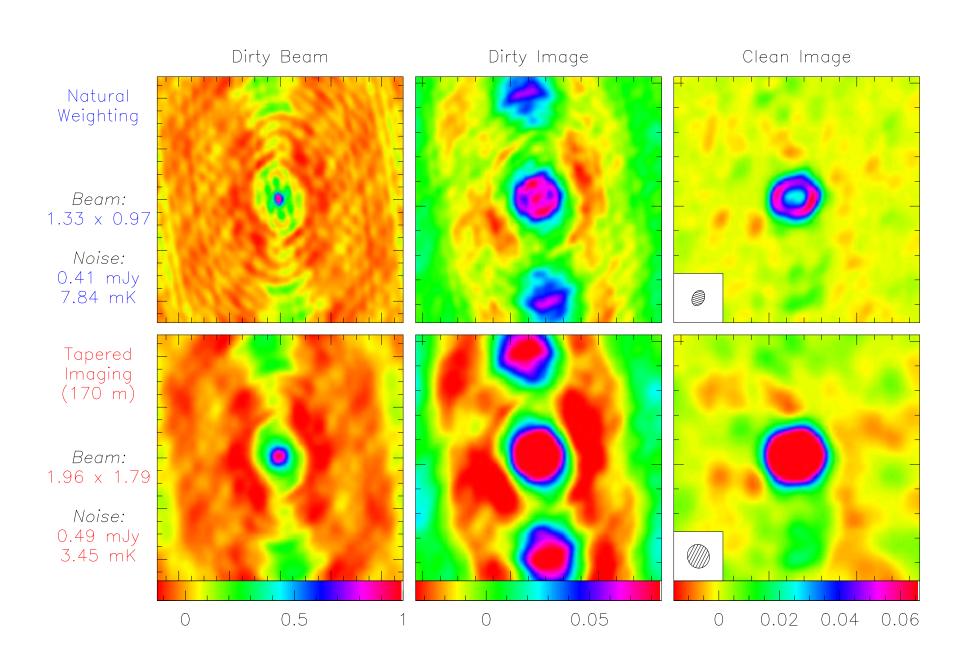
Tapering: II. Examples



Tapering: II. Examples



Tapering: II. Examples



Tapering: III. Definition and Properties

Definition:

ullet Apodization of the uv coverage in general by a Gaussian;

•
$$W = \exp\left\{-\frac{\left(u^2 + v^2\right)}{t^2}\right\}$$
 where $t =$ tapering distance.

 \Rightarrow Convolution (i.e. smoothing) of the image by a Gaussian.

Properties:

- Decrease the resolution;
- Degrade point source sensitivity;
- Increase sensitivity to "medium size" structures.

Inconvenient: Throw out some information.

⇒ To increase sensitivity to extended sources, use compact arrays not tapering.

Weighting and Tapering: Summary

	Robust	Natural	Tapering
Resolution	High	Medium	Low
Side Lobes		Medium	?
Point Source Sensitivity		Maximum	
Extended Source Sensitivity		Medium	7

Non-circular tapering + Robust weighting: Sometimes \Rightarrow Better (*i.e.* smaller and more circular) beams.

Weighting and Tapering: GILDAS implementation

Resolution, point/extended source sensitivity as a function of robust threshold or tapering distance.

MAPPING> UV_STAT WEIGHT

Robust	Major	Minor	PA	Noise		Sidelobe	
	(")	(")	(deg)	(mJy)	(K)	%	
0.10	0.840	0.527	18.5	0.791	0.044	-16.1	13.9
None	1.271	0.940	155.1	0.406	0.008	-2.7	25.9
I-UV_STAT,	Recommen	nded pixel	size is	0.080 -	0.264"		

MAPPING> UV_STAT TAPER

Taper	Major	Minor	PA	Noi	se	Sidelob	e
(m)	(")	(")	(deg)	(mJy)	(K)	%	
30.00	4.844	3.817	11.9	1.019	0.001	-44.7	14.5
None	1.323	0.967	151.5	0.406	0.008	-12.9	28.7

From Calibrated Visibilities to Images: GILDAS implementation

MAPPING> INPUT UV_MAP: display UV_MAP control parameters. Default = $0 \Rightarrow$ Try something clever.

- Gridding kernel: CONVOLUTION (default: 5, i.e. spheroidals).
- Data cube setup:
 - First and last data channels to map: MCOL (default: 0, i.e. all channels).
 - Pixel size: MAP_CELL (in arcsec, default: 0, i.e. 1/3 to 1/4 synthesized beam).
 - Map size: MAP_SIZE (in pixels, default: 0, *i.e.* \sim twice primary beam size).
- Weighting:
 - kind: WEIGHT_MODE
 (Possibilities: NATURAL/UN. Default: NATURAL).
 - Size of uv plane cell and robust threshold: uv_CELL (Defaults: 7.5 m, 1).
- Tapering: Gaussian taper parameters UV_TAPER (in m and degree, default: 0, i.e. no tapering).

From Calibrated Visibilities to Images: Summary

Fourier Transform and Deconvolution: The two key issues in imaging.

Stage	Implementation
Calibrated Visibilities	
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Physical information	
on your source	

Deconvolution: I. Philosophy

$$I_{\text{meas}} = B_{\text{dirty}} * \{B_{\text{primary}}.I_{\text{source}}\} + N.$$

Information lost:

- Irregular, incomplete sampling \Rightarrow convolution by B_{dirty} ;
- Noise ⇒ Low signal structures undetected.
- \Rightarrow 1. Impossible to recover the intrinsic source structure!
- \Rightarrow 2. Infinite number of solutions!

$$\begin{cases} S \text{ solution } (i.e. \ I_{\text{meas}} = B_{\text{dirty}} * S + N) \\ B_{\text{dirty}} * R = 0 \end{cases} \Rightarrow (S+R) \text{ solution.}$$

Deconvolution: I. Philosophy (continued)

$$I_{\text{meas}} = B_{\text{dirty}} * \{B_{\text{primary}}.I_{\text{source}}\} + N.$$

Information lost:

- \Rightarrow 1. Impossible to recover the intrinsic source structure!
- \Rightarrow 2. Infinite number of solutions!

Deconvolution goal: Finding a sensible intensity distribution compatible with the intrinsic source one.

Deconvolution needs:

- Some *a priori* assumptions about the source intensity distribution;
- As much as possible knowledge of
 - $-B_{dirty}$ (OK in radioastronomy);
 - Noise properties.

The best solution: A Gaussian $B_{\text{dirty}} \Rightarrow \text{No deconvolution needed!}$

Deconvolution: II. MEM principle

a priori assumptions: Smoothed and positive intensity.

Idea:

"Select from the images that agree with the measured visibilities to within the noise level the one that maximizes entropy."

Algorithm:

• Entropy:

$$S = -\sum_{ij} I_{ij} \log(I_{ij}/M_{ij})$$
 with $M =$ first guess image.

• Constraint:

$$\sum_k \frac{|V(u_k,v_k)-\tilde{I}(u_k,v_k)|^2}{\sigma_k^2} = \text{number of visibilities}$$
 with $\tilde{I}=2\text{D FT}(I)$.

Deconvolution: II. MEM properties

Advantages:

- Fast: Computational load $\propto N \ln(N)$ with N = number of pixels.
- Easy to generalize (Arrays with different antenna diameters).
- Flatten low-level extended emission.
- Resolve peaks.

Inconvenients:

- Angular resolution increases with peak height.
- Unable to clean ripples (e.g. point source sidelobes) in extended emission.
- Biased residuals:
 - ⇒ Noise increase and spurious emission at low signal.
- Impossibility to deal with absorption features.
- ullet Poor performance with limited uv coverage
 - \Rightarrow Not used at PdBI.

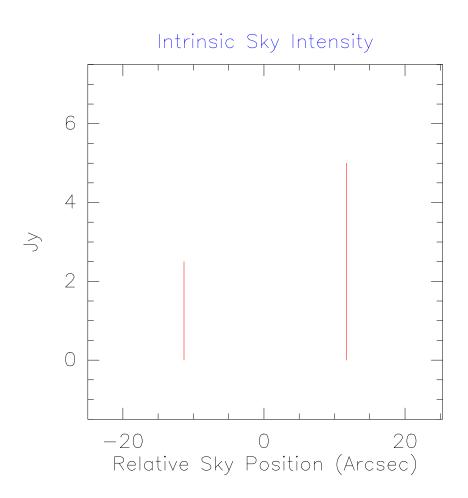
Deconvolution: III. The Basic CLEAN Algorithm

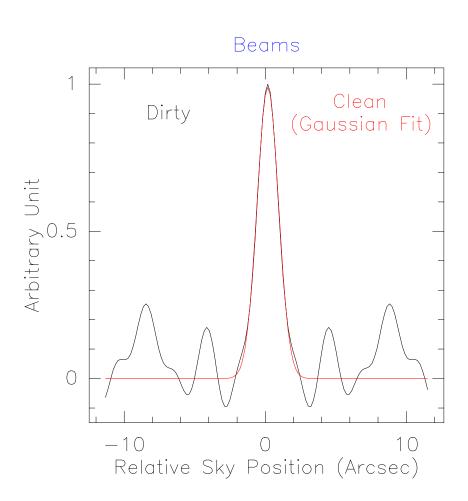
a priori assumption: Source = Collection of point sources.

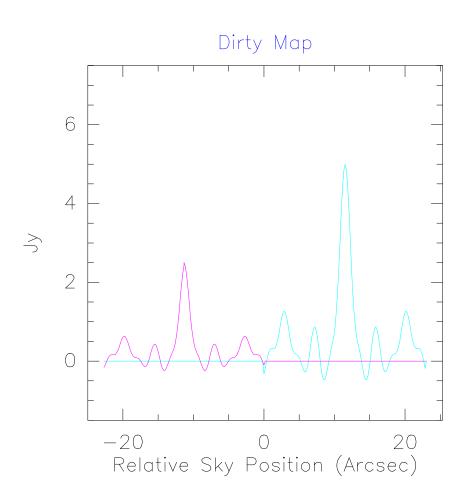
Idea: "Matching pursuit".

