

The Northern Extended Millimeter Array NOEMA

IXth Interferometry School, Oct 11, 2016

Roberto Neri, IRAM

The NOrthern Extended Millimeter Array NOEMA

IXth Interferometry School

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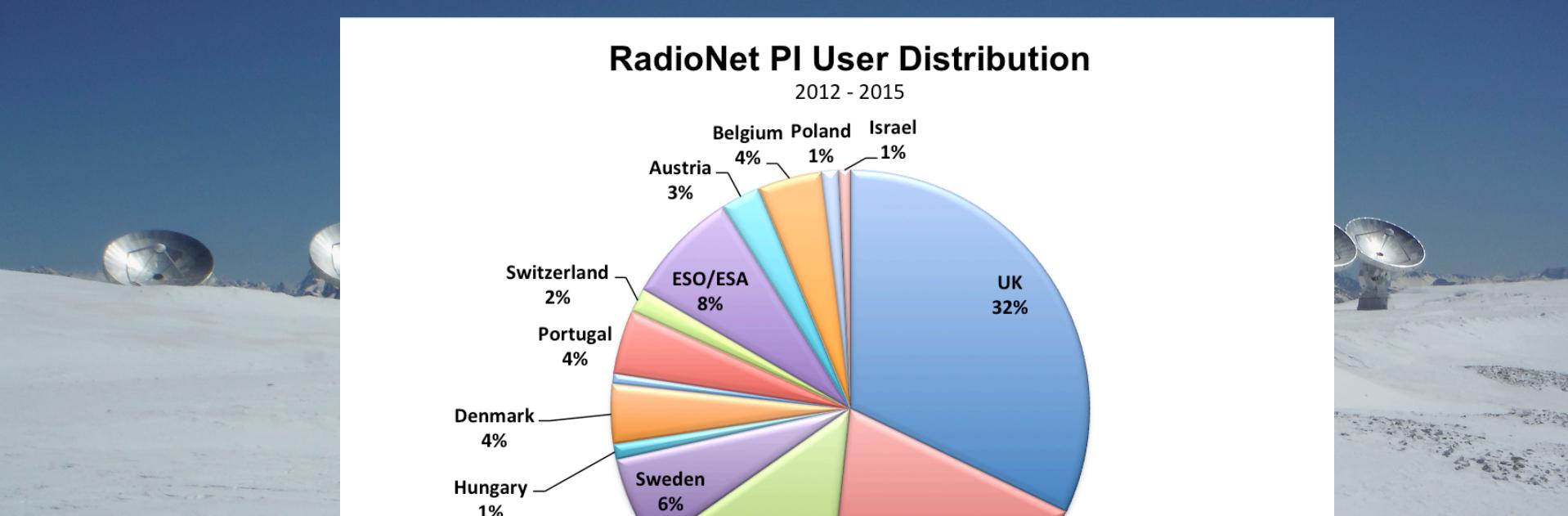
1. a general overview
2. instrumentation (receivers, correlators)
3. sensitivity considerations
4. position considerations

A view on the NOEMA Observatory



- IRAM = two observatories : NOEMA + IRAM 30m-telescope
- three partners: CNRS, MPG, IGN
- open time (up to 15%), RadioNet4

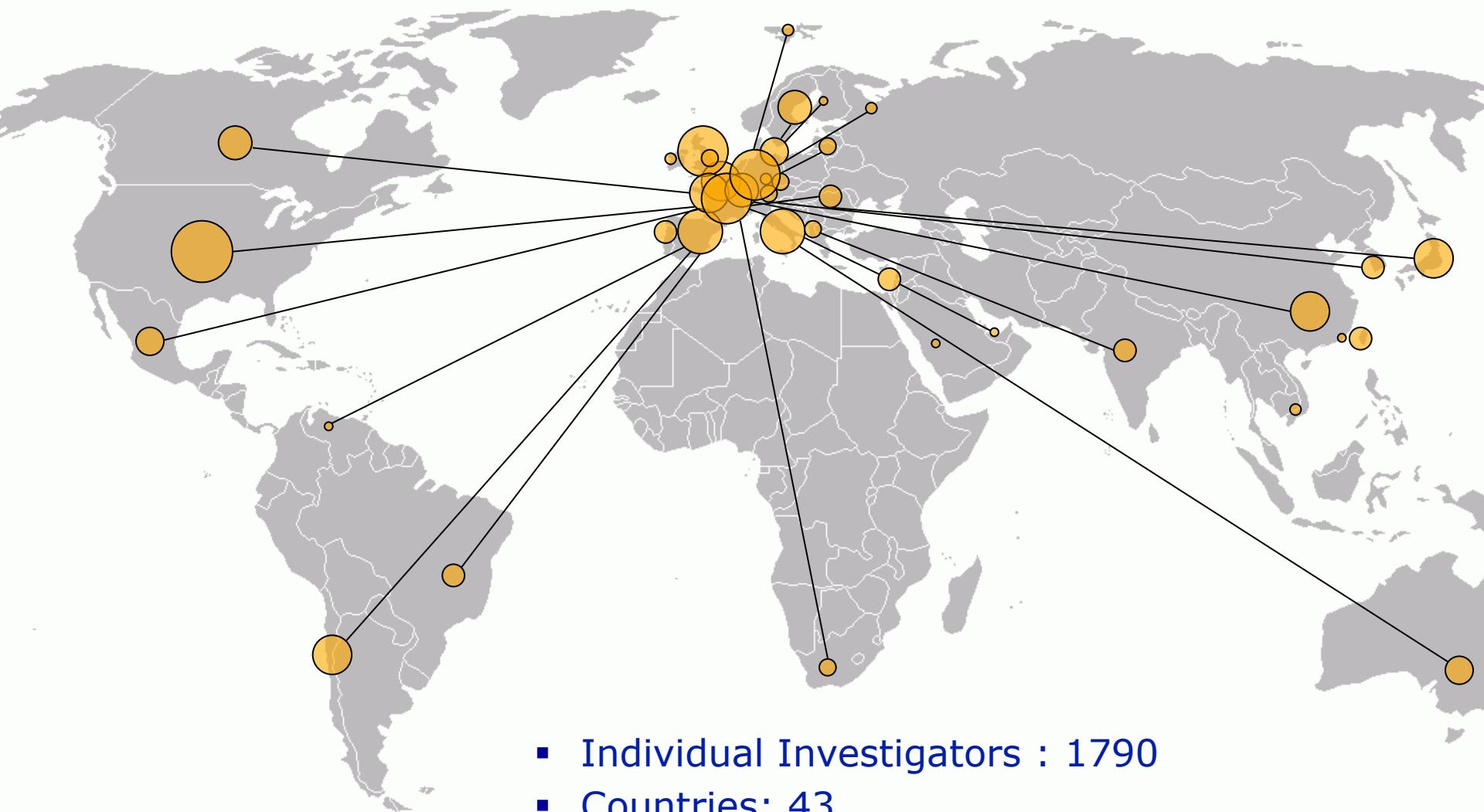
A view on the NOEMA Observatory



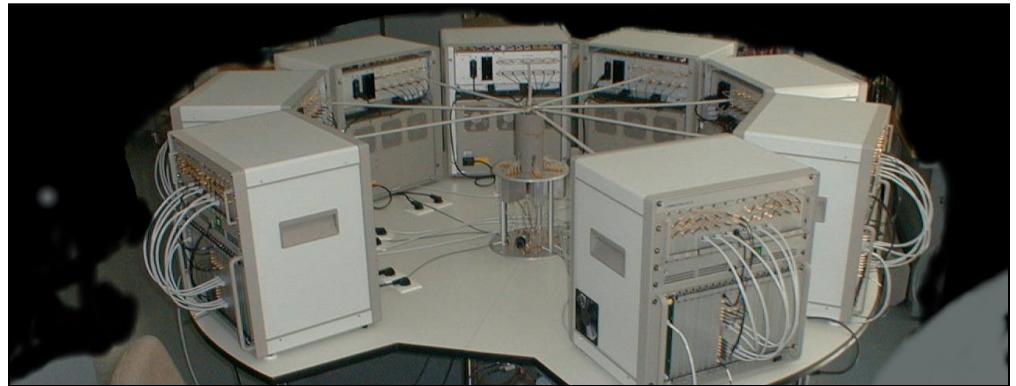
- IRAM =
- three pa
- open time (up to 15%), RadioNet4

scope

INVESTIGATORS DISTRIBUTION MAP 2010 – 2016

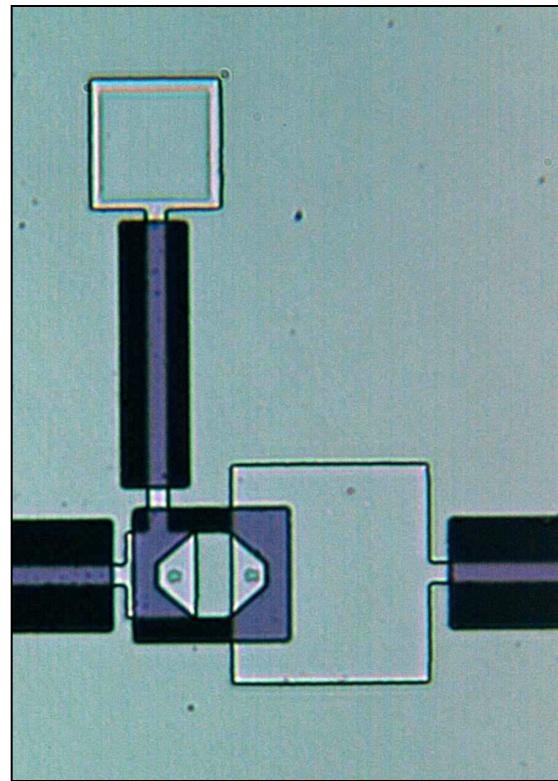


IRAM's expertise: pictures worth a thousand words



- Telescope design (~ 30 um), construction and operation
- Receiver design and development e.g. ALMA Band7, AETHRA
- HS-digital backends + LO systems e.g. PolyFix (32 GHz)

IRAM's expertise: pictures worth a thousand words



- Class 100 clean room for thin film technology
- complete mm/THz-wave technology laboratory
- developments for e.g. Herschel

progress timeline

Semester	Project	Done
W05/06	EW/NS track extensions	✓
W06/07	band 1 + band 3	✓
W07/08	band 2	✓
W09/10	WIDEX	✓
W10/11	band 4	✓
S12	double-array mode	✓
S13	LO reference system	✓
2015	N7 + 2SB receivers #1, #2	✓
2016	N8 + 2SB receivers #3, #4, #5, #6	(✓)
2017	POLYFIX + N9 + N10	



e

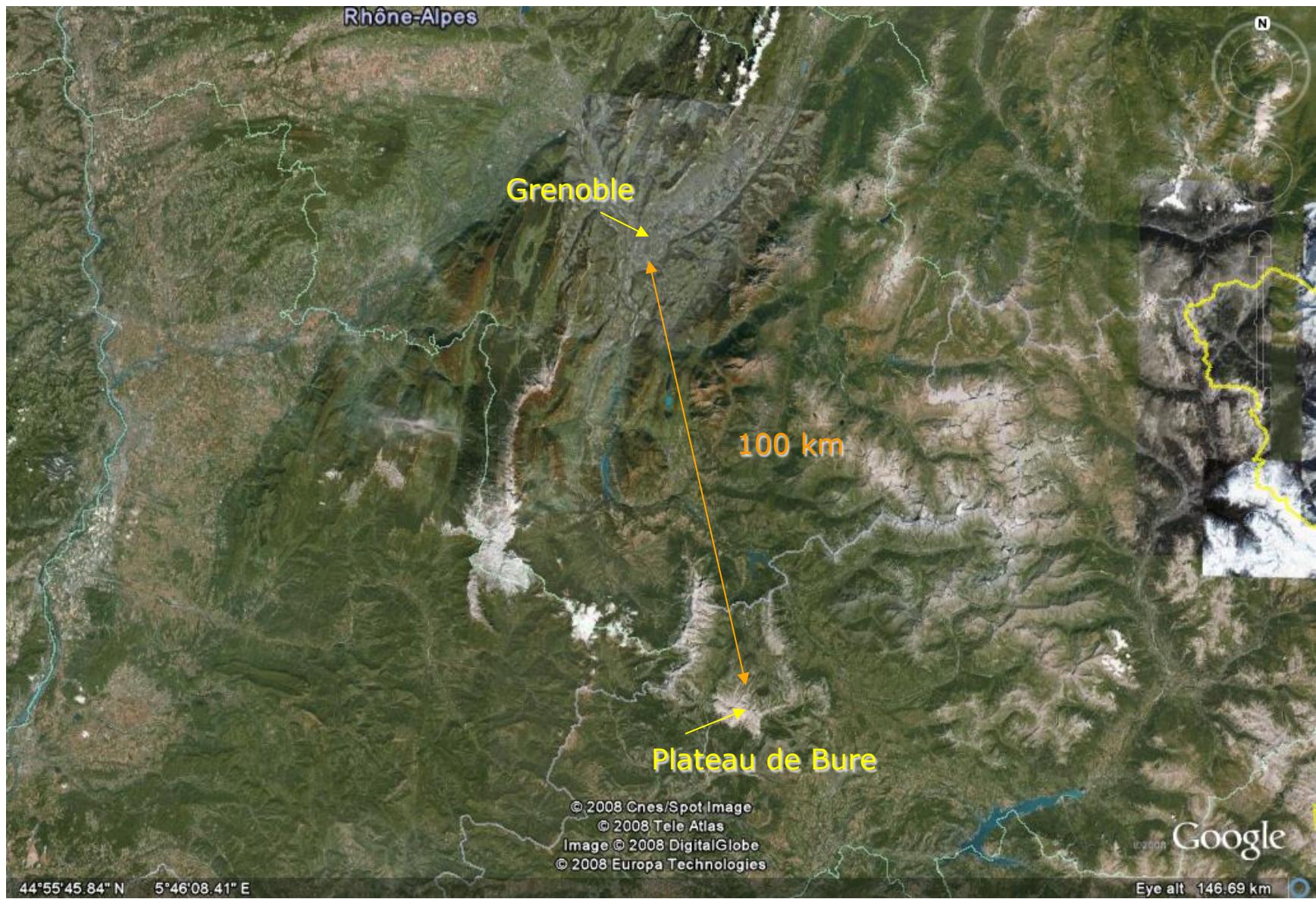
2010

N0 + ZSD receivers #3, #4, #5, #6

(✓)