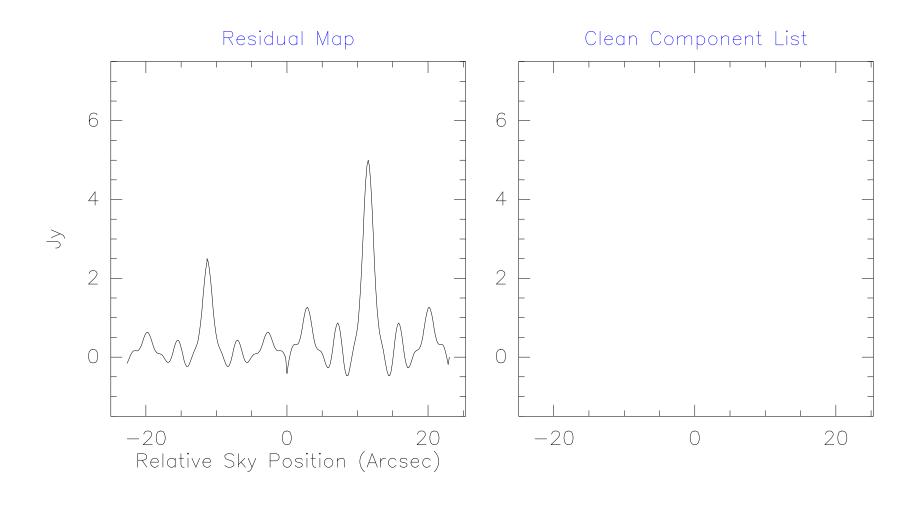
Algorithm:

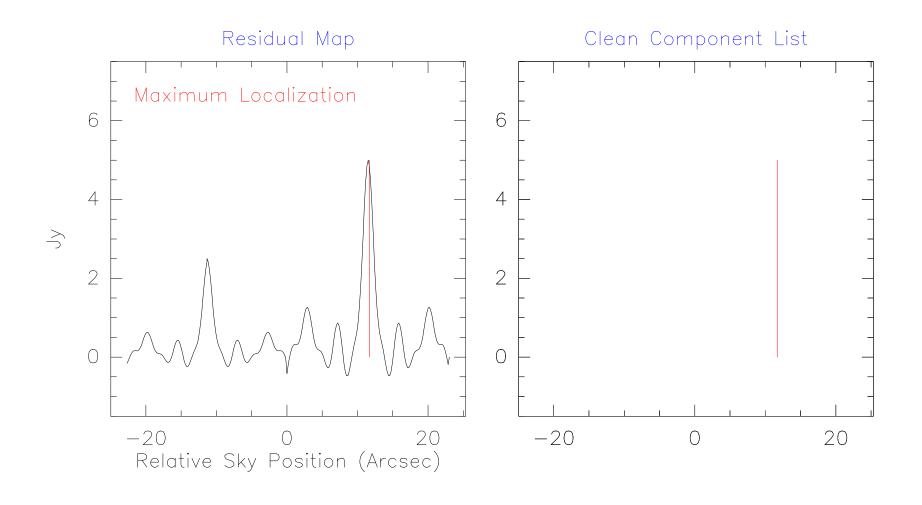
- 1 Initialize
 - the residual map to the dirty map;
 - the Clean component list to an empty (NULL) value;
- 2 Identify pixel of $|I_{max}|$ in residual map as a point source;
- 3 Add $\gamma.I_{\text{max}}$ to clean component list;
- 4 Subtract $\gamma.I_{max}$ from residual map;
- 5 Go back to point 2 while stopping criterion is not matched;
- 6 Convolution by Clean beam (a posteriori regularization);
- 5 Addition of residual map to enable:
 - Correction when cleaning is too superficial;
 - Noise estimation.

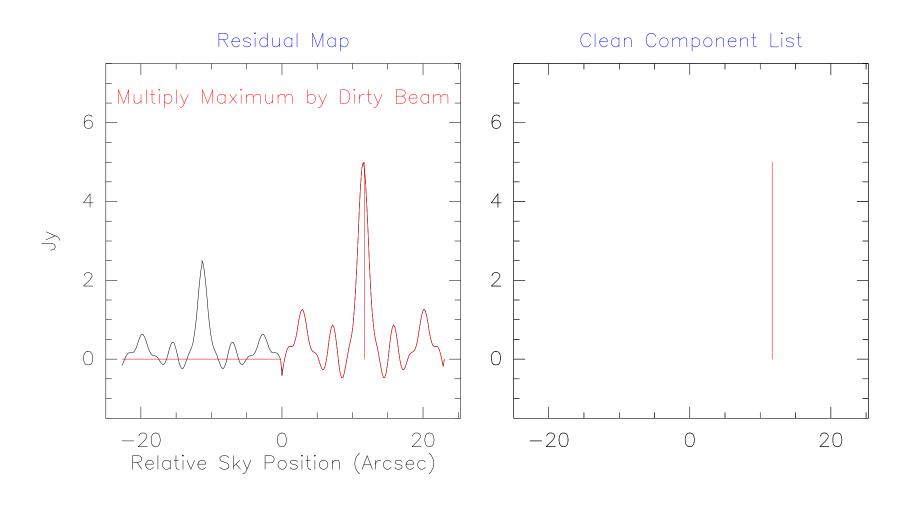


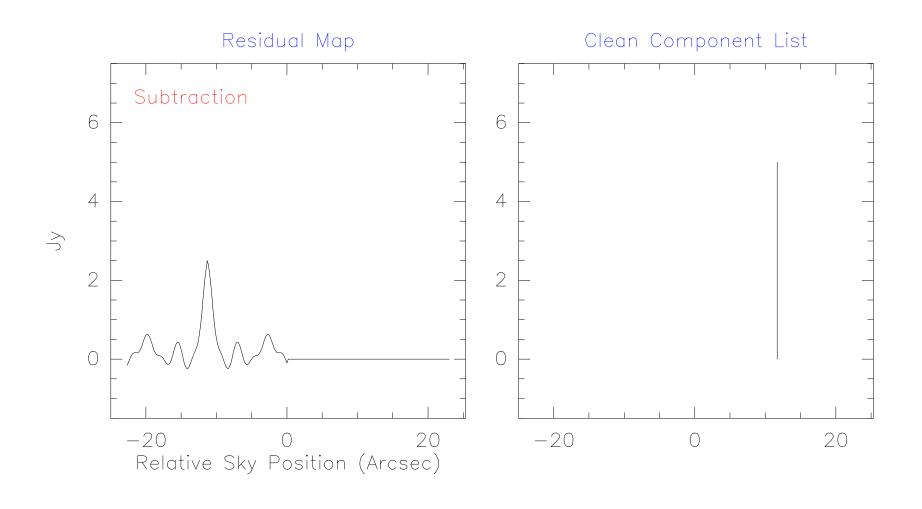


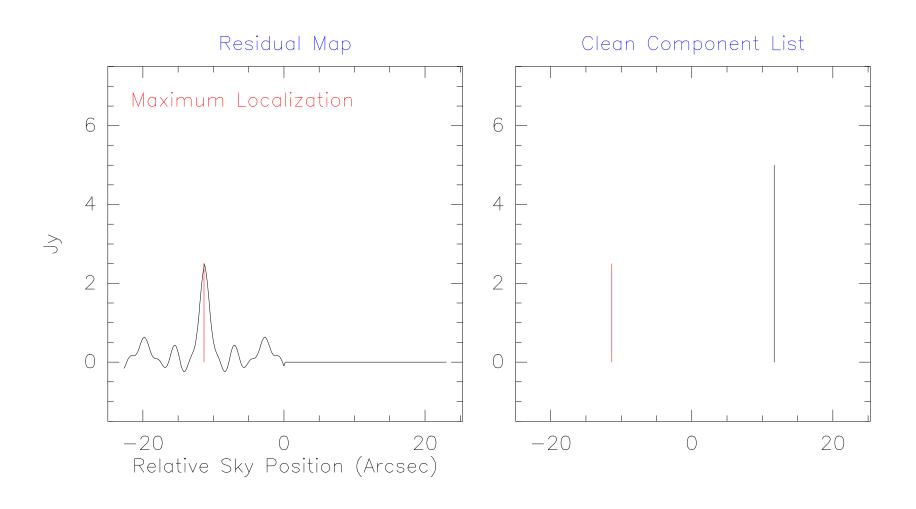


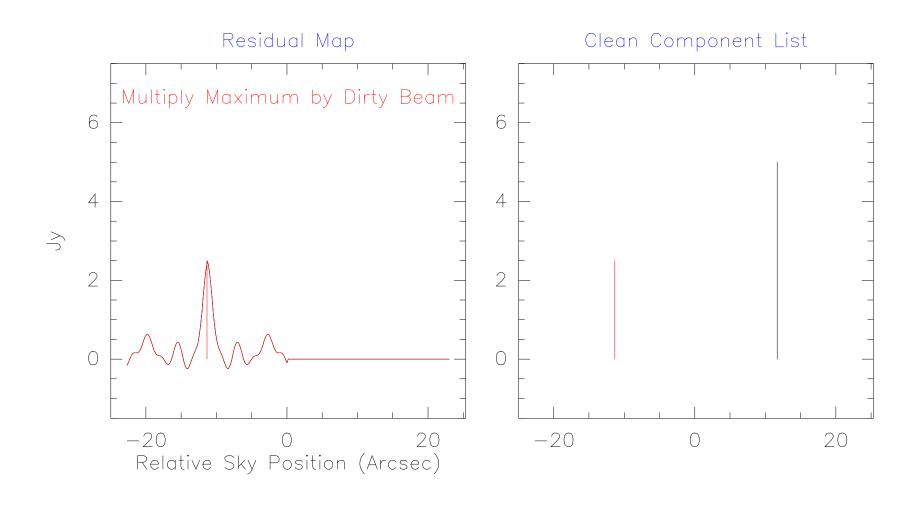


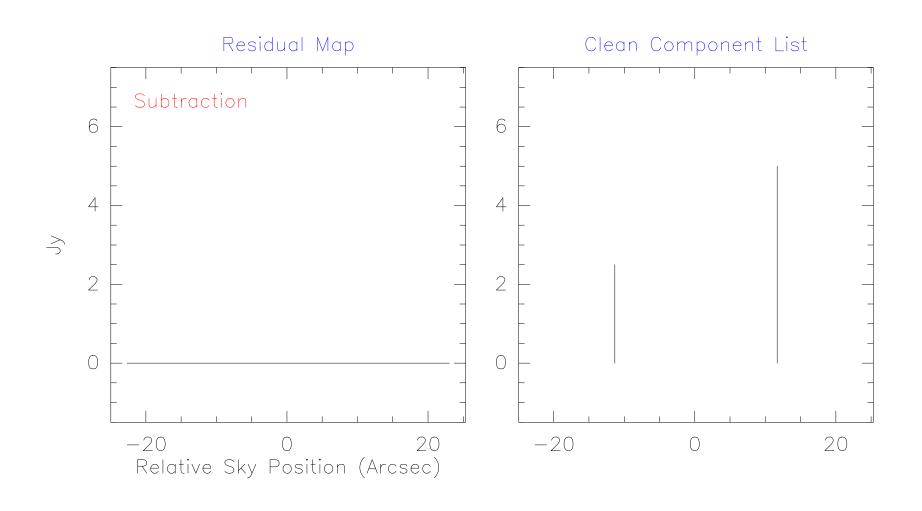


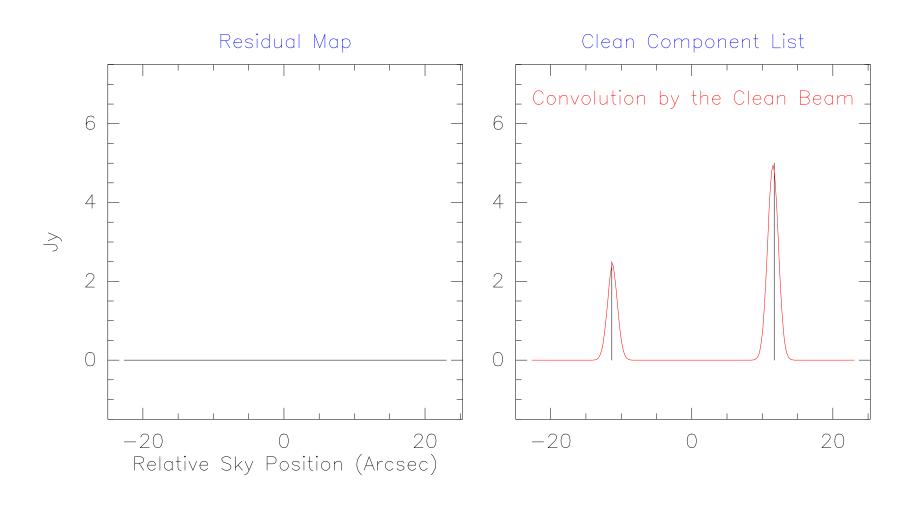


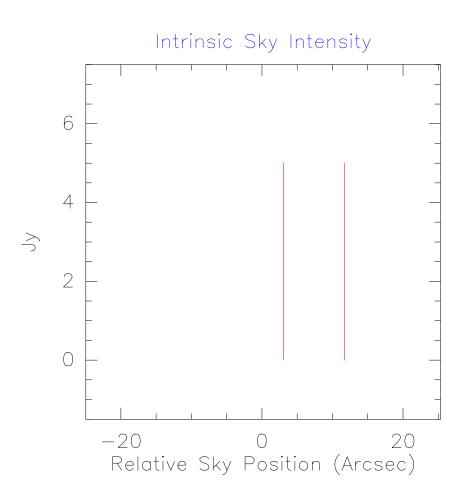


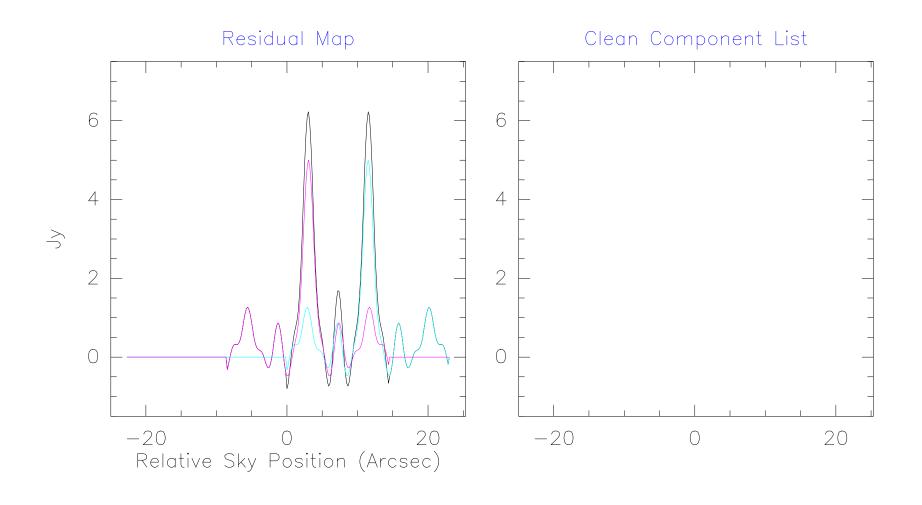


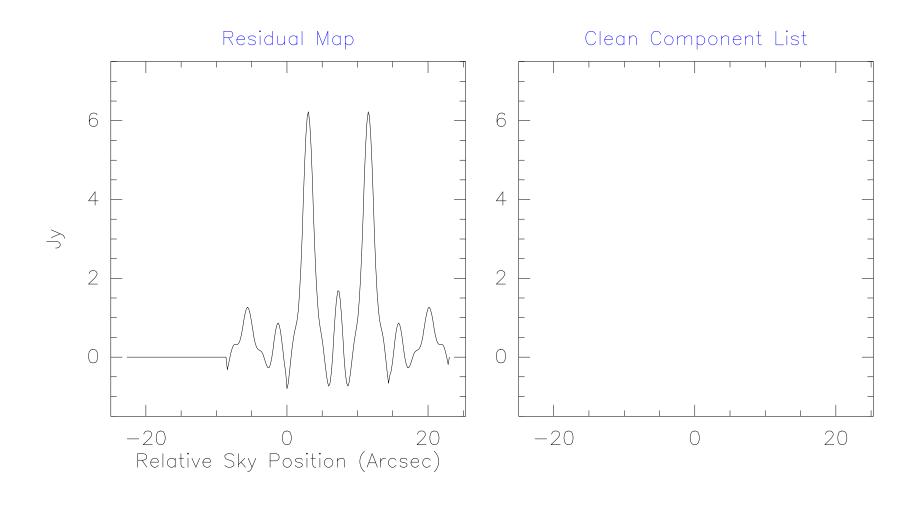


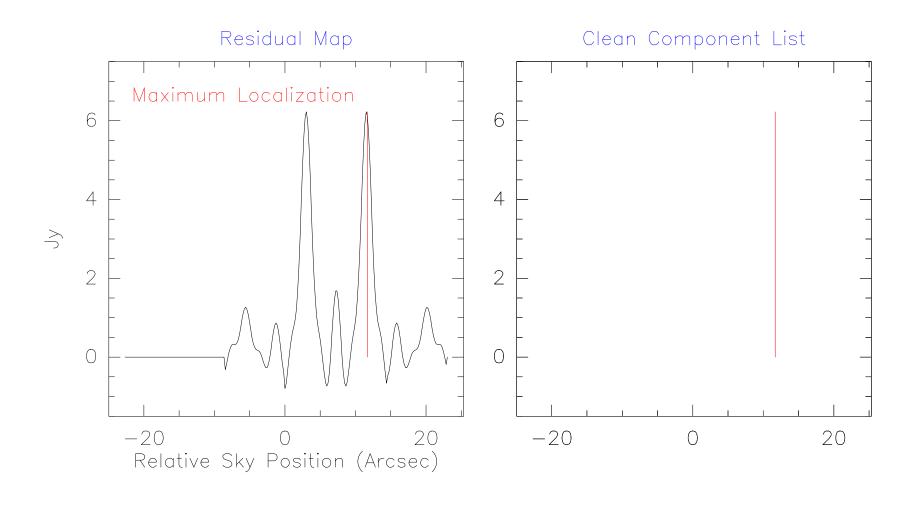


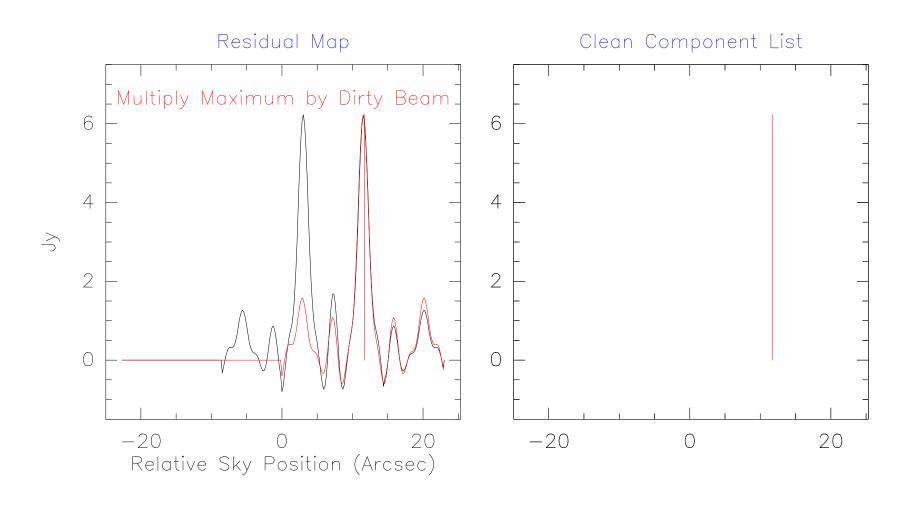


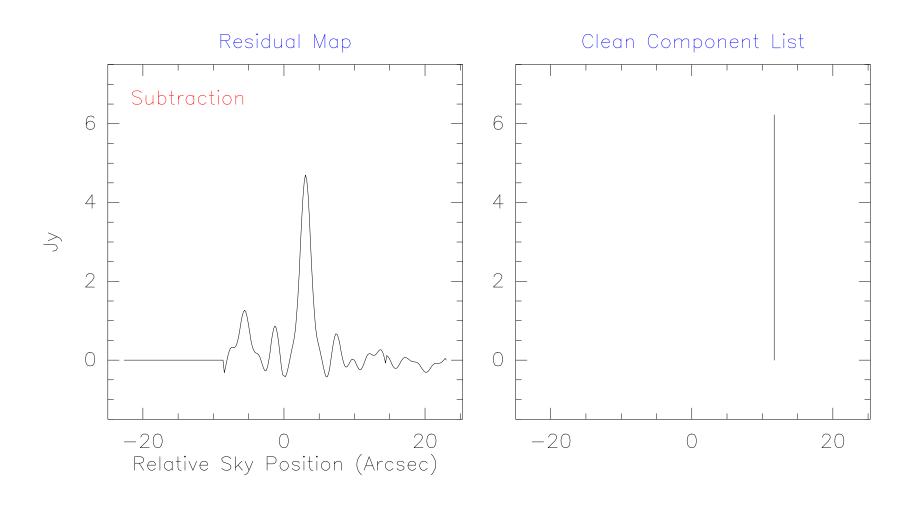


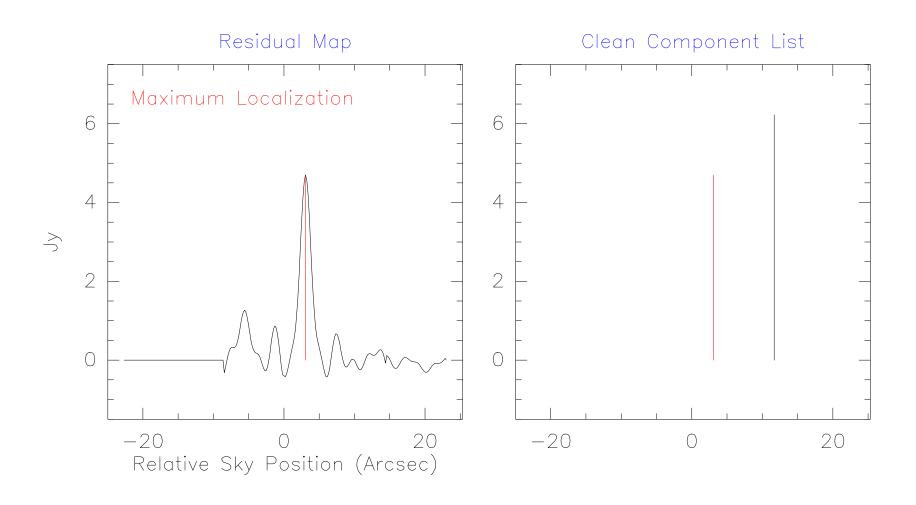


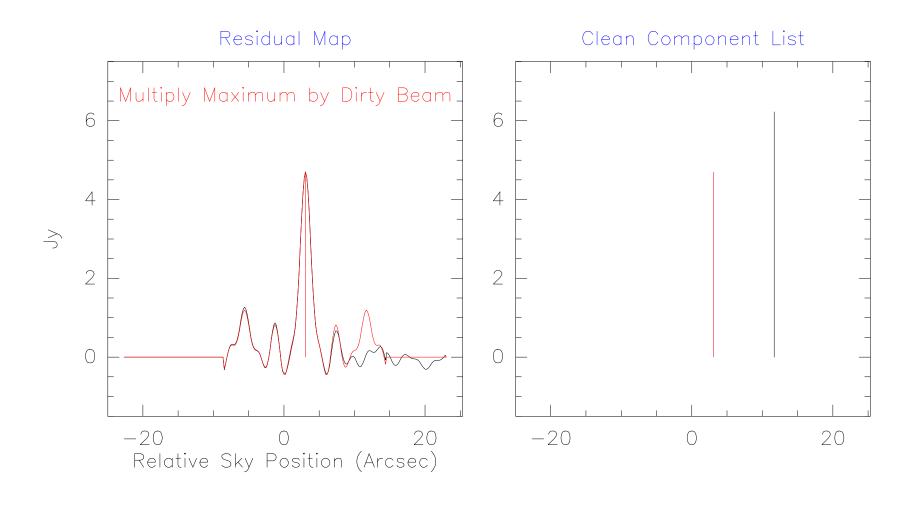


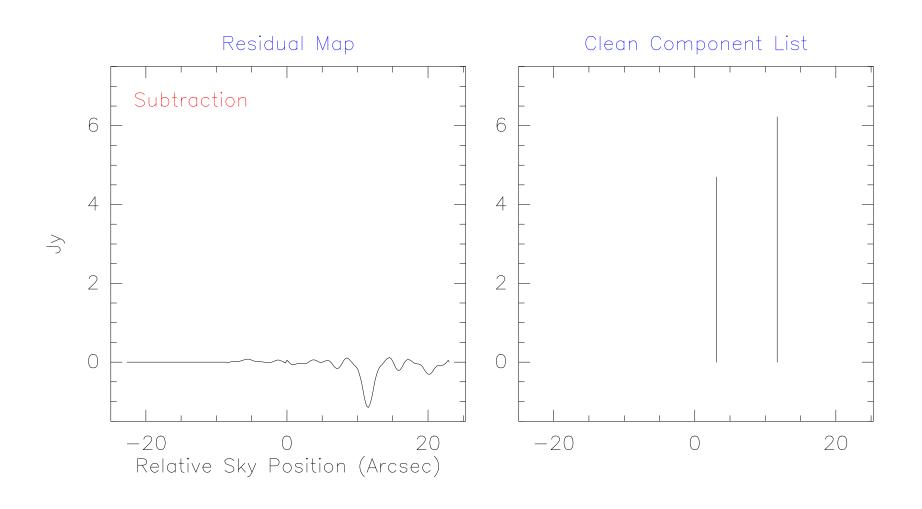


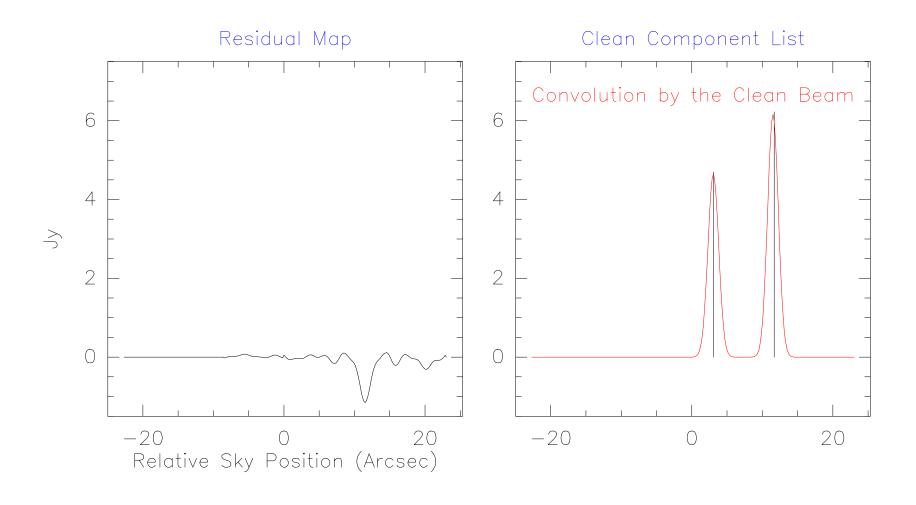