2017

POLYFIX + N9 + N10







E

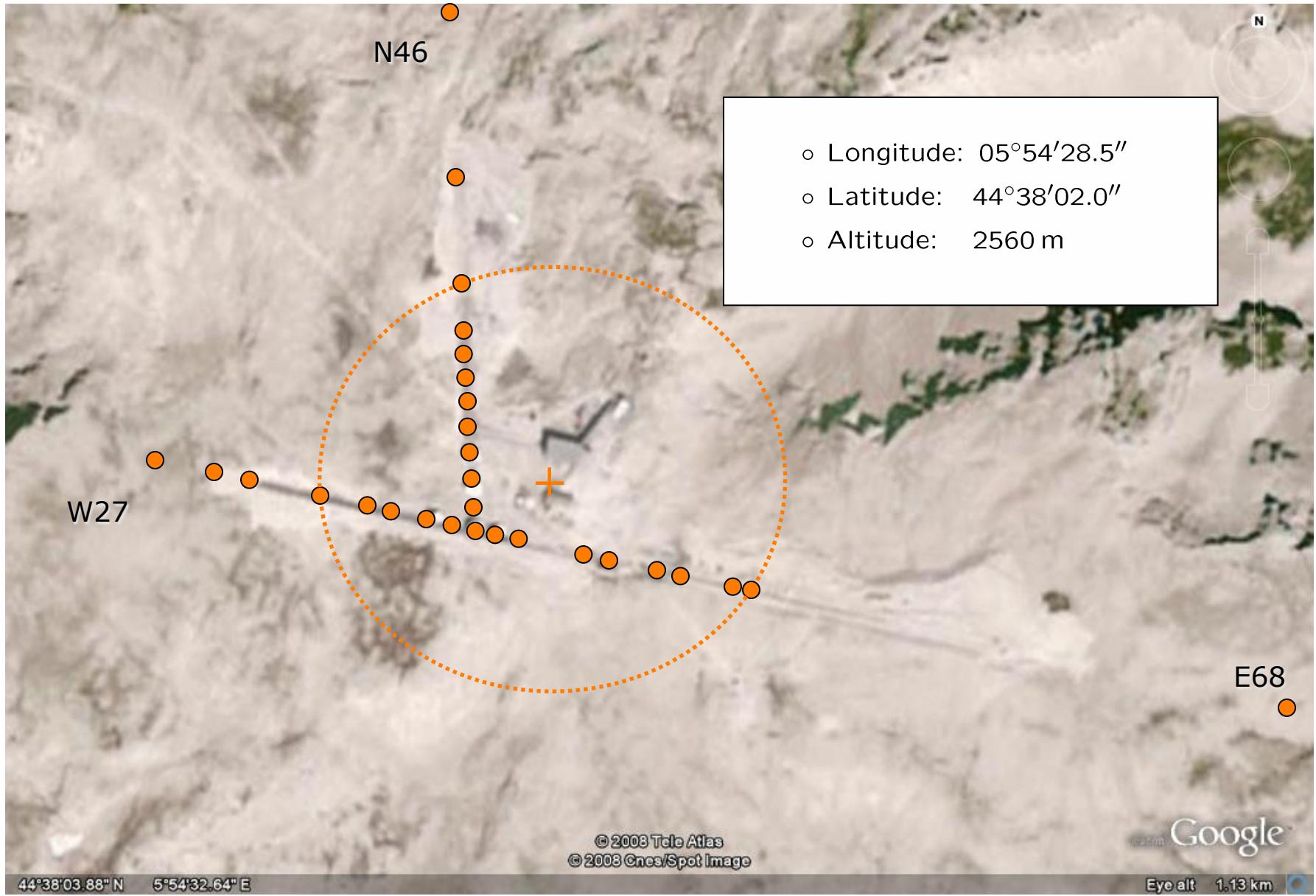
N

NOEMA site



- Latitude : 05°54' 28.5"
- Longitude : 44°38' 02.0"
- Altitude : 2560 m
- RFI protection : terrain shielding + NRQZ (30 km)

- Water vapor : 40% (<3mm); 25% (<1mm) in winter
down to 0.3mm in best winter conditions
submm conditions ~5 % of the time



NOEMA site

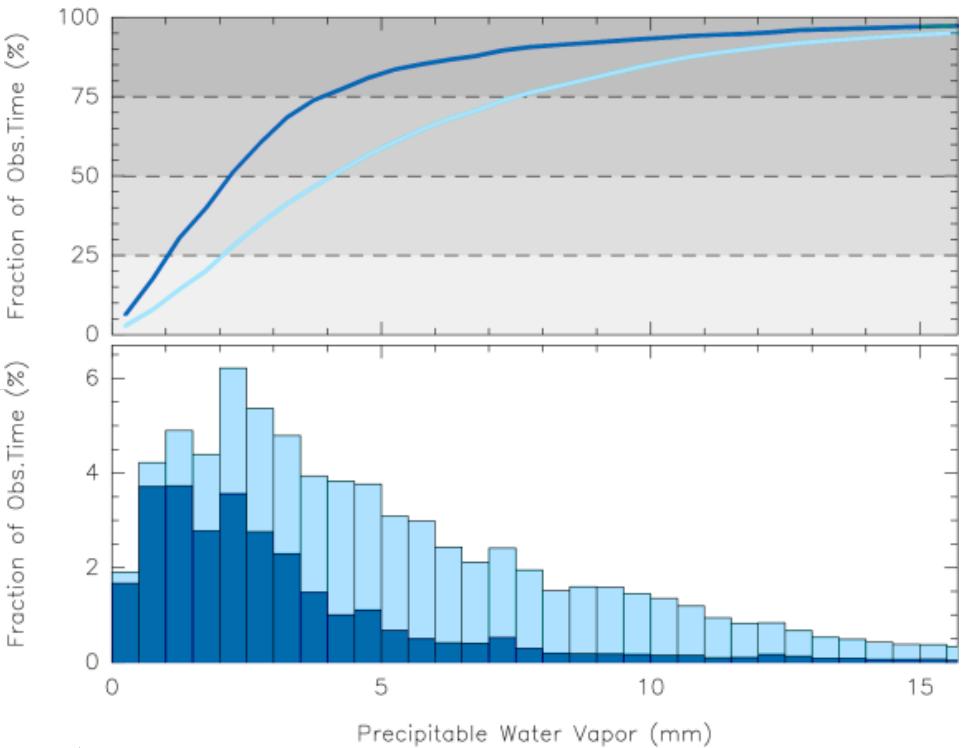
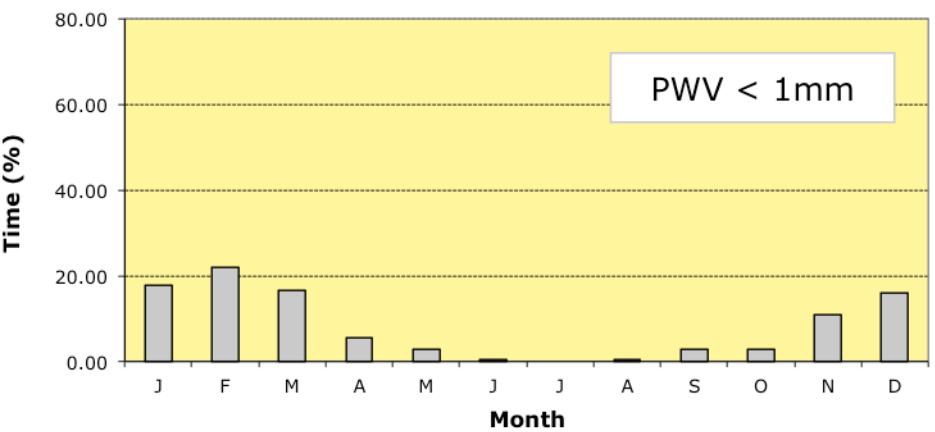
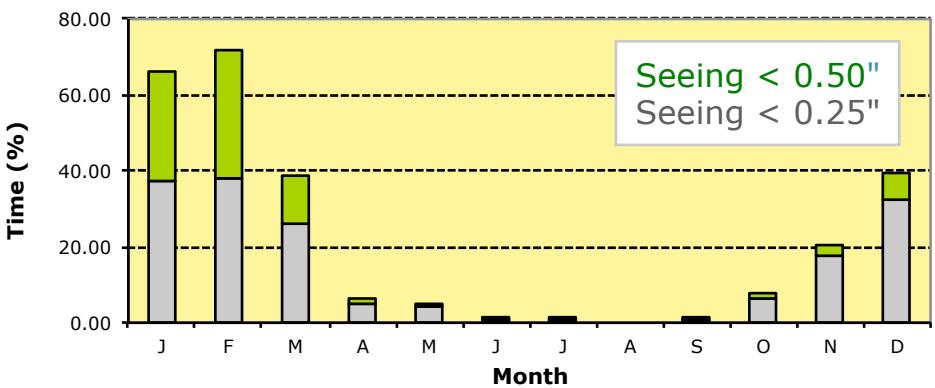


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down to 0.3mm in best winter conditions
submm conditions ~5 % of the time

- Weather downtime : 25 - 35%

some weather statistics



→ 2015: 80% of the observing time invested @ B1-3mm and B2-2mm

NOEMA observatory

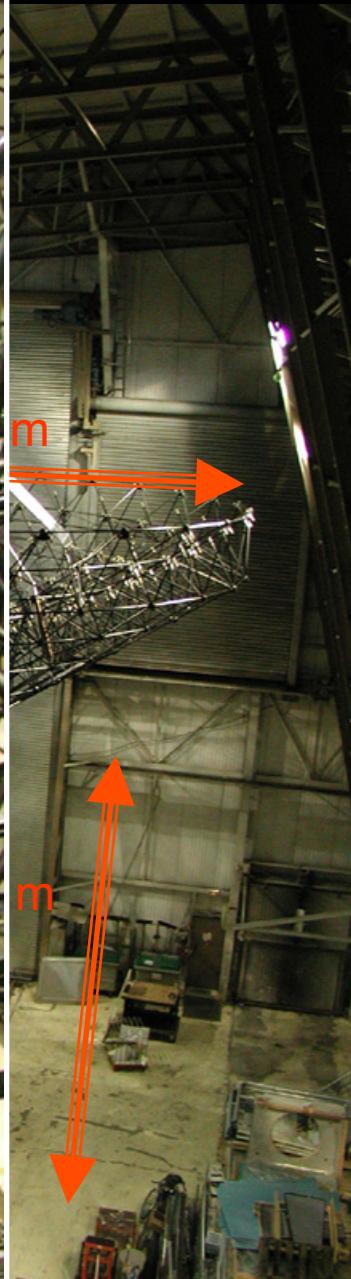
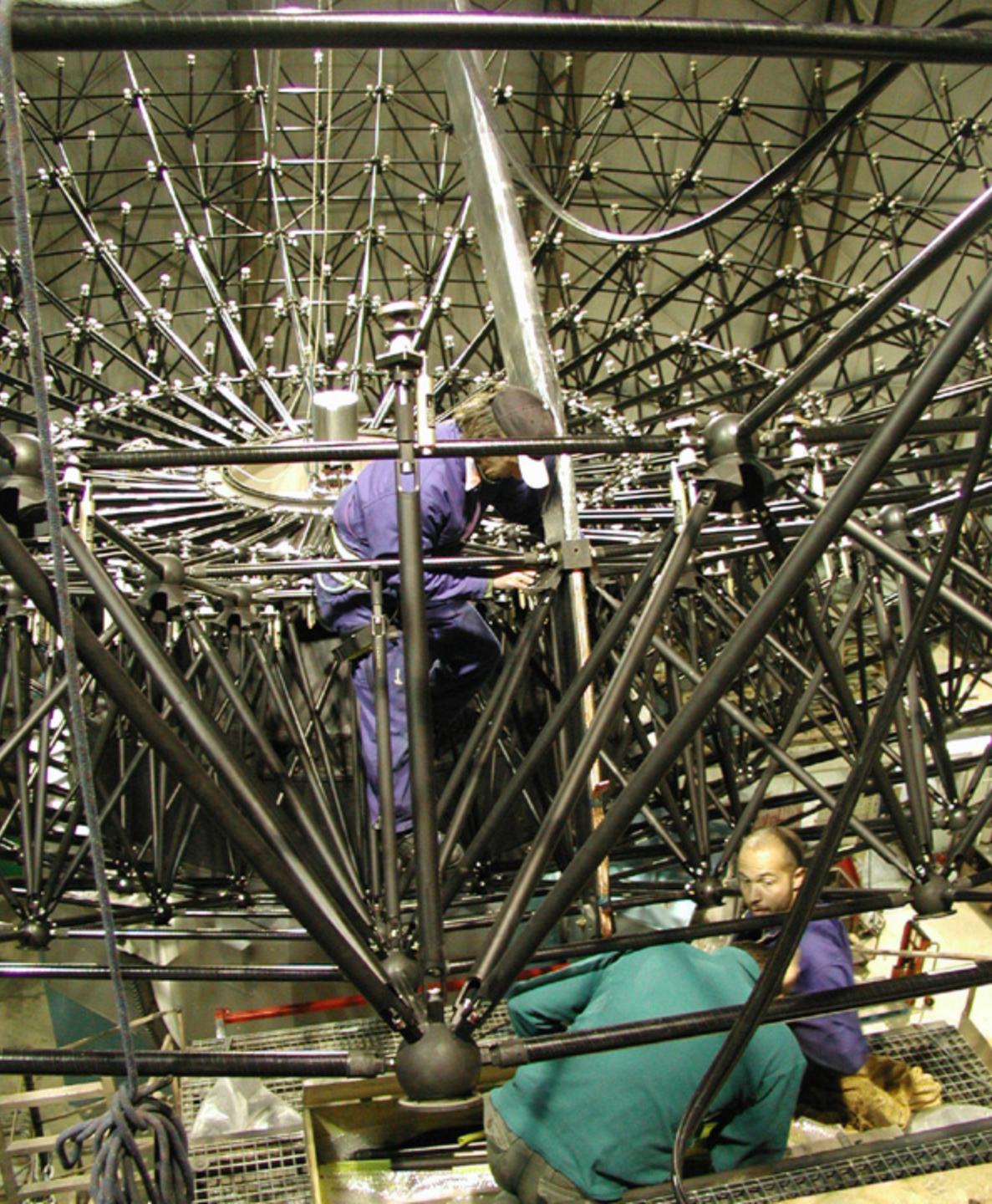


- Operation : 24 hrs, 365 days, service mode
 staff @ Bure + SOG @ Grenoble
- Team @ site : 6 staff members (incl. astronomer)
- Working schedule : 1 team per week, every 3 weeks
- VLBI @ 3mm : 5 days sessions, twice a year (GMVA)
 1mm intercontinental with ALMA in the future

NOEMA antennas



- antennas : 8, Cassegrain type
- collecting area : $177\text{m}^2 \times 8 = 1416\text{m}^2$ (2016)
- surface panels : 176, aluminum
- surface accuracy : 25 - 40 μm
- aperture efficiency : 0.65 @ 230 GHz
- primary beam : 21" @ 230 GHz
- pointing / tracking RMS : 1.5" / 0.2"
- wind speed (max) : 14 m/s



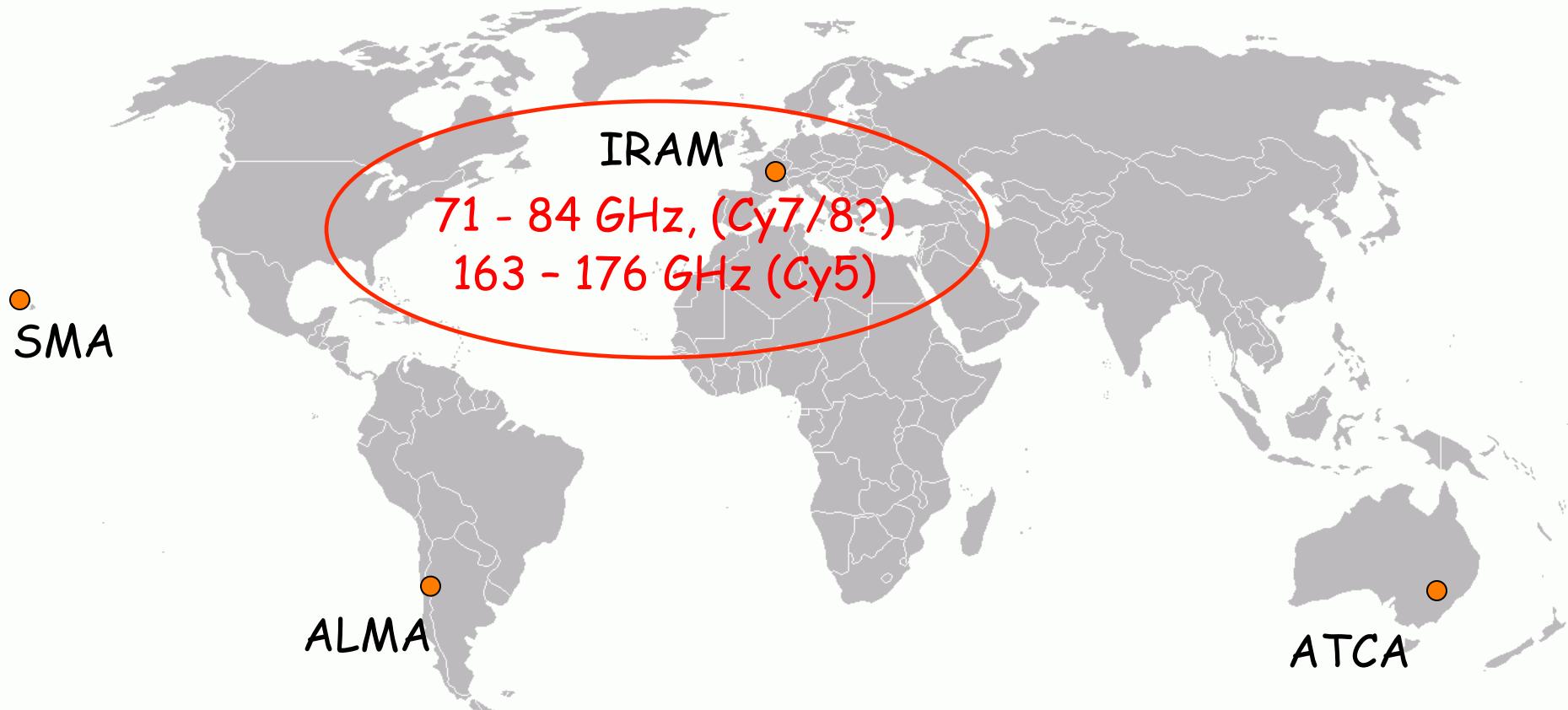
(sub)mm-interferometers worldwide (2010)

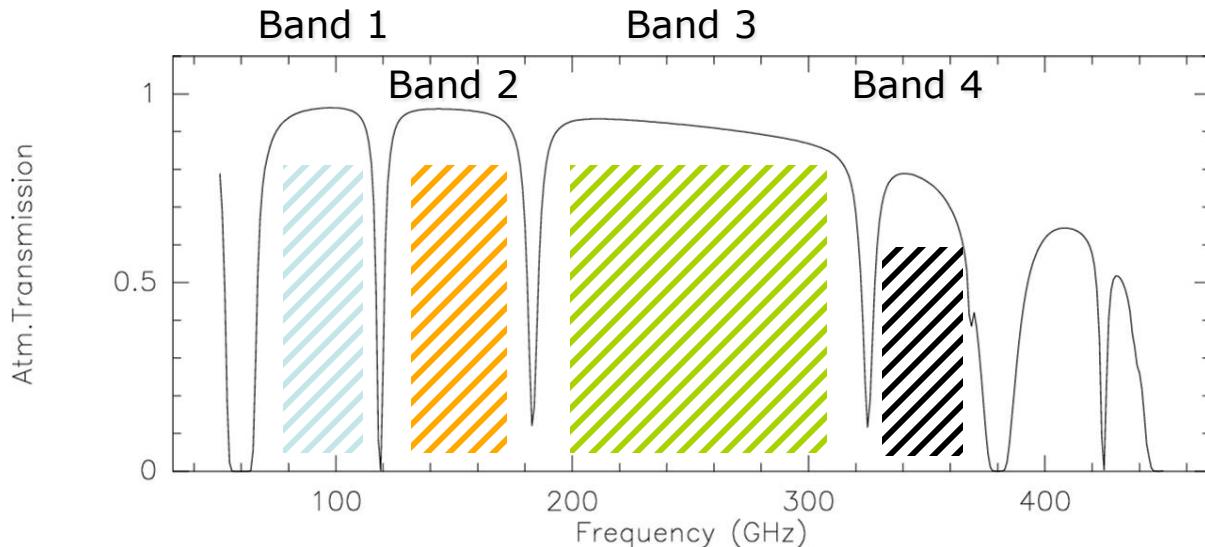


(sub)mm-interferometers worldwide (2016)



(sub)mm-interferometers worldwide (2016)





3mm = 100 GHz

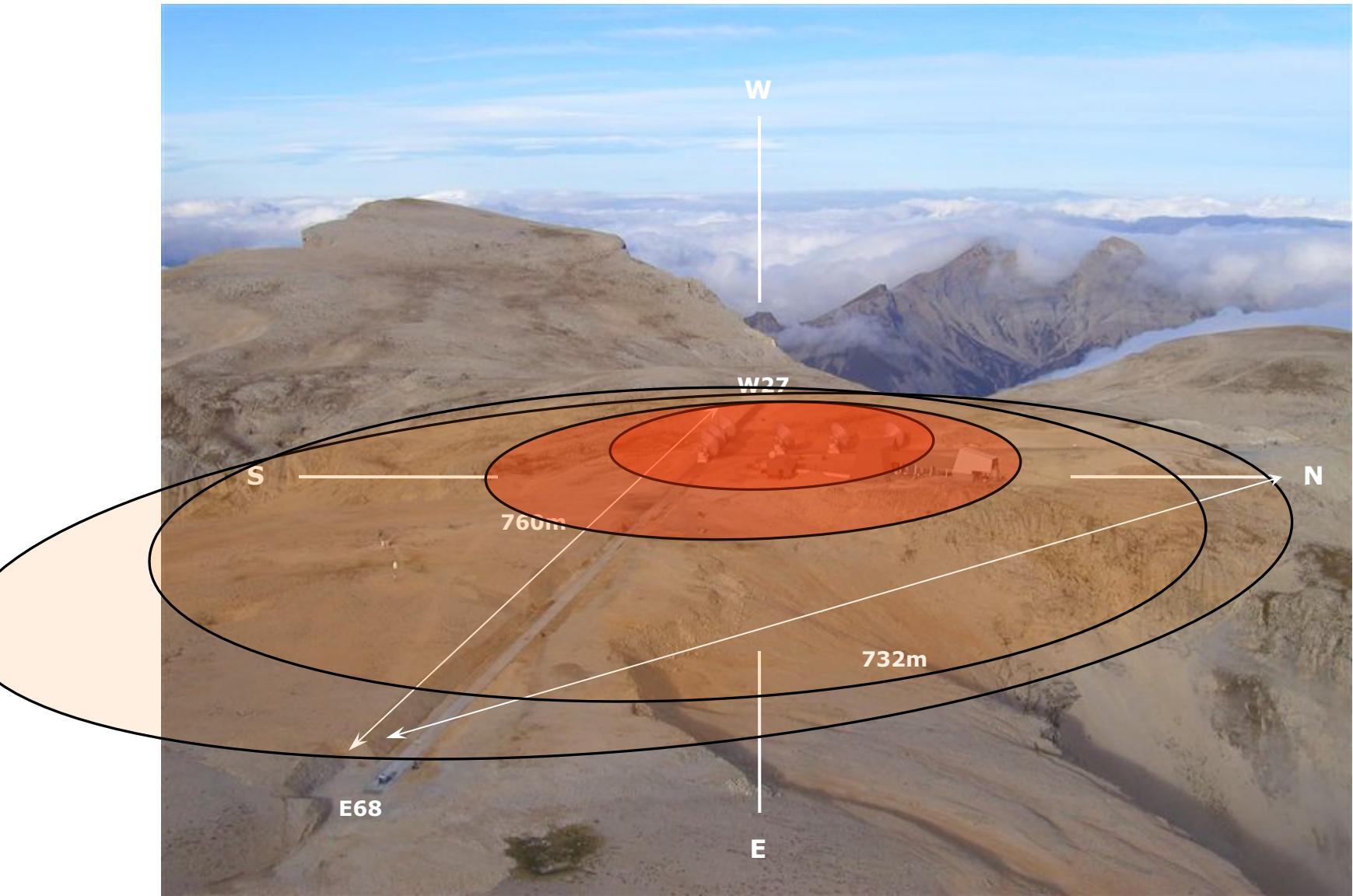
2mm = 150 GHz

1mm = 300 GHz

0.8mm = 350 GHz

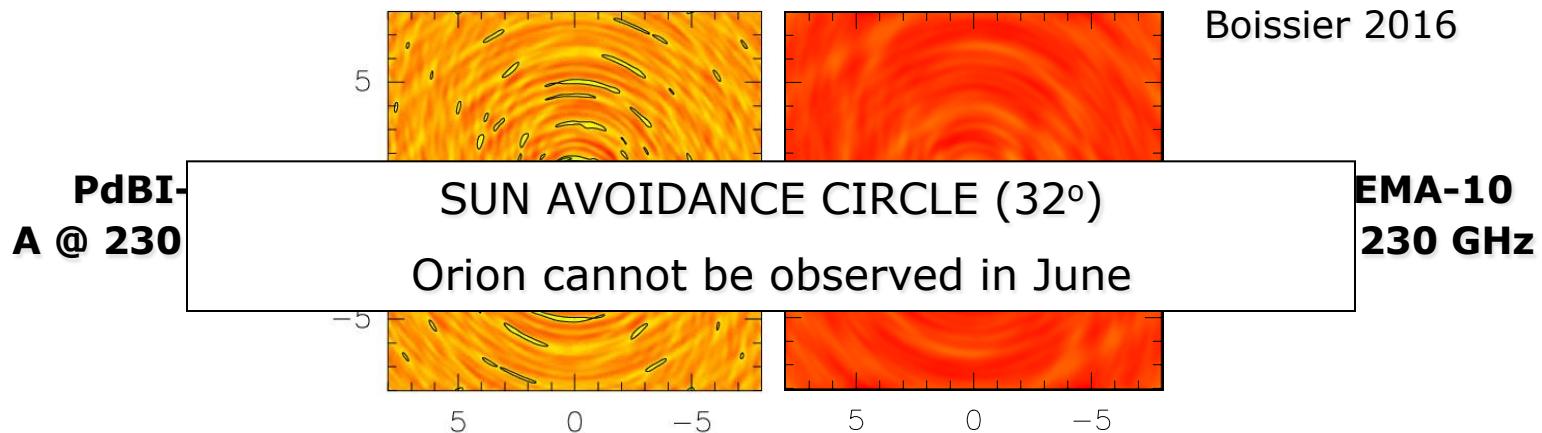
Interferometer	Atmospheric window	Ang.Resolution
ATCA	3mm	1.6" @ 105 GHz
NOEMA	3mm, 2mm, 1mm, 0.8mm	0.2" @ 300 GHz
SMA	1mm, 0.8mm, 0.4mm	0.15" @ 690 GHz
ALMA	3mm 1mm → Band 10	0.03" @ 350 GHz

Large differences !