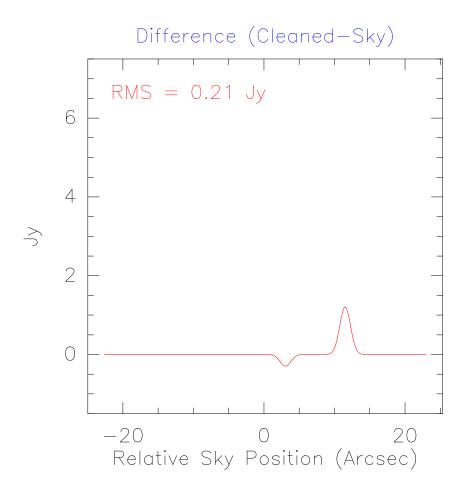




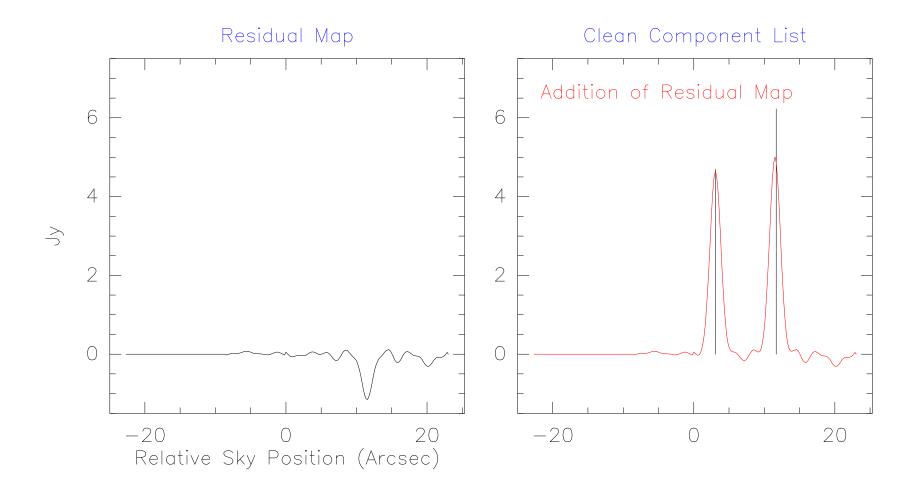


Convergence:

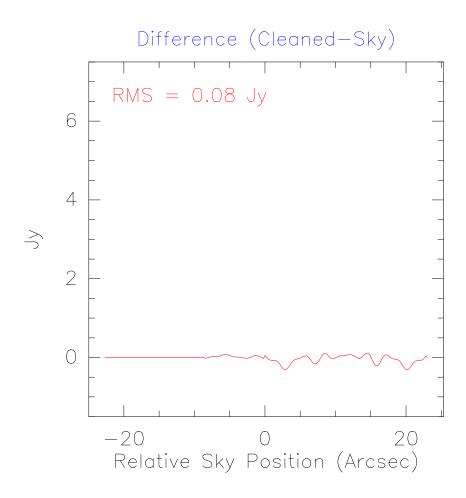
Too superficial cleaning \Rightarrow Approximate results. Too deep cleaning \Rightarrow Divergence.



Addition of residual map: Improvement when convergence not reached; Noise estimation.



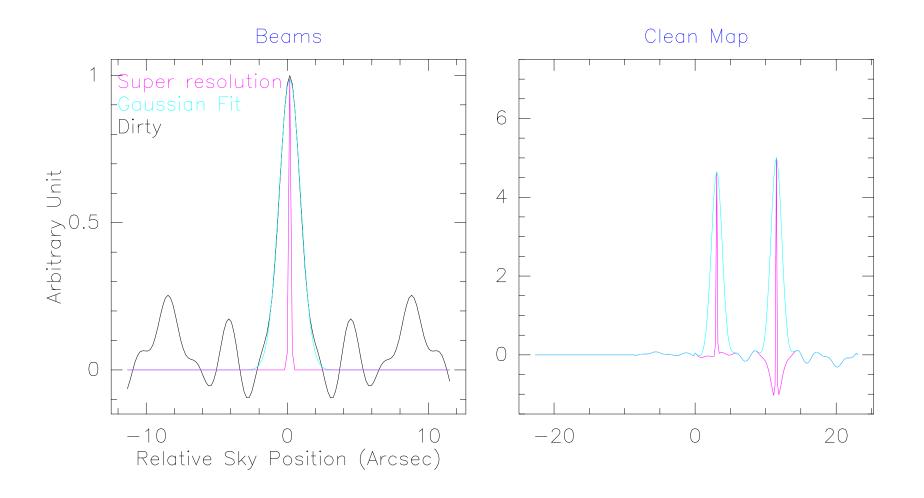
Addition of residual map: Improvement when convergence not reached; Noise estimation.

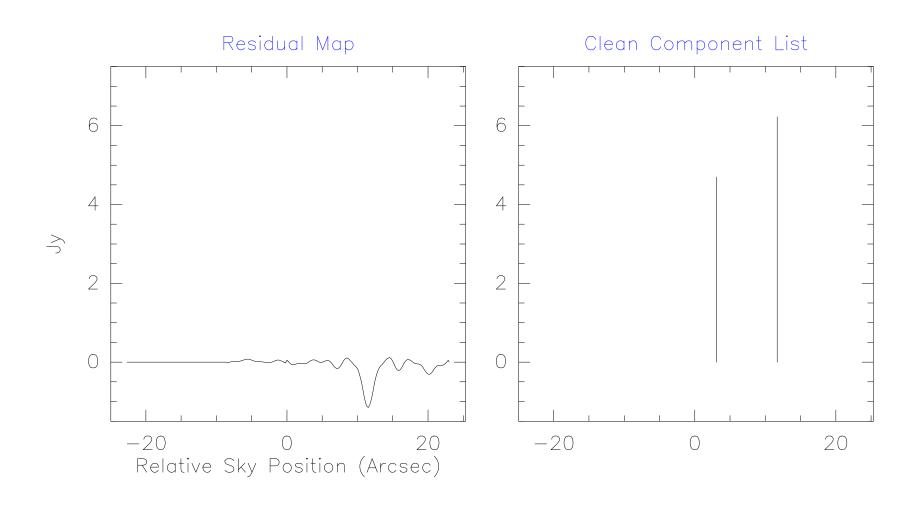


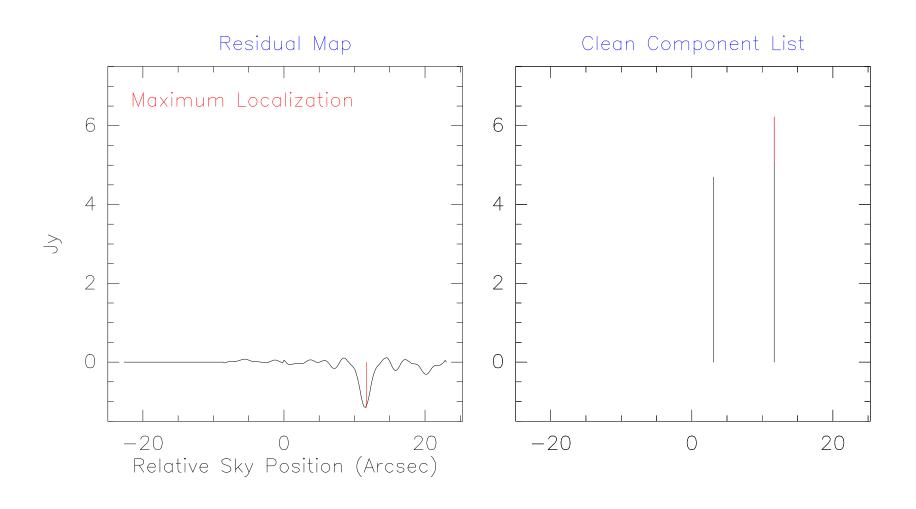
Choice of clean beam:

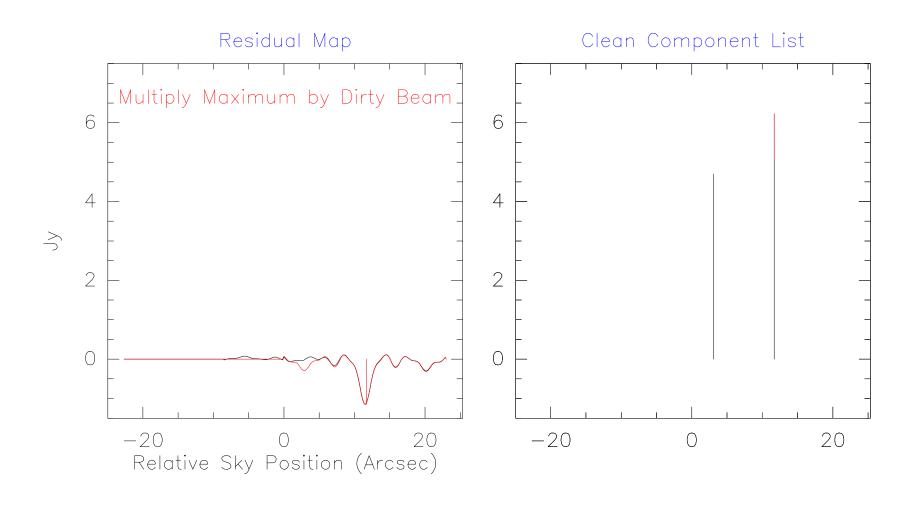
Gaussian of FWHM matching the synthesized beam size.