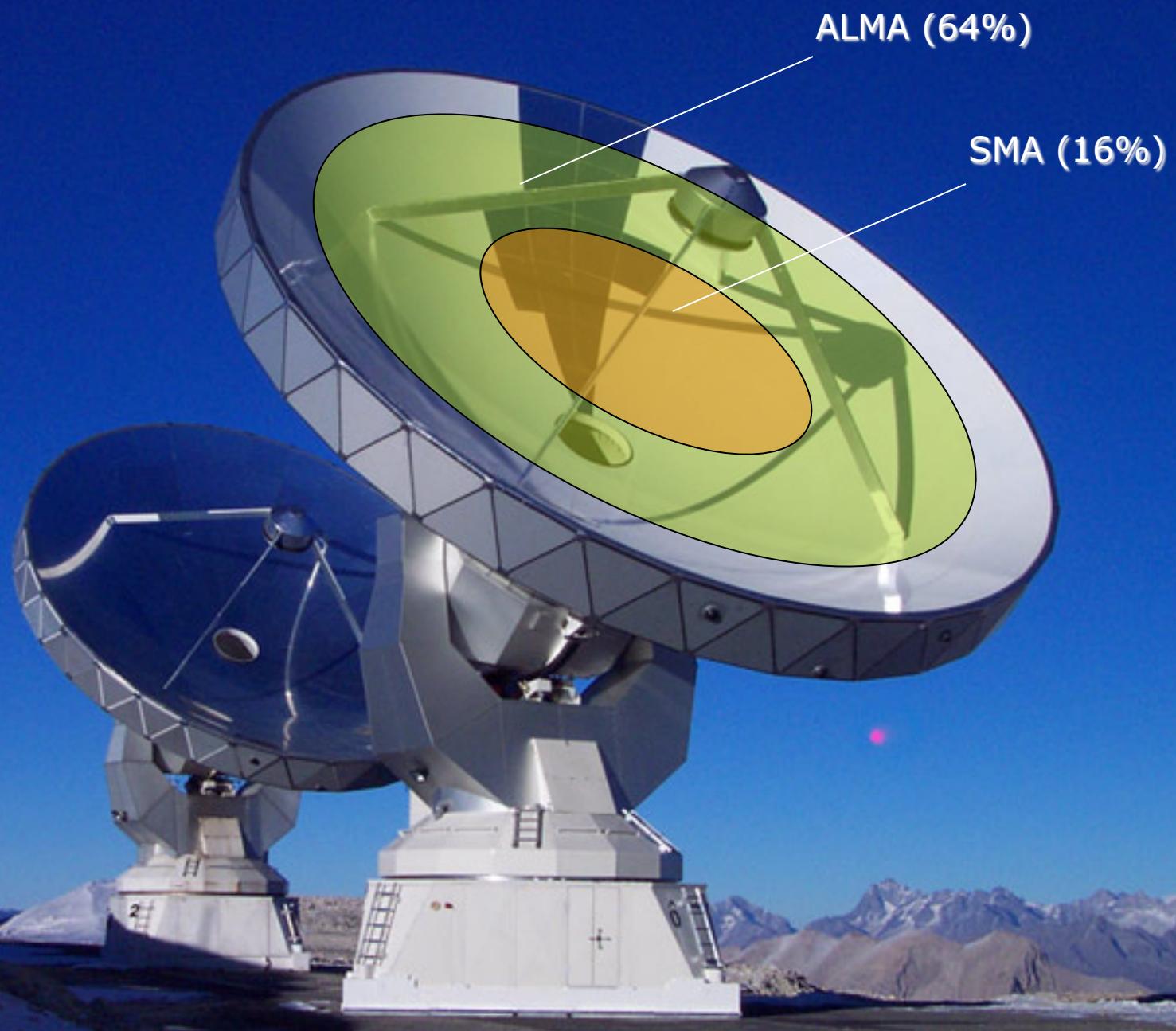


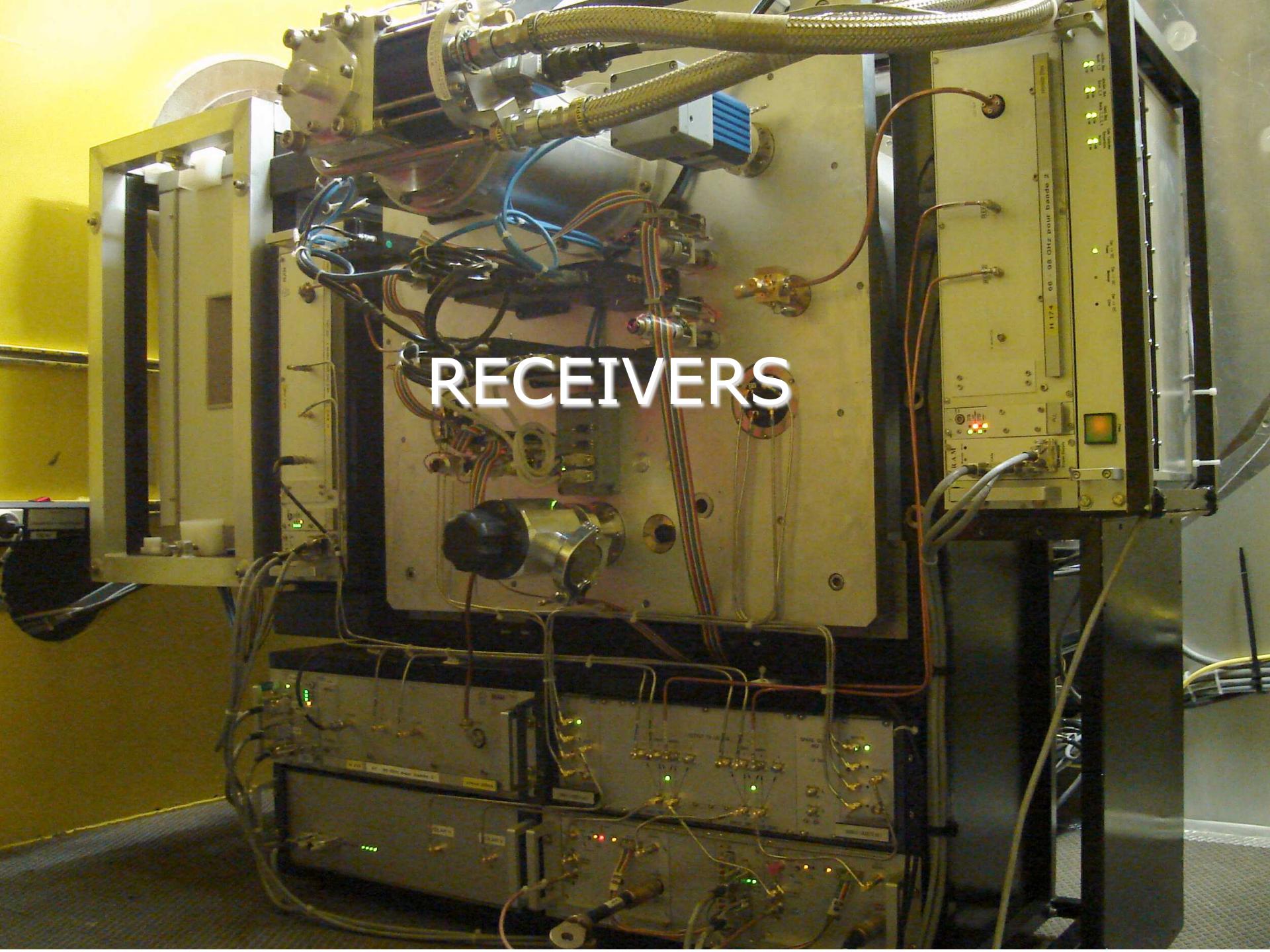
NOEMA array configurations

Design: 3 configurations, optimization 40° decl.



Configurations	D	C	A
Months	Apr – Nov	Mar - Apr Nov - Dec	Jan - Mar
Resolution @ 230 GHz	2"		0.3"-0.4" 0.2" (2018/2019)





The image shows a sophisticated electronic receiver system. It consists of several metal panels, some with transparent windows, and a complex network of blue, red, and black cables. A prominent feature is a large cylindrical component at the top left. In the center, there's a circular component with a lens-like appearance. The word "RECEIVERS" is overlaid in large, white, sans-serif capital letters across the middle of the image. On the right side, there's a vertical stack of modules with various connectors and a small orange button. The background is a plain yellow wall.

RECEIVERS

NOEMA state of the art receiver technology

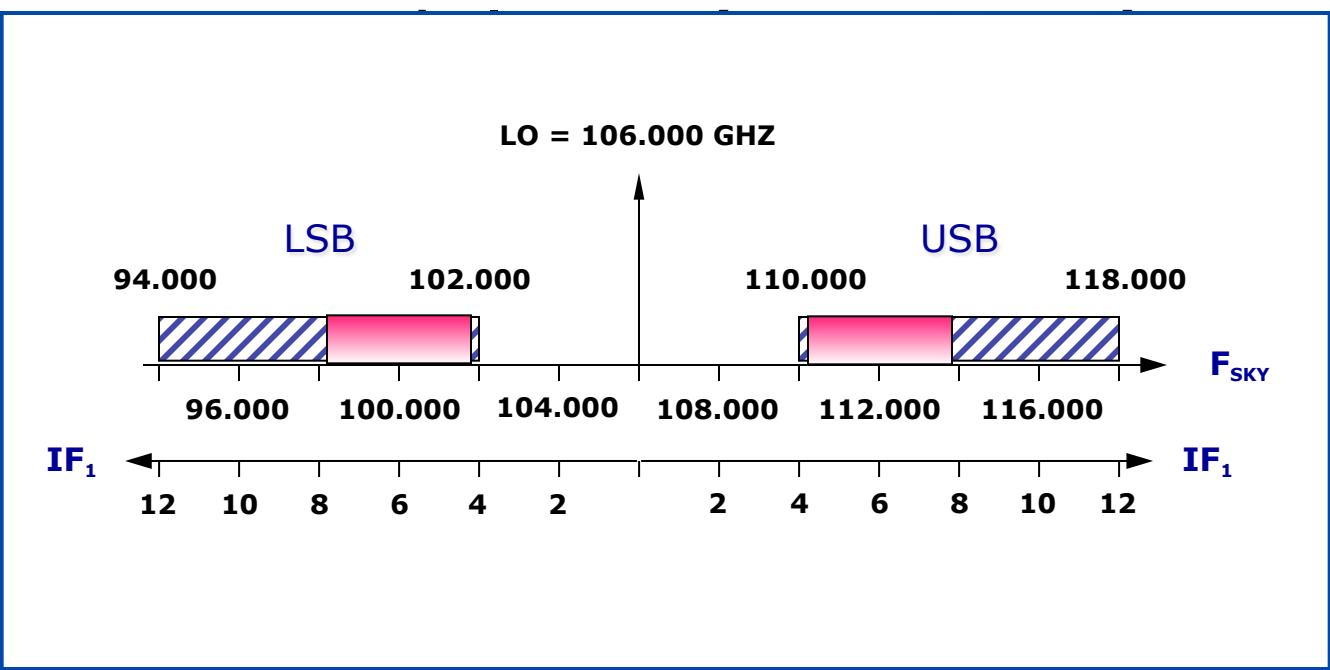
- closed cycle cryocoolers → no liquid He refills
- SIS mixers → 8 GHz Band in each polarization
 - USB and LSB operation (2SB)
- fully reflective optics → lower loss
- design optm → high density, best EMI control, simplified wiring
- tuneless mixers and LOs for band 4 → simplified frequency tuning and switching

SEP 2016 = 6 ANTENNAS EQUIPPED

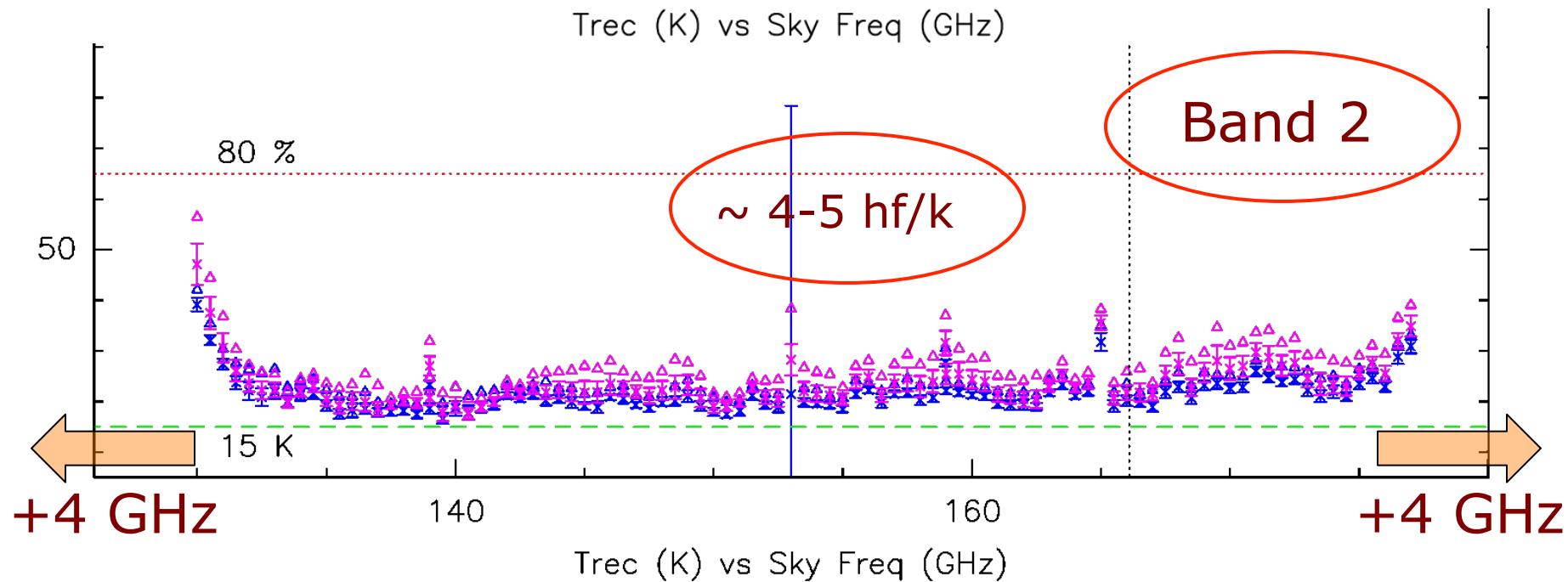
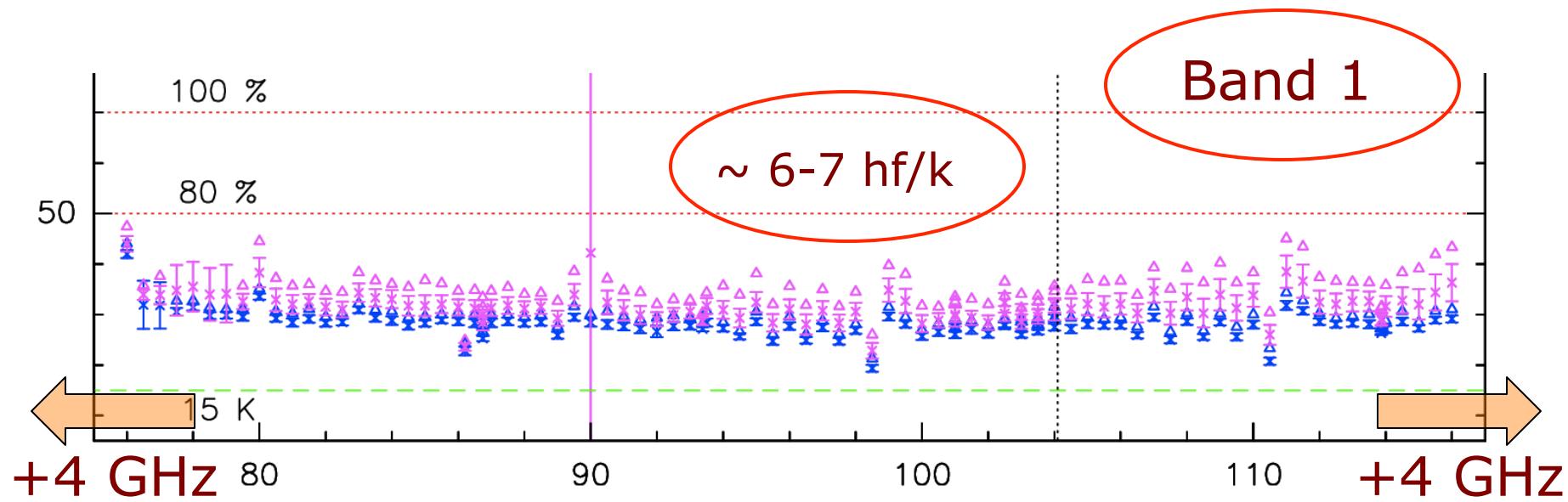
DEC 2016 = ALL ANTENNAS EQUIPPED WITH 2SB RECEIVERS

NOEMA receiver

Item
RF bands
WVR radiometer
B1 = ALMA Band 3
B2 = ALMA Band 4
B3 = ALMA Band 6
B4 = ALMA Band 7



Parameter	Description	Notes
RF response	2SB mixers	LSB and USB image gain <-10dB
IF band	4 – 12 GHz	total of 32 GHz
Polarization	dual linear	circular also possible
Observing mode	single frequency dual polarization	second band in standby potential for Dual freq, Dual pol

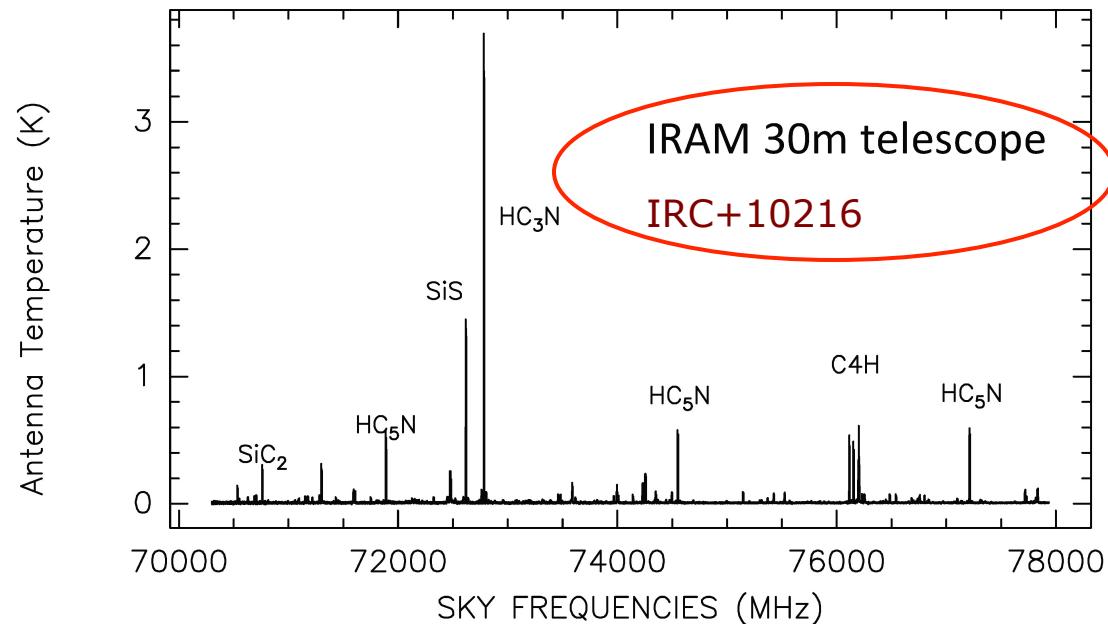
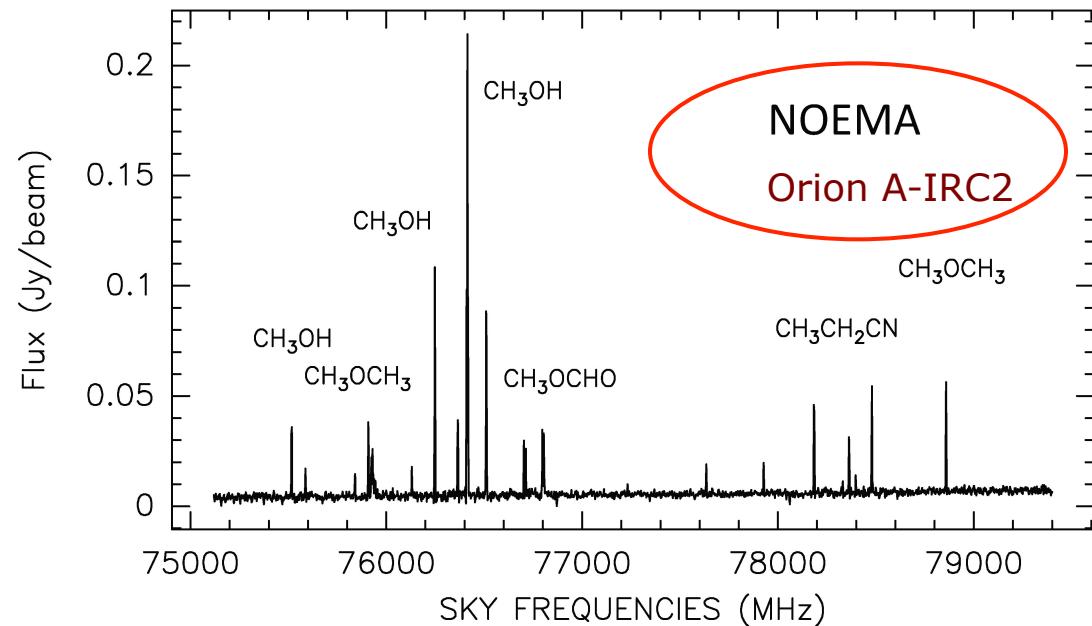


70-80 GHz band offers

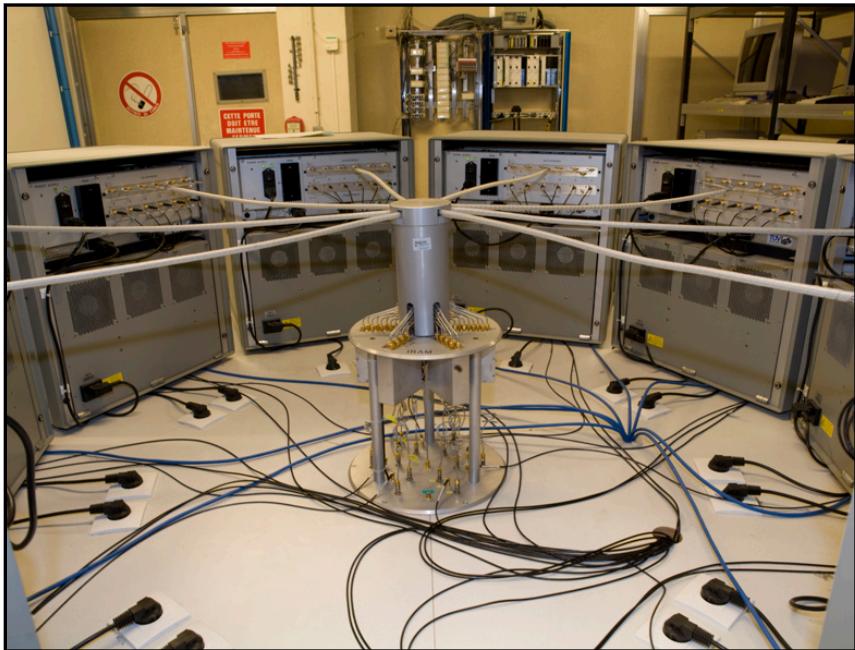
- new discovery space
- deep molecular line surveys
- first-ever opportunity to perform synthesis mapping (no ALMA)
- NOEMA + 30m telescope to sample spatial scales down to 1.3"

NOEMA:

- 74.7-80 GHz, Dec 01, 2016
- 70.8-80 GHz in 2017



NB - Correlator



WB – Correlator
(WIDEX)

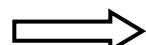


today: NOEMA runs two correlators in parallel

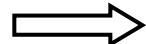
spring 2017: PolyFix (lecture by J.Boissier)

NOEMA correlators

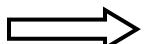
Item	Value	Notes
Correlator		
1 = Narrow Band	8 Units : 20 – 320 MHz	Freq.res : 0.039 – 2.5 MHz
2 = Wide Band	4 Units : 2 GHz	Freq.res : 2 MHz Fixed
IF band	4.2 – 7.8 GHz	IF processor limited
Polarization	Dual linear	Full Stokes not supported yet



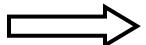
galactic work, planetary work



multi-resolution, line de-blending



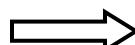
extragalactic work, line searches (@ high redshift)



improved relative line intensity calibration

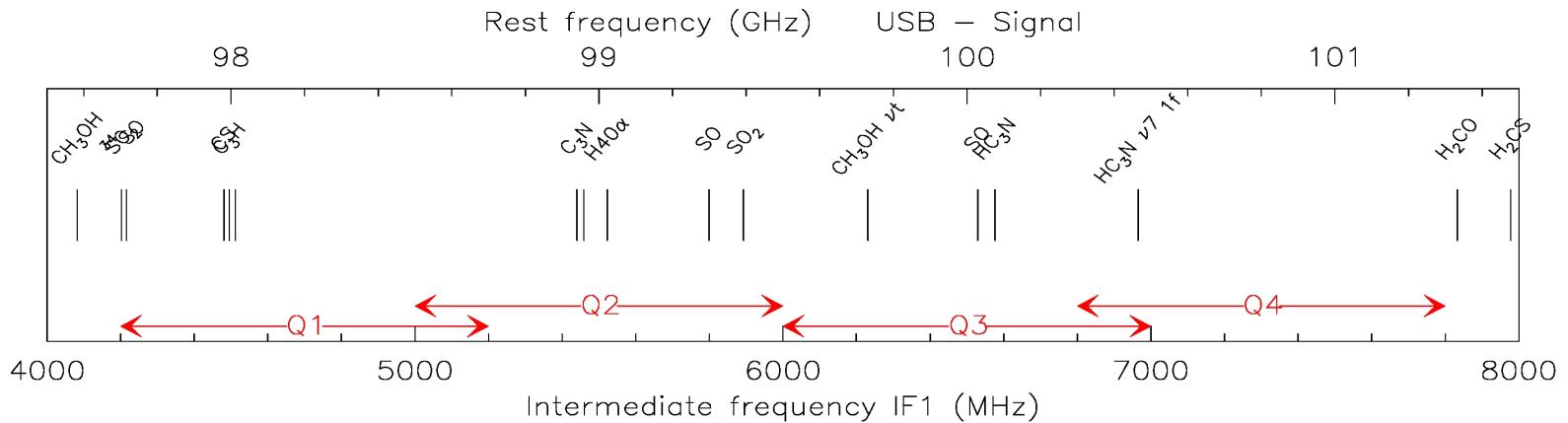


sensitive continuum



calibration, polarization,
spectral index

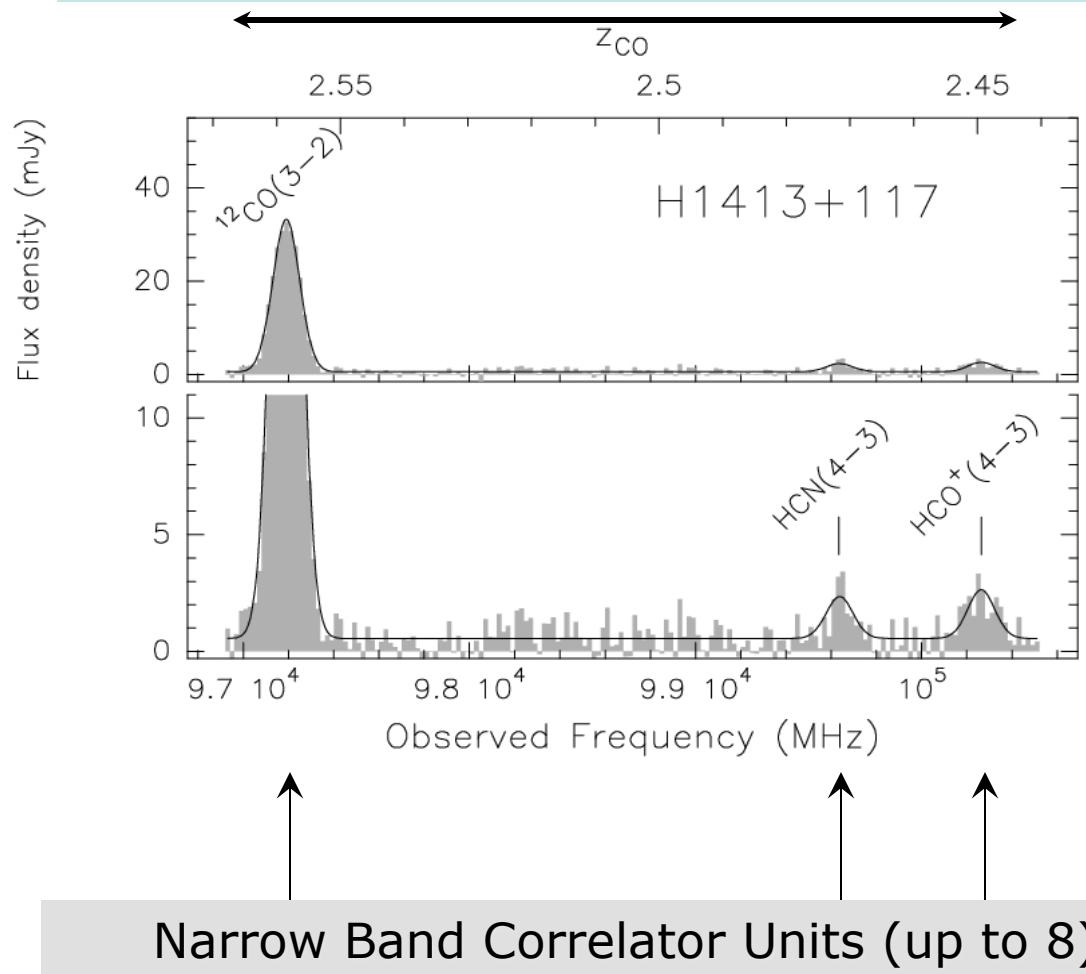
a 3.6 GHz IF but ...