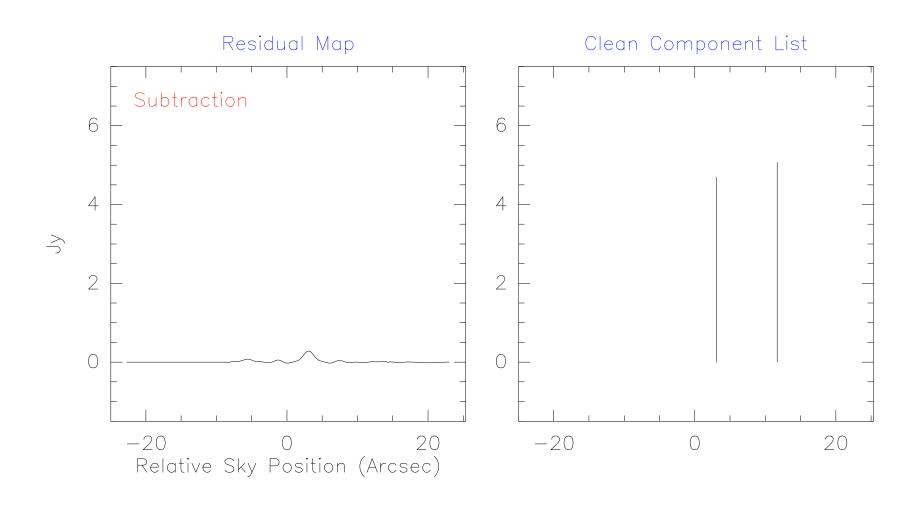
⇒ Super resolution strongly discouraged.

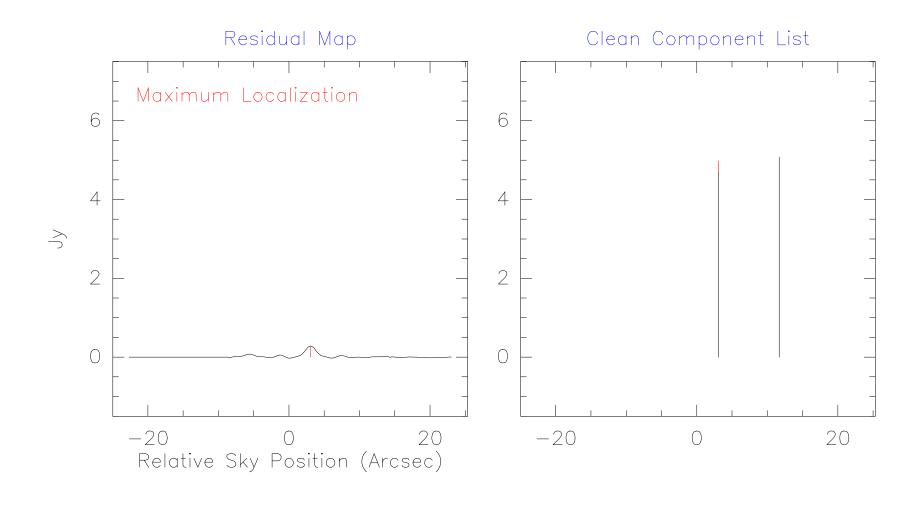


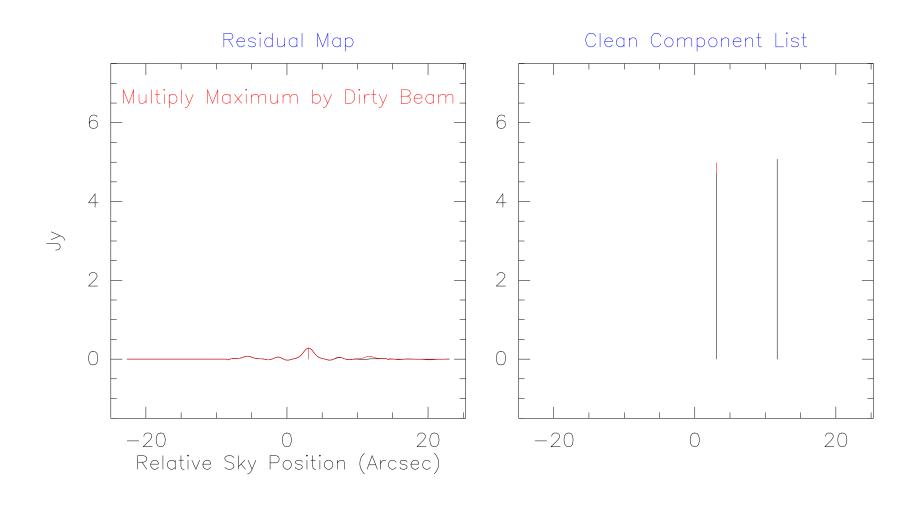


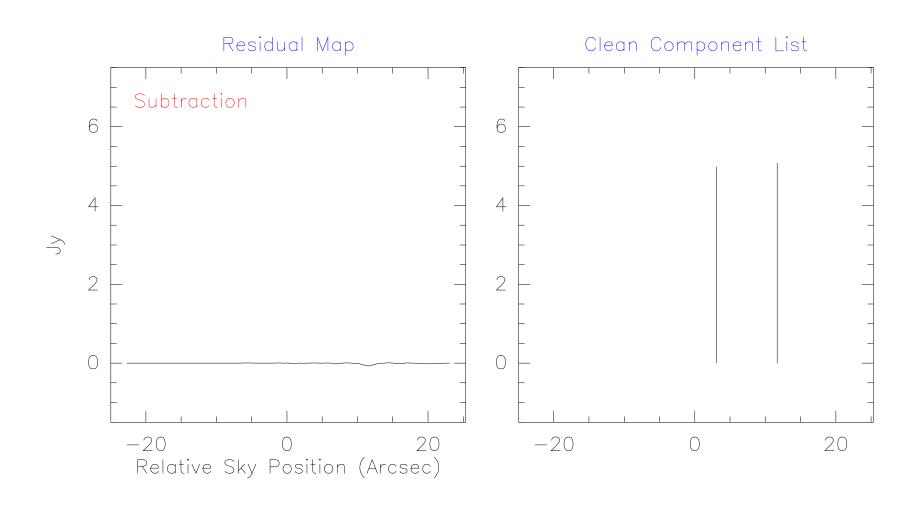


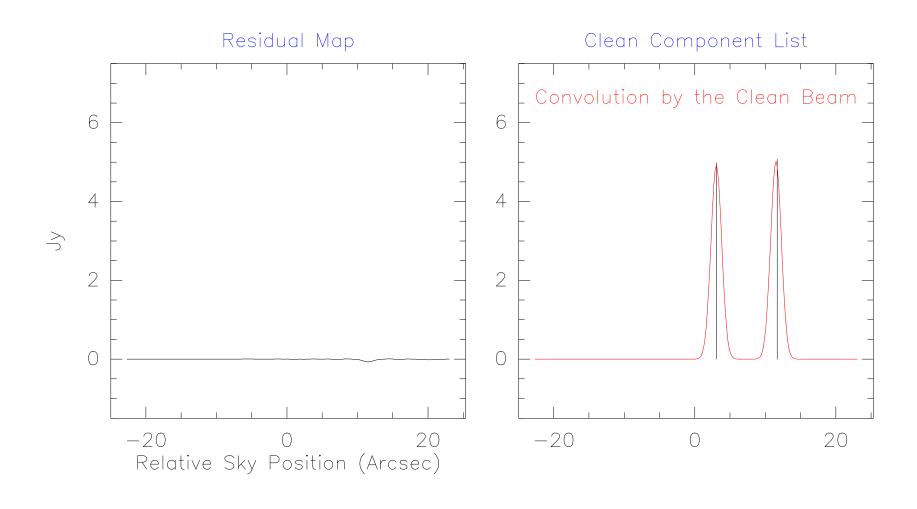


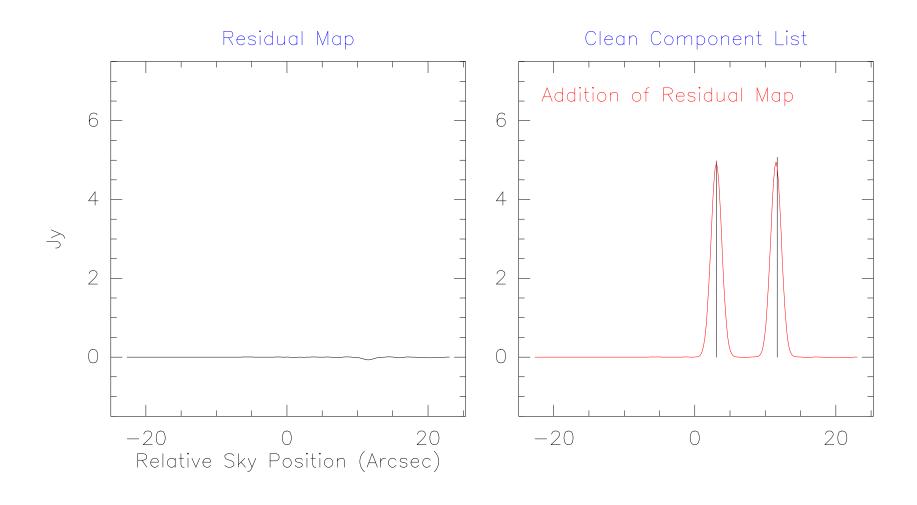


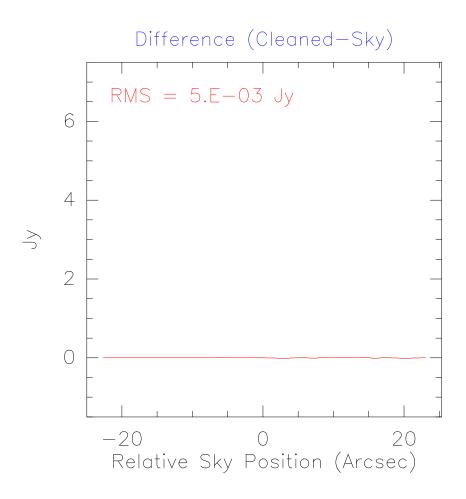






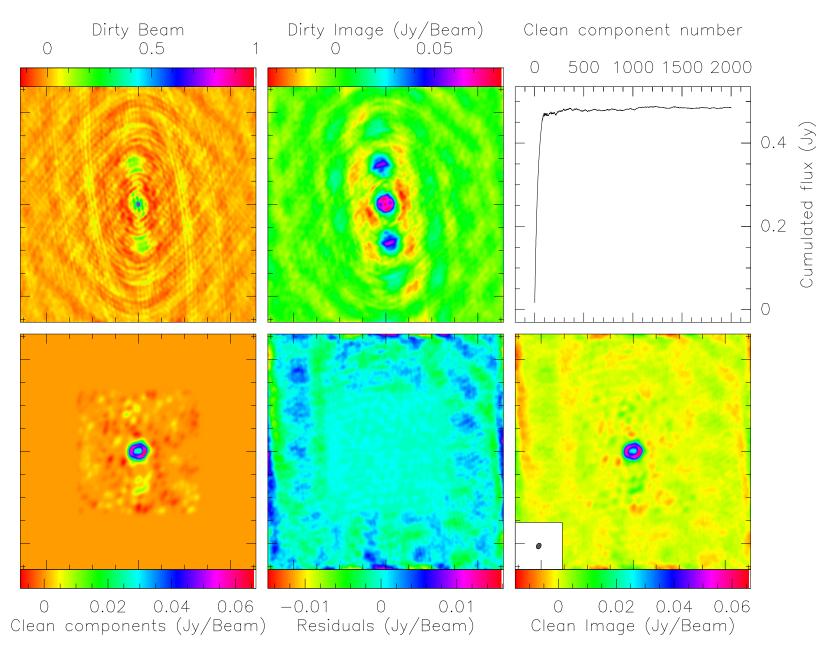




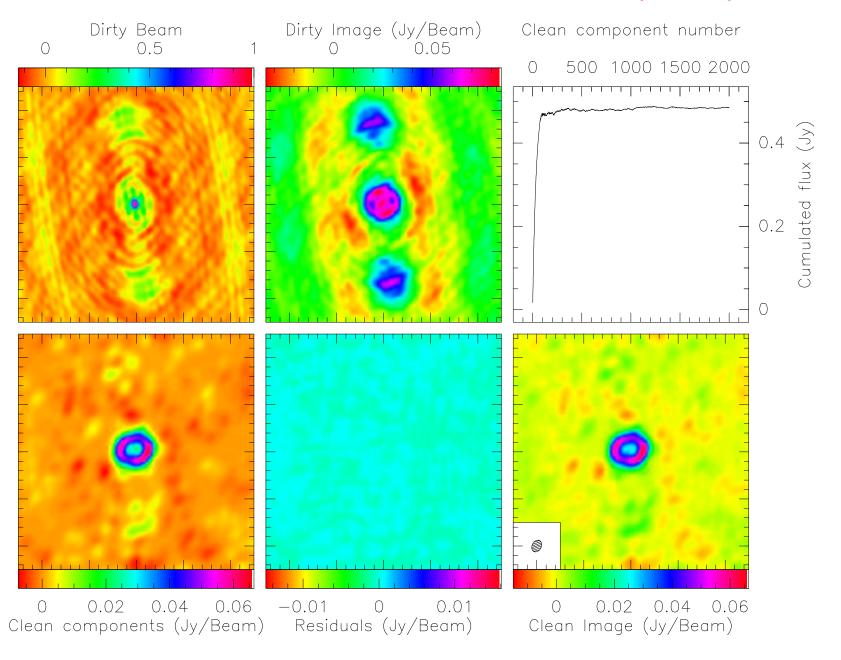


- Stopping criterions:
 - Total number of Clean components;
 - $-|I_{\text{max}}| < \text{fraction of noise (when noise limited)};$
 - $-|I_{\text{max}}| < \text{fraction of dirty map max (when dynamic limited)}.$
- Loop gain: Good results when $\gamma \sim 0.1 0.3$.
- Cleaned region: Only the inner quarter of the dirty image.
- Support: Definition of a region where CLEAN components are searched.
 - A priori information \Rightarrow Help CLEAN convergence.
 - But bias if support excludes signal regions
 ⇒ Be wise!

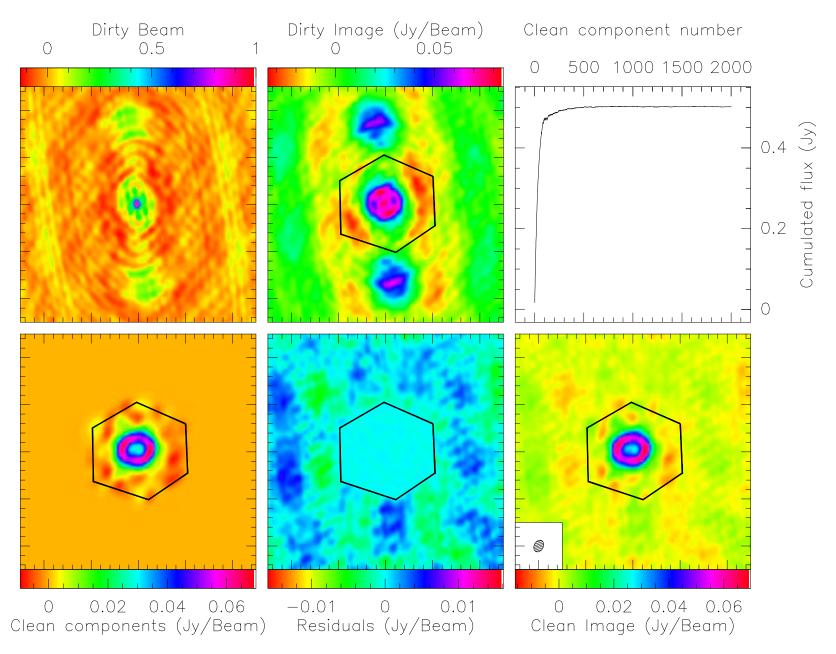
Deconvolution: III. The Basic Clean Algorithm 5. A True Example without support



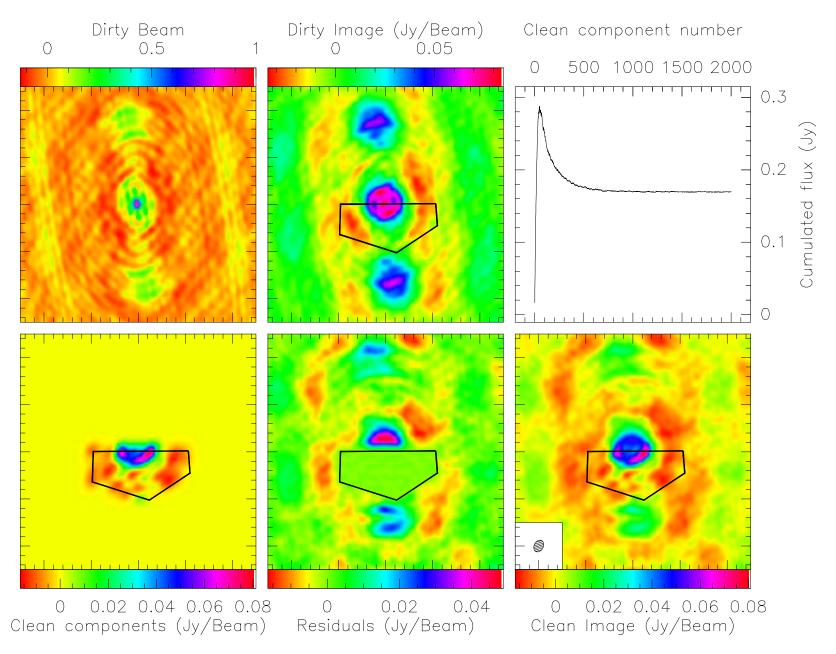
Deconvolution: III. The Basic Clean Algorithm 5. A True Example without support (zoom)



Deconvolution: III. The Basic Clean Algorithm 5. A True Example with right support



Deconvolution: III. The Basic Clean Algorithm 5. A True Example with wrong support



Deconvolution: IV. CLEAN Variants

Basic:

• HOGBOM (Hogböm 1974)
Robust but slow.

Faster Search Algorithms:

- CLARK (Clark 1980)
 Fast but instable (when sidelobes are high).
- MX (Cotton& Schwab 1984)

 Better accuracy (Source removal in the uv plane), but slower (gridding steps repeated).

Deconvolution: IV. CLEAN Variants (continued)

Better Handling of Extended Sources:

- SDI (Steer, Dewdney, Ito 1984) Created to minimize stripes.
- MRC (Multi-Resolution Clean by Wakker & Schwarz 1988) Simple multi-resolution approach.
- MULTI (Multi-Scale Clean by Cornwell 1998)
 Complex multi-resolution approach.

In practice: Exotic use at PdBI!

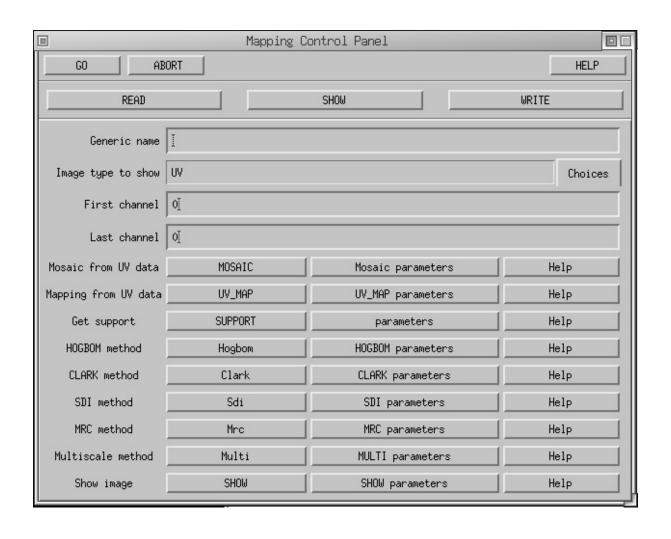
Deconvolution: IV. GILDAS Implementation 1. MAPPING Command Line

MAPPING> INPUT CLEAN: display CLEAN control parameters.

- Loop gain: GAIN (default: 0.2).
- Stopping criterions:
 - Maximum number of iterations: NITER (default: 100).
 - Maximum residual amplitude, expressed as fraction of peak intensity: FRES (default: 0.05).
 - Maximum residual amplitude, in map units (Jy/Beam):
 ARES (default: 0).
- Support: BLC and TRC are the Bottom Left Corner and Top Right Corner of a square support in pixel units (default: 0, *i.e.* no support).
- Gaussian clean beam parameters: MAJOR, MINOR, ANGLE (Default: 0, *i.e.* Fit dirty beam).

Deconvolution: IV. GILDAS Implementation

2. MAPPING Window Interface



Deconvolution: IV. Recommended Practices

- Method: Start with CLARK and turn to HOGBOM in case of problems.
- Support:
 - Start without one.
 - Define one on your first clean image if really needed (i.e. difficulties of convergence).
- Stopping criterion:
 - Use a large enough number of iterations to ensure convergence.
 - Clean down to the noise level unless a very strong source is present.
- Misc: Consult an expert until you become one.

Typical MAPPING session

Look at the mapping-tutorial.map procedure for details.

```
MAPPING> read uv 1mm
MAPPING> show uv
MAPPING> input uv_map
MAPPING> uv_map
MAPPING> show beam
MAPPING> show dirty 1mm
MAPPING> write beam 1mm
MAPPING> write dirty
MAPPING> input clean
MAPPING> hogbom /flux 0 1
MAPPING> show clean
MAPPING> show residual
MAPPING> write clean 1mm
MAPPING> write residual 1mm
MAPPING> exit
```

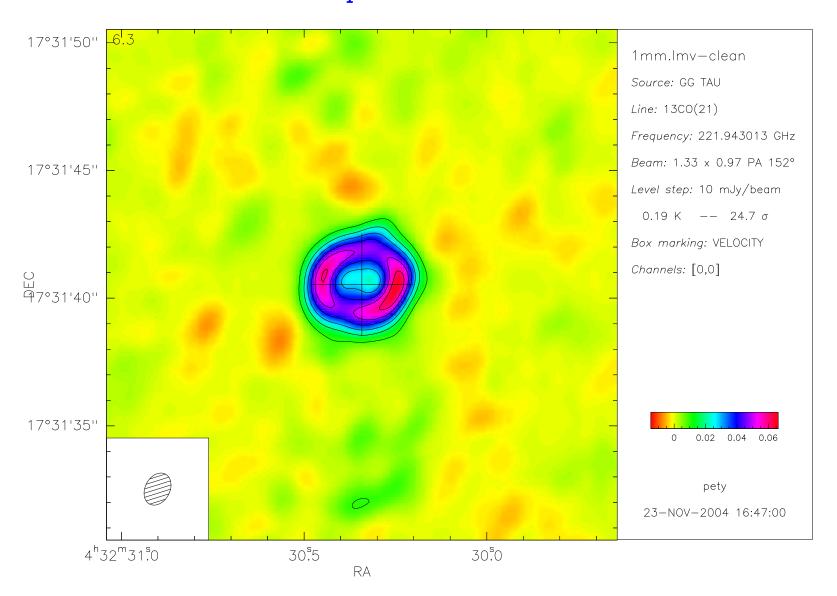
Visualization and Image Analysis

Fourier Transform and Deconvolution: The two key issues in imaging.