- correlator accepts only 2 quarters ; max bandwidth = 2 x 1 GHz
- eight (8) correlator units : 20 ... 320 MHz (40 KHz ... 2.5 MHz)

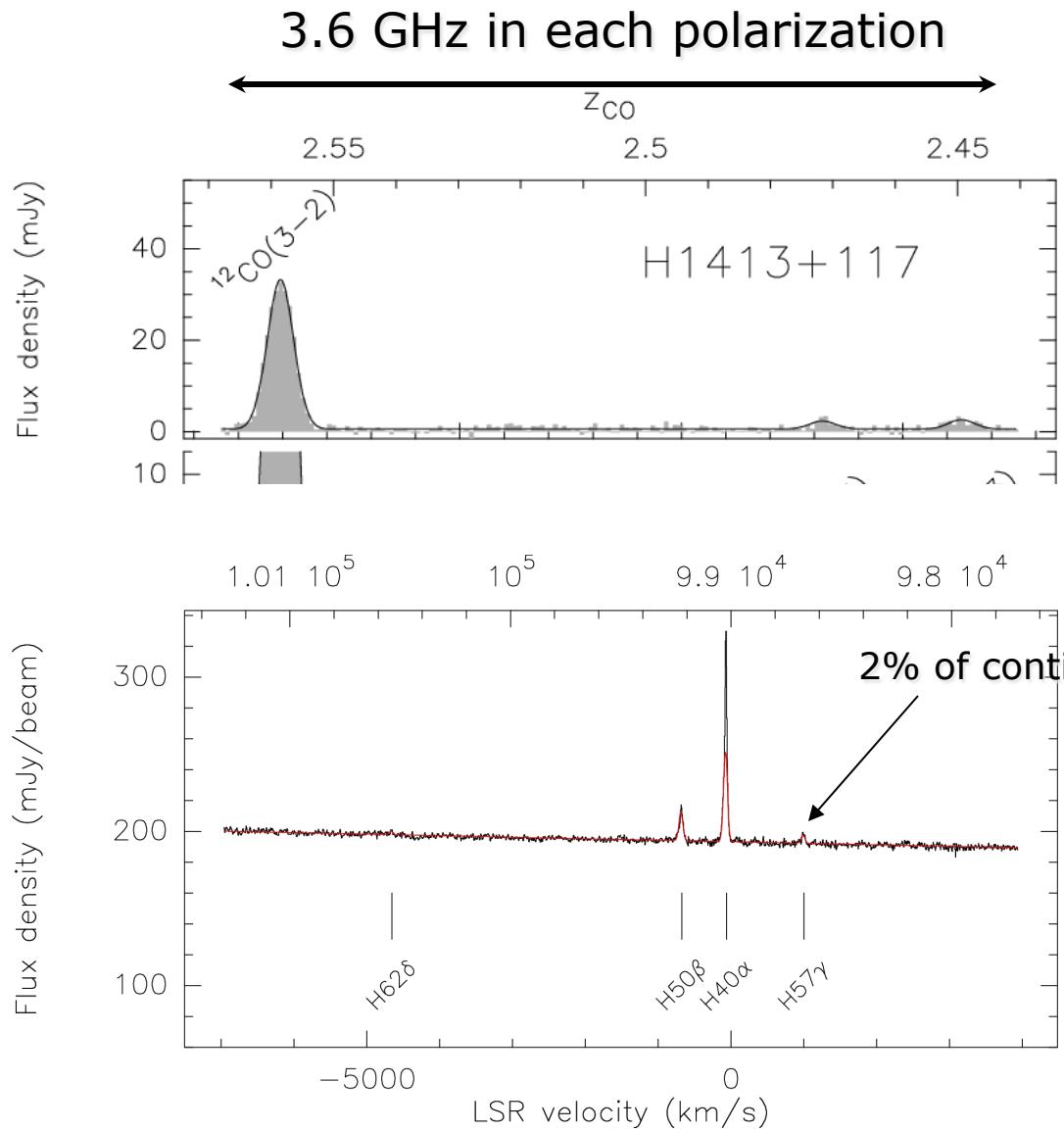
Band (MHz)	Channel (MHz)	Δv (100 / 230) (km/s)	Sensitivity (100 / 230) (mJy after 1 hr)
320	2.5	7.5 / 3.3	2.3 / 5.9
160	0.6	1.9 / 0.8	4.7 / 12.0
80	0.3	0.9 / 0.4	6.6 / 17.0

WIDEX = 3.6 GHz in each polarization



spect.cover. = 3.6 GHz
chan.sampl. = 20 MHz
integra.time = 2.2 hrs
r.m.s. = 0.66 mJy

coarse spec. resolution
high spec. resolution

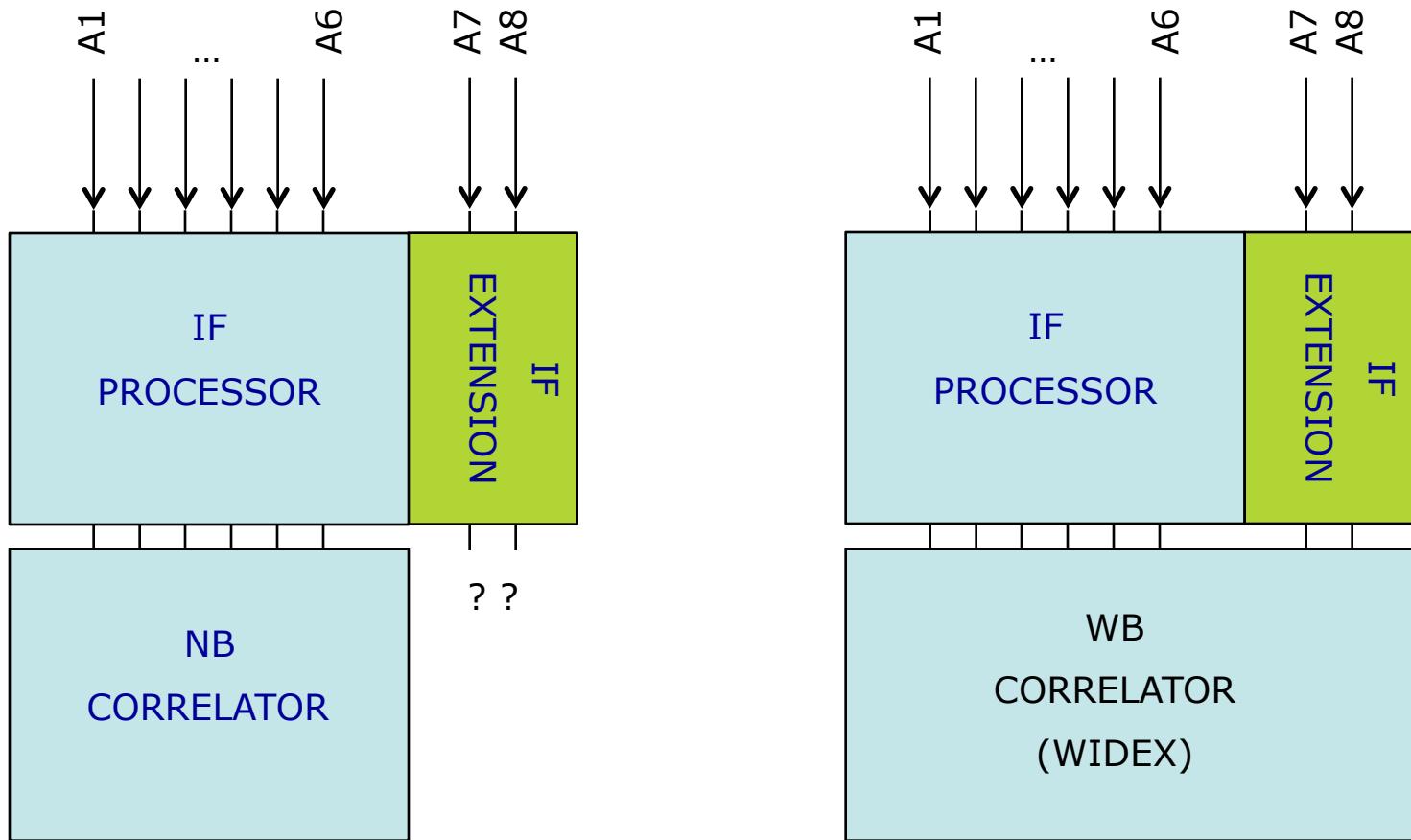


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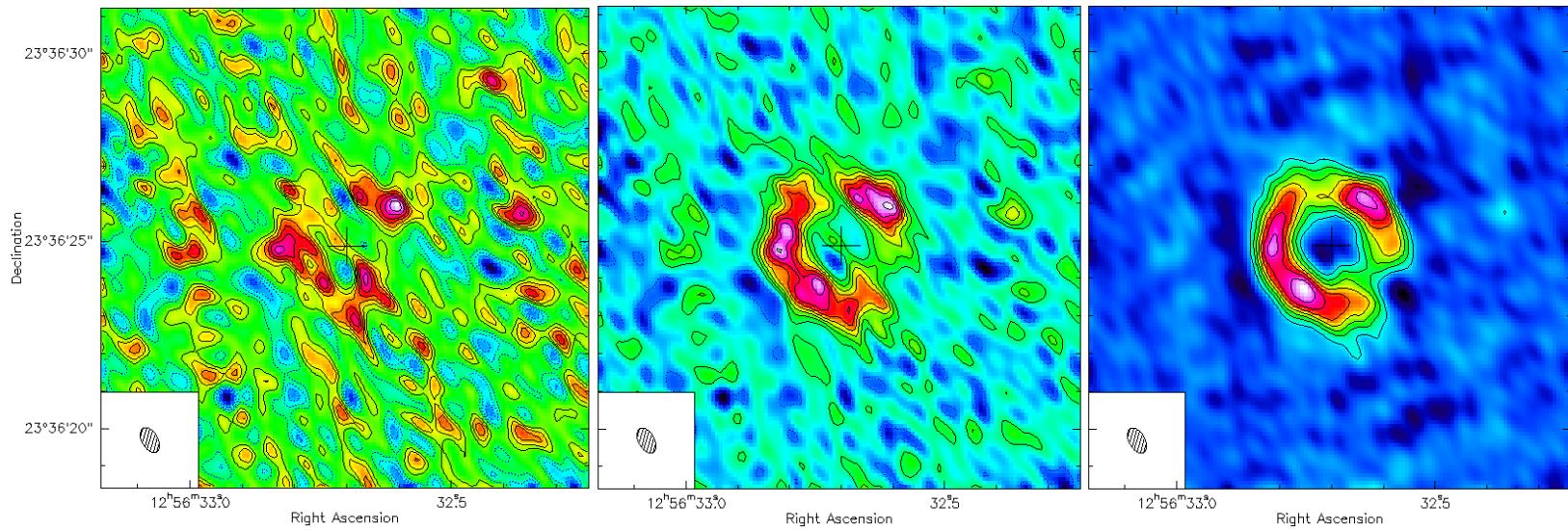
→ **line searches**

→ **improved relative line intensity calibration**

IF processor extension + WIDEX



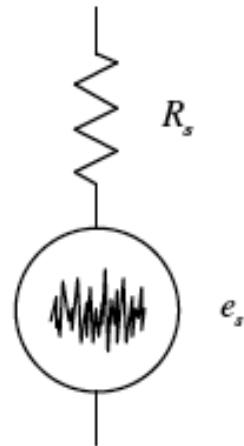
sensitivity considerations



Noise Power

The output power of a ...

... Resistor :



... Receiving System :

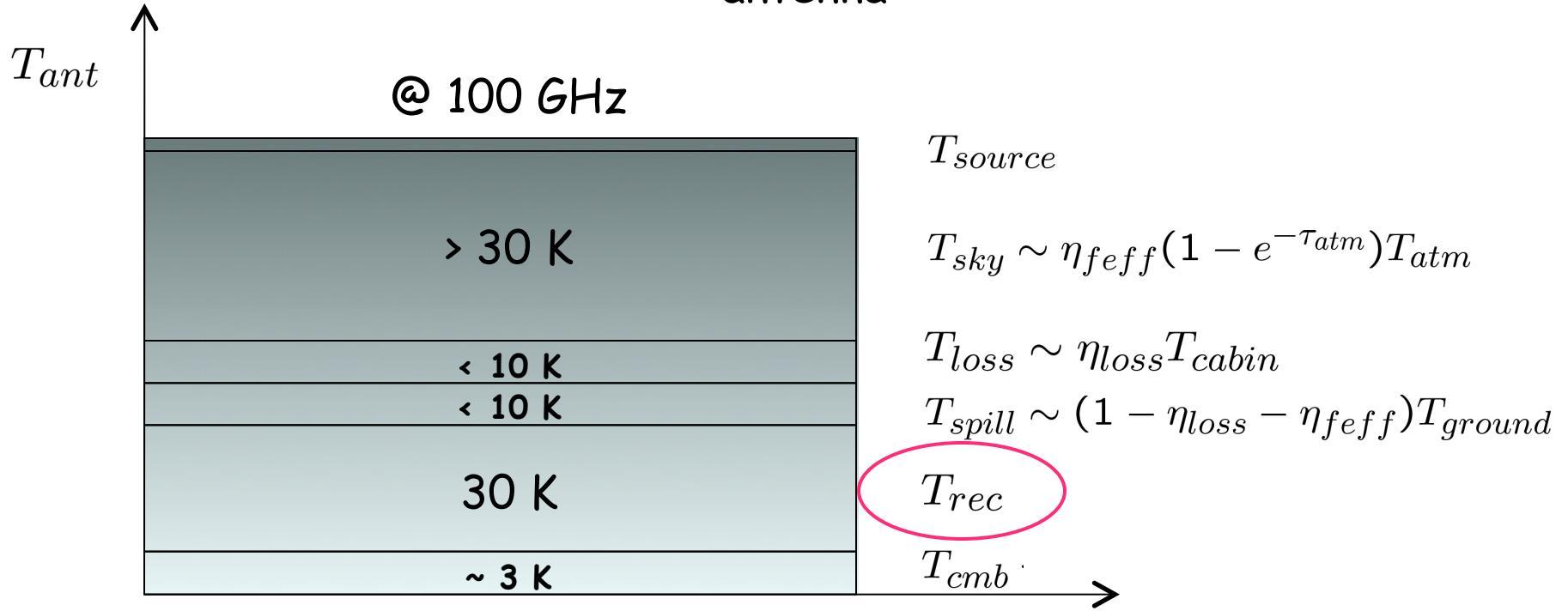
$$P_N = kT_{ant}\Delta\nu$$

Antenna System Temperature



Antenna System Temperature

is the temperature of the equivalent blackbody observed by the antenna



$$T_{ant} = T_{cmb} + T_{sky} + T_{spill} + T_{loss} + T_{rec}$$

We refer the **System Temperature**

Noise Power 

$$T_{sys} = \frac{e^{\tau_{atm}}}{\eta_{feff}} T_{ant}$$

and the **Antenna Temperature**

Astronomical 
Signal

$$\begin{aligned} T_A^* &= \frac{e^{\tau_{atm}}}{\eta_{feff}} T_{source} \\ &= \frac{\eta_A A}{2k} S \end{aligned}$$

to an ideal antenna located outside the atmosphere.

NOEMA system temperatures

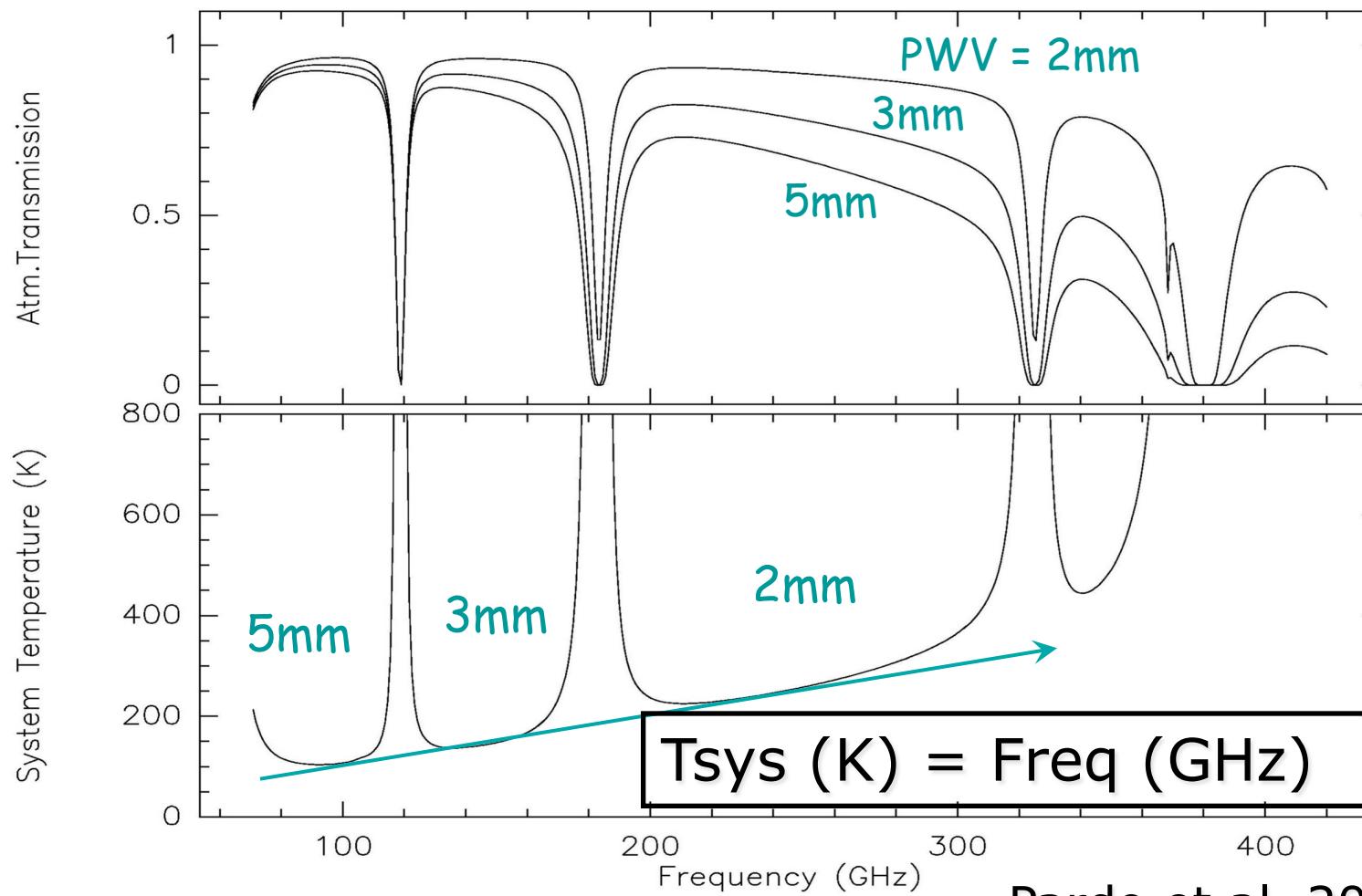
Winter values: Tamb=273K, A=1.4 airmass

ATM (Cernicharo, Pardo)



	PWV	G	η_{eff}	Trec	τ	Tsys	Obs. Tim
100 GHz	3	0.05	0.95	32	0.07	77	90%
150 GHz	3	0.05	0.92	35	0.10	113	70%
230 GHz	1	0.05	0.87	50	0.07	141	30%

NOEMA system temperatures



Pardo et al. 2007

The point source sensitivity

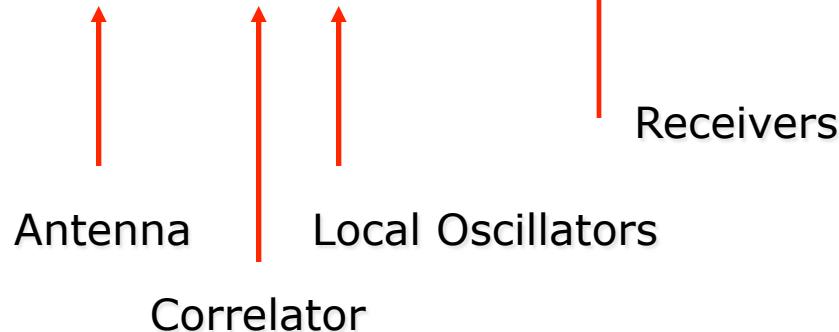
$$\sigma_S = \frac{2k}{\eta_A A} \times \frac{\langle T_{\text{SYS}} \rangle}{\eta_C \eta_J \eta_P \sqrt{N(N-1) \Delta\nu \Delta t}} \times \frac{1}{\sqrt{N_P}}$$

A	Collecting Area of a Single Antenna (177 m^2)
η_A	Aperture Efficiency (0.70 @ 3mm; 0.45 @ 1mm)
η_C	Correlator Efficiency (0.88)
η_J	Instrumental Jitter $\exp(-\sigma_J^2/2) \simeq 0.95$
η_P	Atmospheric Decorrelation $\exp(-\sigma_P^2/2) \leq 0.95$
N_P	Linear Polarizations (1 - 2)
T_{SYS}	System Temperature (K)
$\Delta\nu$	Spectral Bandwidth (39 kHz - 3600 MHz)
Δt	Integration Time On-Source (sec)

ATMOSPHERE (SITE)

Seeing Transparency

$$\sigma_S = \frac{2k}{\eta_A A} \times \frac{\langle T_{SYS} \rangle}{\eta_C \eta_J \eta_P \sqrt{N(N-1)\Delta\nu\Delta t}} \times \frac{1}{\sqrt{N_P}}$$



INSTRUMENTAL PERFORMANCE

Single Dish Efficiency (Jy/K)

$$\sigma_S = \frac{2k}{\eta_A A} \times \frac{\langle T_{SYS} \rangle}{\eta_C \eta_J \eta_P \sqrt{N(N-1)\Delta\nu\Delta t}} \times \frac{1}{\sqrt{N_P}}$$

ATMOSPHERE (SITE)

Seeing Transparency

Antenna Local Oscillators Correlator

$\eta_A = \eta_{\text{Blocage}} \cdot \eta_{\text{Spillover}} \cdot \eta_{\text{Receiver}} \cdot \eta_{\text{Ruze}}$

The diagram illustrates the components of the Single Dish Efficiency formula. At the top, a blue vertical arrow points down to the term $\frac{2k}{\eta_A A}$. Below this, a red vertical arrow points up from the term η_A to the labels 'Antenna' and 'Local Oscillators'. Another red vertical arrow points up from the term η_P to the label 'Correlator'. Above the formula, the text 'ATMOSPHERE (SITE)' is centered, with 'Seeing' and 'Transparency' positioned below it. Red arrows point down from these two terms to their respective parts in the formula. A blue circle highlights the term $\frac{2k}{\eta_A A}$.

INSTRUMENTAL PERFORMANCE

06-may-2016-holo-r1

RF: FC(B) - 06-MAY-2016 09:11:47 - beaklini@pipeline-pd - Ant 8 - W09N17N09E04W12E12N13
 Am: Rel.(B) 3C454.3 7ant-Special scans 8335 to 8438 06-MAY-2016 06:08UT El: 56.44
 Ph: Rel.(B)

rms Pha.

17 13.4 Edge taper = 12.13x 11.19 dB - offset X= -0.45 Y= 0.24 m
 27 4.87 Focus offsets (X,Y,Z) = -0.41 0.11 0.00 mm; Astigmatism = 37.6 μm (178.2deg.)
 37 5.39 Phase rms (unweighted)= 0.085 (weighted)= 0.083 radians
 47 11.6 Surface rms (unweighted)= 26.90 - (weighted)= 25.66 μm
 57 14.3 $\eta_A(86.243 \text{ GHz}) = 0.800$; $\eta_A(230.0 \text{ GHz}) = 0.767$; $\eta_A(345.0 \text{ GHz}) = 0.721$
 67 13.3 S/T(86.243 GHz)= 19.518 Jy/K; S/T(230GHz)= 20.362 Jy/K; S/T(345 GHz)= 21.651 Jy/K
 $\eta_I = 0.806 - \eta_S = 0.731 - \eta_P(86.243 \text{ GHz}) = 0.993 - \eta_P(230 \text{ GHz}) = 0.952 - \eta_P(345 \text{ GHz}) = 0.895$

Rms/ring:

29.5

23.1

22.8

22.5

25.5

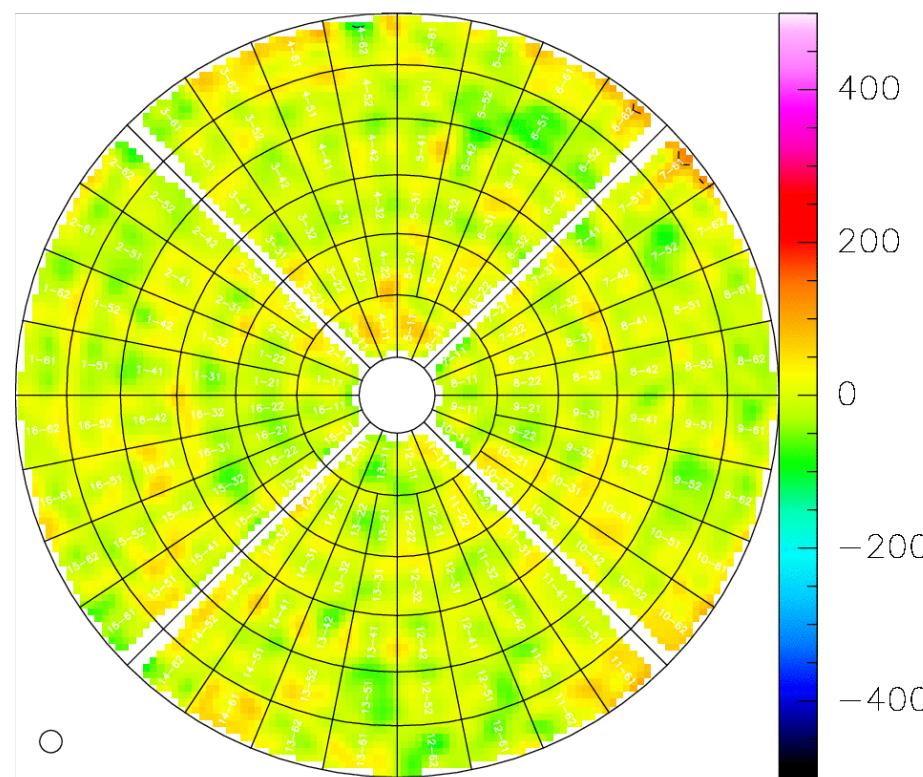
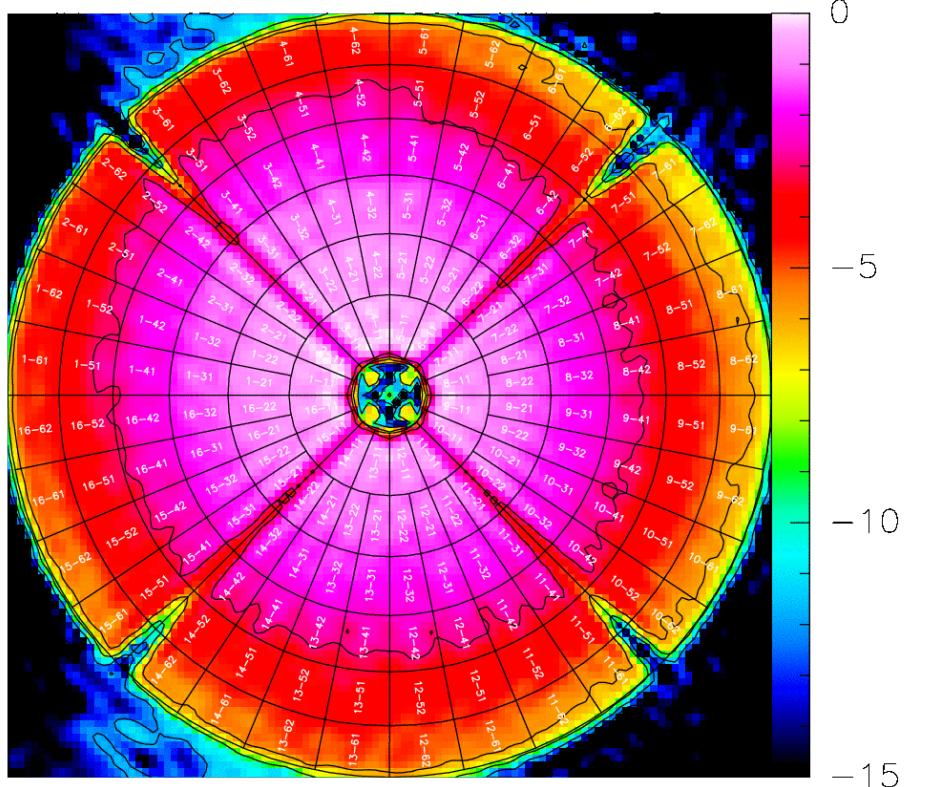
31.8