Stage	Implementation
Calibrated Visibilities	
↓ Fourier Transform	UV_STAT, UV_MAP
Dirty beam & image	
↓ Deconvolution	HOGBOM, CLARK
Clean beam & image	
↓ Visualization	GO BIT, GO VIEW
↓ Image analysis	GO NOISE, GO FLUX, GO MOMENTS
Physical information	
on your source	

Visualization: I. GO BIT for continuum

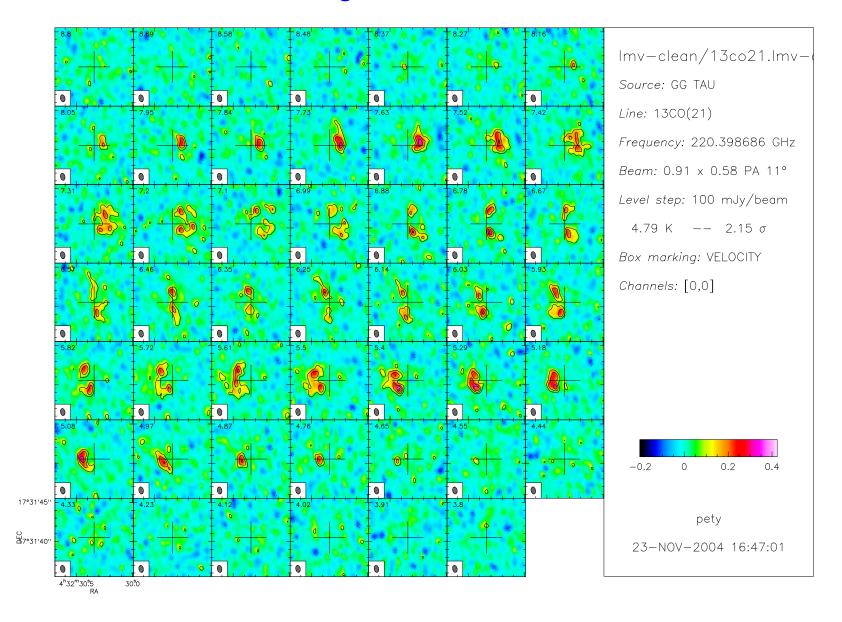
MAPPING> let name 1mm
MAPPING> let type lmv-clean
MAPPING> go bit
MAPPING> input bit



Visualization: II. GO BIT for spectra

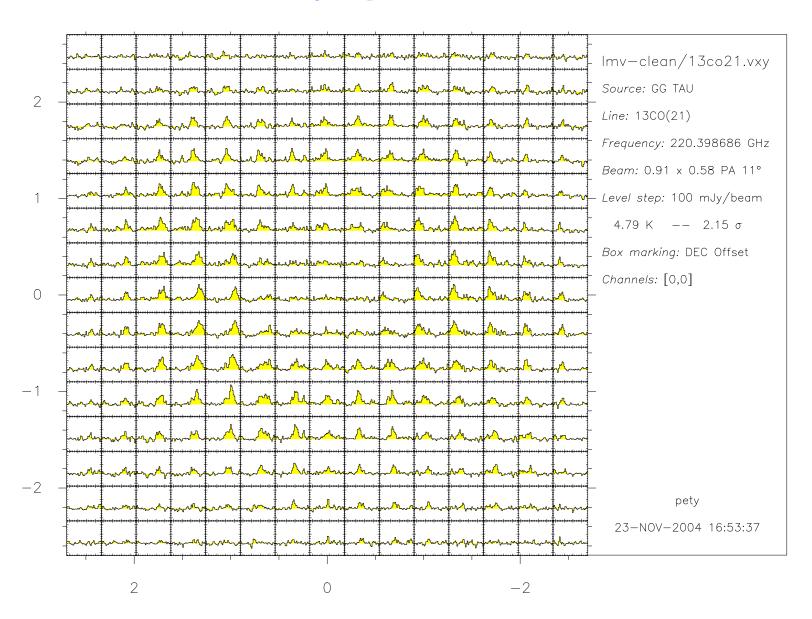
MAPPING> let name 13co21
MAPPING> let type lmv-clean

MAPPING> go bit



Visualization: III. GO SPECTRUM for spectra

MAPPING> let name 13co21 MAPPING> let type lmv-clean MAPPING> go spectrum

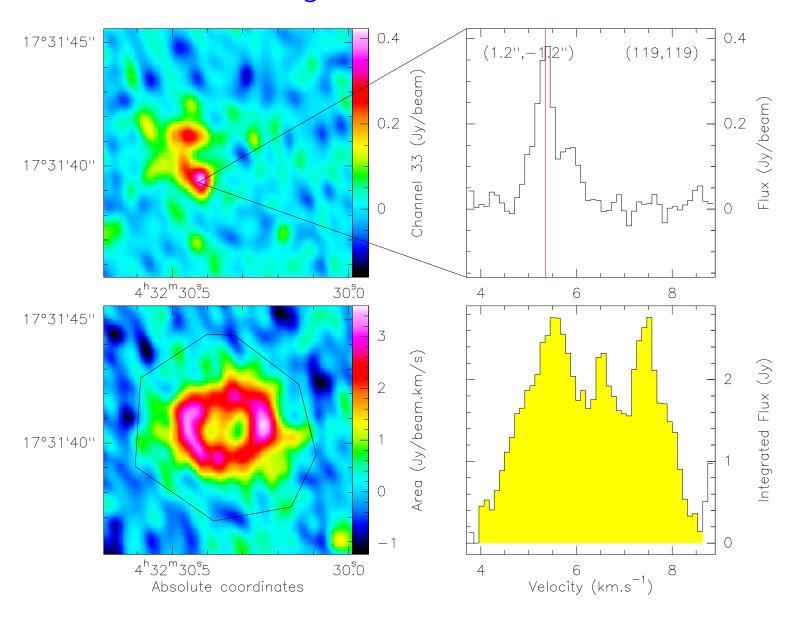


Visualization: IV. GO VIEW for spectra

MAPPING> let name 13co21

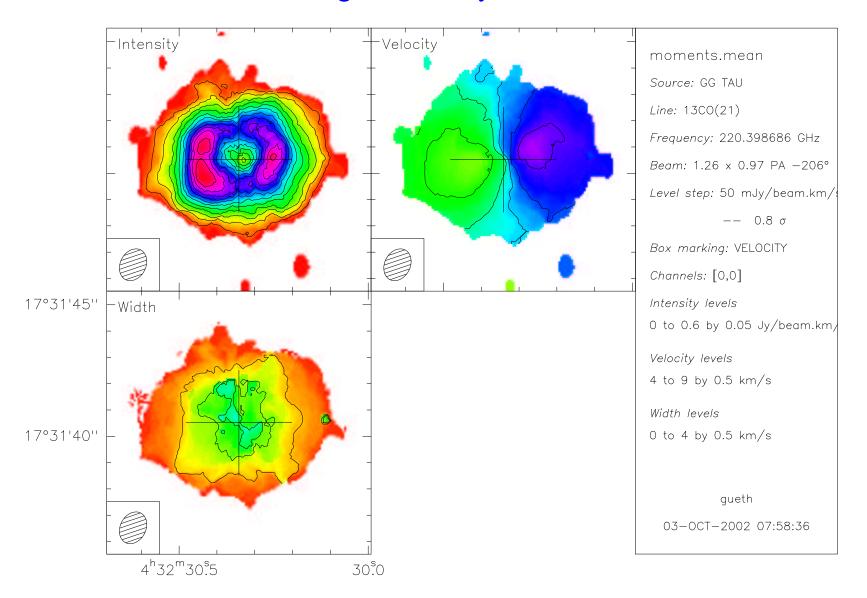
MAPPING> let type lmv-clean

MAPPING> go view



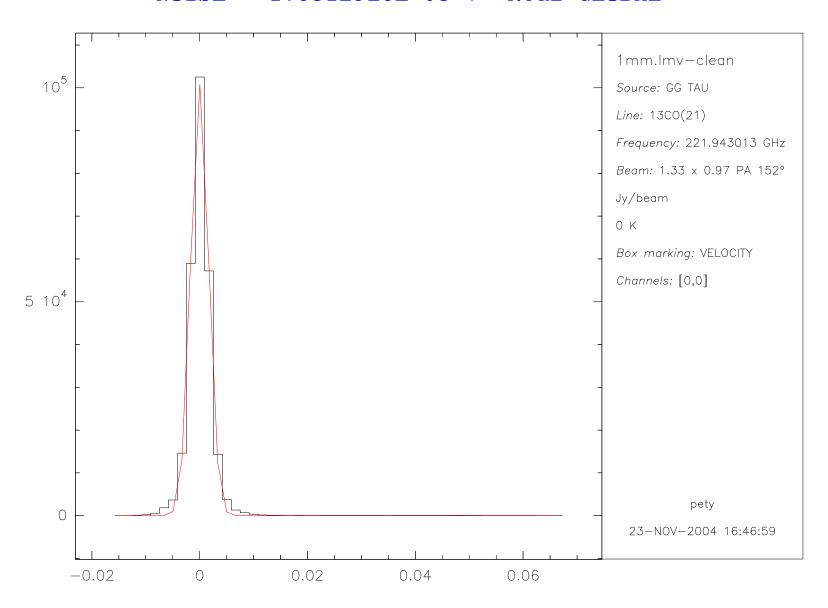
Analysis: I. Moment Estimation with GO MOMENT + GO VELOCITY

```
MAPPING> let name 13co21
MAPPING> let type lmv-clean
MAPPING> go moments
MAPPING> go velocity
```



Analysis: II. Noise Estimation with GO NOISE

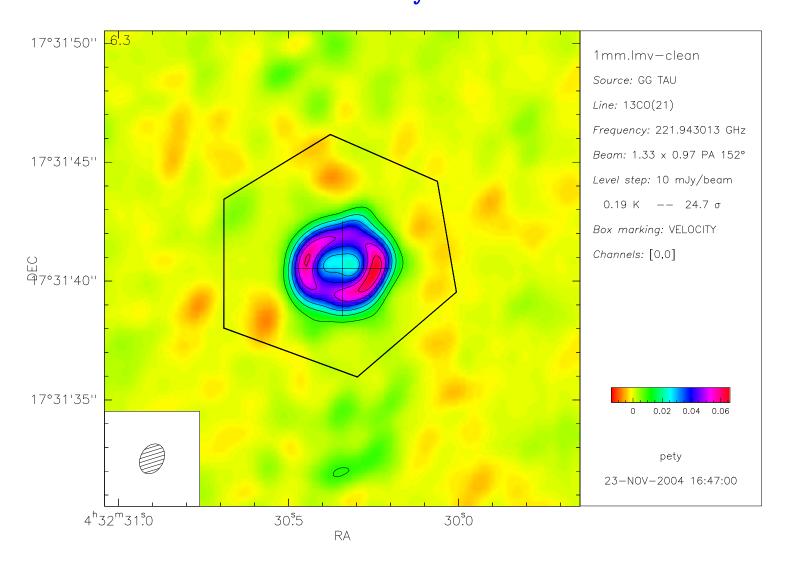
```
MAPPING> let name 1mm
MAPPING> let type lmv-clean
MAPPING> go noise
NOISE = 1.6312926E-03 ! Real GLOBAL
```



Imaging, Deconvolution & Image Analysis

Analysis: III. Flux Estimation with GO FLUX

```
MAPPING> let name 1mm
MAPPING> let type lmv-clean
MAPPING> go bit
MAPPING> go flux
Total Flux 461 mJy
```



Photometry: I Generalities

- Brightness = Intensity (e.g. Power = $I_{\nu}(\alpha, \beta) dA d\Omega d\nu$)
- Flux unit: $1 \text{ Jy} = 10^{-26} \text{ W m}^{-2} \text{ Hz}^{-1}$.
- Source flux measured by a single-dish antenna: $F_{\nu} = B * I_{\nu}$ with B the antenna beam.
- Relationship between measured flux and temperature scales:

$$T_A=rac{\lambda^2}{2k\Omega_A}F_
u$$
, $T_A^\star=rac{\lambda^2}{2k\Omega_{2\pi}}F_
u$ and $T_{mb}=rac{\lambda^2}{2k\Omega_{mb}}F_
u$ because

- $-P_{\nu}=\frac{1}{2}A_{e}F_{\nu}$ Power detected by the single-dish antenna.
- $-P'_{\nu}=kT$ Power emitted by a resistor at temperature T.

$$-P_{\nu}=P_{\nu}'\Rightarrow T_{A}=\frac{A_{e}}{2k}F_{\nu}.$$

$$-\lambda^2 = A_e \Omega_A$$
 (diffraction).

$$-\Omega_{2\pi} = F_{\text{eff}}\Omega_A$$
 or $F_{\text{eff}} = \frac{\text{Forward beam}}{\text{Total beam}}$.

$$-\Omega_{mb} = B_{\text{eff}}\Omega_A$$
 or $B_{\text{eff}} = \frac{\text{Main beam}}{\text{Total beam}}$.

Photometry: II Visibilities

Visibility unit: Jy because:

$$V = 2D FT \{B_{\text{primary}}.I_{\text{source}}\}$$
$$= \iint B_{\text{primary}}(\sigma).I_{\text{source}}(\sigma) \exp(-i2\pi \mathbf{b}.\sigma/c)d\Omega.$$

Effect of flux calibration errors on your image:

- Multiplicative factor if uniform in uv plane.
- Convolution (i.e. distorsion) else.

Photometry: III Dirty map

III—defined because:

- $S(u = 0, v = 0) = 0 \Rightarrow$ Area of the dirty beam is 0!
- $V(u = 0, v = 0) = 0 \Rightarrow$ Total flux of the dirty image is 0! \Rightarrow A source of constant intensity will be fully filtered out.
- A single point source of 1 Jy appears with peak intensity of 1.
- Several close-by point sources of 1 Jy appears with peak intensities different of 1.

Photometry: IV Clean map (my dream: Don't take it seriously)

 $I_{\rm Clean} = \frac{1}{\Omega_{\rm Clean}} \left(B_{\rm Clean} * I_{\rm point} \right)$: *i.e.* convolution of a set of point sources (mimicking the sky intensity distribution) by the clean beam.

Behavior: Brightness, *i.e.* Source flux measured in a given solid angle (*i.e.* clean beam).

Unit: Jy/sr

Consequences:

• Source flux computation by integration inside a support:

Flux =
$$\sum_{ij \in \mathcal{S}} I_{\mathsf{clean}} \ d\Omega$$
 [Jy] [Jy/sr] [sr]

with $d\Omega$ the image pixel surface.

• From Brightness to temperature: $T_{\text{clean}} = \frac{\lambda^2}{2k} I_{\text{clean}}$

Photometry: IV Clean map (reality)

 $I_{\text{clean}} = B_{\text{clean}} * I_{\text{point}}$: *i.e.* convolution of a set of point sources (mimicking the sky intensity distribution) by the clean beam.

Behavior: Brightness, *i.e.* Source flux measured in a given solid angle (*i.e.* clean beam).

Unit: Jy/beam with 1 beam = Ω_{clean} sr.

Consequences:

• Source flux computation by integration inside a support:

Flux =
$$\sum_{ij \in \mathcal{S}} I_{\text{clean}}$$
 . $\frac{d\Omega}{\Omega_{\text{clean}}}$ [Jy] [Jy/beam] [beam]

with $\frac{d\Omega}{\Omega_{\rm clean}}$ the nb of beams in the surface of an image pixel.

• From Brightness to temperature: $T_{\rm clean} = \frac{\lambda^2}{2k\Omega_{\rm clean}} I_{\rm clean}$

Photometry: IV Clean map

Consequences of a Gaussian clean beam shape:

- No error beams, no secondary beams.
- \bullet T_{clean} is a main beam temperature.

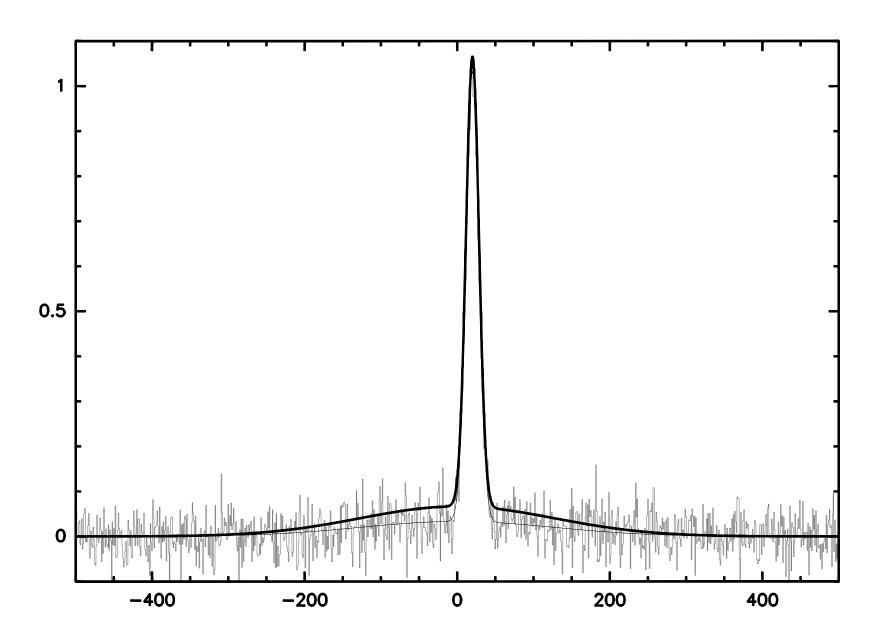
Natural choice of clean beam size: Synthesized beam size (i.e. fit of the central peak of the dirty beam).

⇒ Minimize unit problems when adding the dirty map residuals.

Caveats of flux measurements:

- CLEAN does not conserve flux
 (i.e. CLEAN extrapolates unmeasured short spacings).
- Large scales are filtered out (source size > 1/3 primary beam size ⇒ need of short spacings, cf. lecture by F. Gueth).
- $I_{\text{clean}} = B_{\text{primary}}.I_{\text{source}} + N$ \Rightarrow Primary beam correction may be needed: $I_{\text{clean}}/B_{\text{primary}} = I_{\text{source}} + N/B_{\text{primary}} \Rightarrow \text{Varying noise!}$
- Seeing scatters flux.

Photometry: V Importance of Extended, Low Level Intensity

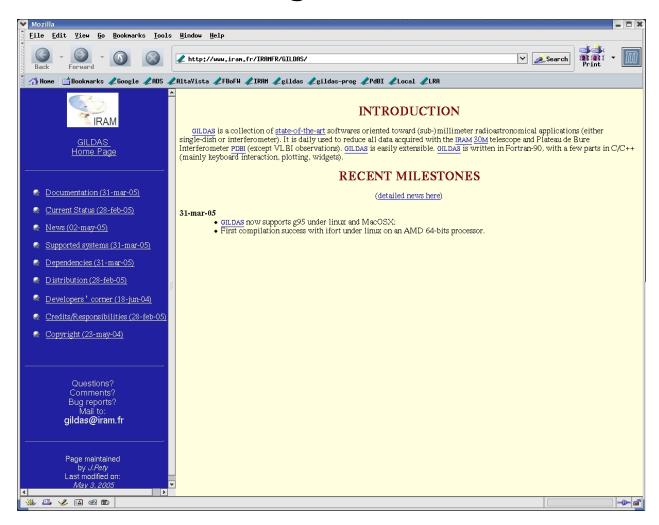


Writing the Paper: Your job!

J.Pety's 2nd life: GILDAS manager

Web page: http://www.iram.fr/IRAMFR/GILDAS

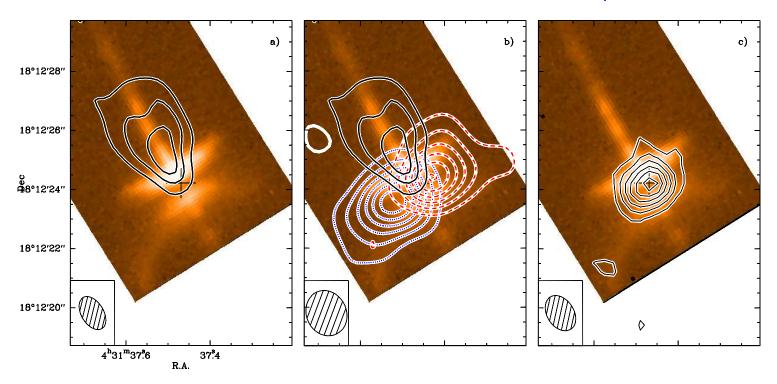
Mail to: gildas@iram.fr



J.Pety's 3rd life: Radioastronomer

For example:

HH 30: A case study for the disk-jet-outflow paradigm. Pety et al, 2006, A&A, in press, astro-ph/0608218



Mathematical Properties of Fourier Transform

- 1 Fourier Transform of a product of two functions
 - = convolution of the Fourier Transform of the functions:

If
$$(F_1 \stackrel{\mathsf{FT}}{\rightleftharpoons} \tilde{F_1} \text{ and } F_2 \stackrel{\mathsf{FT}}{\rightleftharpoons} \tilde{F_2})$$
, then $F_1.F_2 \stackrel{\mathsf{FT}}{\rightleftharpoons} \tilde{F_1} * \tilde{F_2}$.

- 2 Sampling size $\stackrel{\mathsf{FT}}{\rightleftharpoons}$ Image size.
- 3 Bandwidth size $\stackrel{\mathsf{FT}}{\rightleftharpoons}$ Pixel size.
- 4 Finite support

 FT

 Infinite support.
- 5 Fourier transform evaluated at zero spacial frequency = Integral of your function.

$$V(u=0,v=0) \stackrel{\mathsf{FT}}{\rightleftharpoons} \sum_{ij \in \mathsf{image}} I_{ij}.$$

Photographic Credits and References

- R. N. Bracewell, "The Fourier Transform and its Applications".
- J. D. Kraus, "Radio Astronomy".
- R. Narayan and R. Nityananda, Ann. Rev. Astron. Astrophys., 1986, 24, 127–170, "Maximum Entropy Image Restoration in Astronomy"