Amplitude (back view)

-15.000 to 0.000 by 3.000

Normal errors (back view)

-500.000 to 500.000 by 100.000



Interferometric Efficiency (Jy/K)

$$\sigma_S = \frac{2k}{\eta_A A} \times \frac{< T_{SYS} >}{\eta_C \eta_J \eta_P \sqrt{N(N-1)\Delta\nu\Delta t}} \times \frac{1}{\sqrt{N_P}}$$

ATMOSPHERE (SITE)

Seeing Transparency

Receivers

Antenna Local Oscillators

Correlator

The diagram illustrates the components of the Interferometric Efficiency formula. At the top, a blue arrow points down to a large blue circle representing the system. Inside the circle, three red arrows point upwards from the bottom, labeled 'Antenna', 'Local Oscillators', and 'Correlator'. Outside the circle, two red arrows point downwards from the top, labeled 'Seeing' and 'Transparency'. Above the circle, a blue arrow points down to the text 'ATMOSPHERE (SITE)'. To the right of the circle, the text 'Receivers' is shown with a red arrow pointing towards it. The formula itself is centered, with the blue circle enclosing the first term and the red arrows enclosing the second term.

INSTRUMENTAL PERFORMANCE

Point source sensitivities:

$$\begin{aligned}\sigma_S &= \frac{2k}{\eta_A A \times \eta_C \eta_J} \times \frac{\langle T_{SYS} \rangle}{\eta_P \sqrt{N(N-1)\Delta\nu\Delta t}} \times \frac{1}{\sqrt{N_P}} \\ &= \frac{2k}{\eta_A A \times \eta_C \eta_J} \times \sigma_T\end{aligned}$$

- **22** × σ_T [Jy] @ 3mm Calibration precision $\leq 10\%$
- **26** × σ_T [Jy] @ 2mm Calibration precision $\leq 15\%$
- **35** × σ_T [Jy] @ 1mm Calibration precision $\leq 20\%$

ATMOSPHERE (SITE)

Seeing Transparency

$$\sigma_S = \frac{2k}{\eta_A A} \times \frac{1}{\eta_C \eta_J \eta_P \sqrt{N(N-1)\Delta\nu\Delta t}} \times \frac{1}{\sqrt{N_P}}$$

The diagram illustrates the components of the atmospheric seeing equation. At the top, 'Seeing' and 'Transparency' are listed. Below them is a blue oval containing the term $\langle T_{SYS} \rangle$. Red arrows point from this oval to the terms $\eta_C \eta_J \eta_P \sqrt{N(N-1)\Delta\nu\Delta t}$ and $\sqrt{N_P}$ in the equation. Below the equation, red arrows point to the terms $\eta_A A$, $2k$, and $\frac{1}{\eta_C \eta_J \eta_P \sqrt{N(N-1)\Delta\nu\Delta t}}$. At the bottom, labels 'Antenna', 'Local Oscillators', and 'Correlator' are positioned under their respective red arrows. To the right of the 'Correlator' arrow is the label 'Receivers'.

Antenna Local Oscillators Correlator

Receivers

INSTRUMENTAL PERFORMANCE

One baseline, two antennas:

$$\sigma_S \simeq \frac{2k}{\eta_a A} \times \frac{\langle T_{SYS} \rangle}{\sqrt{2\Delta\nu\Delta t}} \times \frac{1}{\sqrt{N_P}} = \frac{\sqrt{T_{SYS}^1 \times T_{SYS}^2}}{\sqrt{2\Delta\nu\Delta t}} \times \frac{1}{\sqrt{N_P}} \quad [\text{Jy}]$$

Ex @ 100 GHz:

$$\sigma_S \simeq 22 \times \frac{100}{\sqrt{2 \times 0.039 \times 10^6 \times 45}} \times \frac{1}{\sqrt{1}} \simeq 1.2 \text{ Jy}$$

$$\sigma_S \simeq 22 \times \frac{100}{\sqrt{2 \times 2.5 \times 10^6 \times 45}} \times \frac{1}{\sqrt{1}} \simeq 150 \text{ mJy}$$

$$\sigma_S \simeq 22 \times \frac{100}{\sqrt{2 \times 3600 \times 10^6 \times 1}} \times \frac{1}{\sqrt{2}} \simeq 18 \text{ mJy}$$

The NOEMA array (N8, 2016):

$$\text{Ex @ 100GHz : } \sigma_S \simeq 22 \times \frac{100}{\sqrt{56 \times 3600 \times 10^6 \times 1}} \times \frac{1}{\sqrt{2}} \simeq 3.9 \text{ mJy}$$

The NOEMA array (N10, 2017):

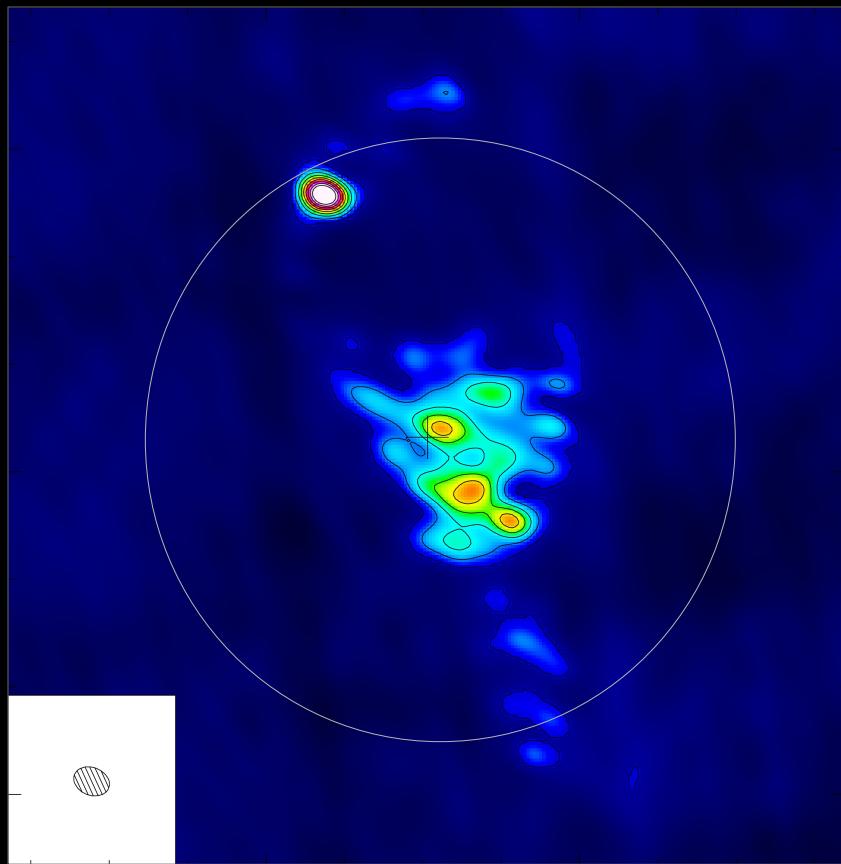
$$\text{Ex @ 100GHz : } \sigma_S \simeq 22 \times \frac{100}{\sqrt{132 \times 15600 \times 10^6 \times 1}} \times \frac{1}{\sqrt{2}} \simeq 1.3 \text{ mJy}$$

The NOEMA array (N12, 2019):

$$\text{Ex @ 100GHz : } \sigma_S \simeq 22 \times \frac{100}{\sqrt{132 \times 15600 \times 10^6 \times 1}} \times \frac{1}{\sqrt{2}} \simeq 1.1 \text{ mJy}$$

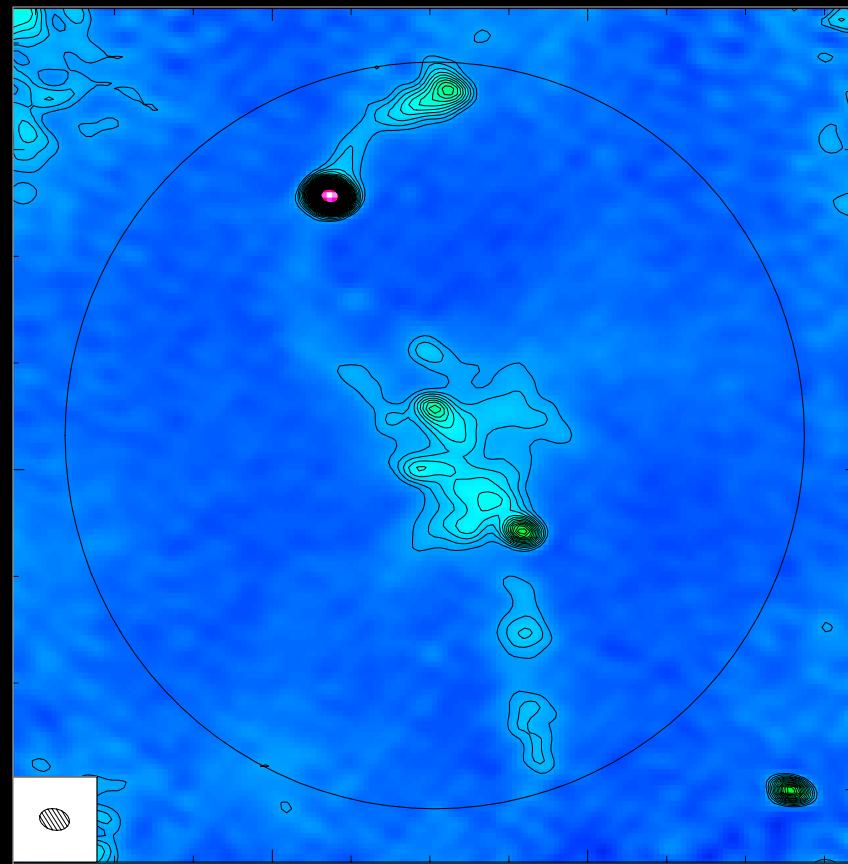
ALMA45 is twice as sensitive as N12 (continuum)

NOEMA8



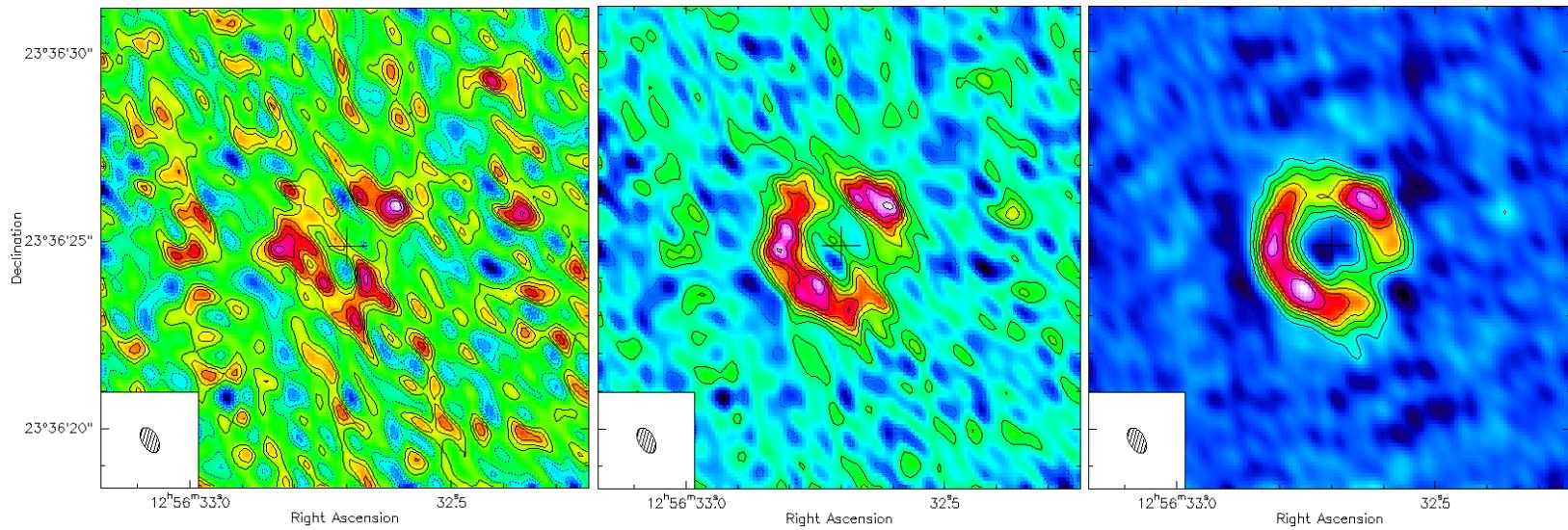
OMC2-FIR4, SOLIS LP
Caselli & Ceccarelli, B1
RMS = 0.10 mJy/(3.5x2.7'')

ALMA35 Cy 3

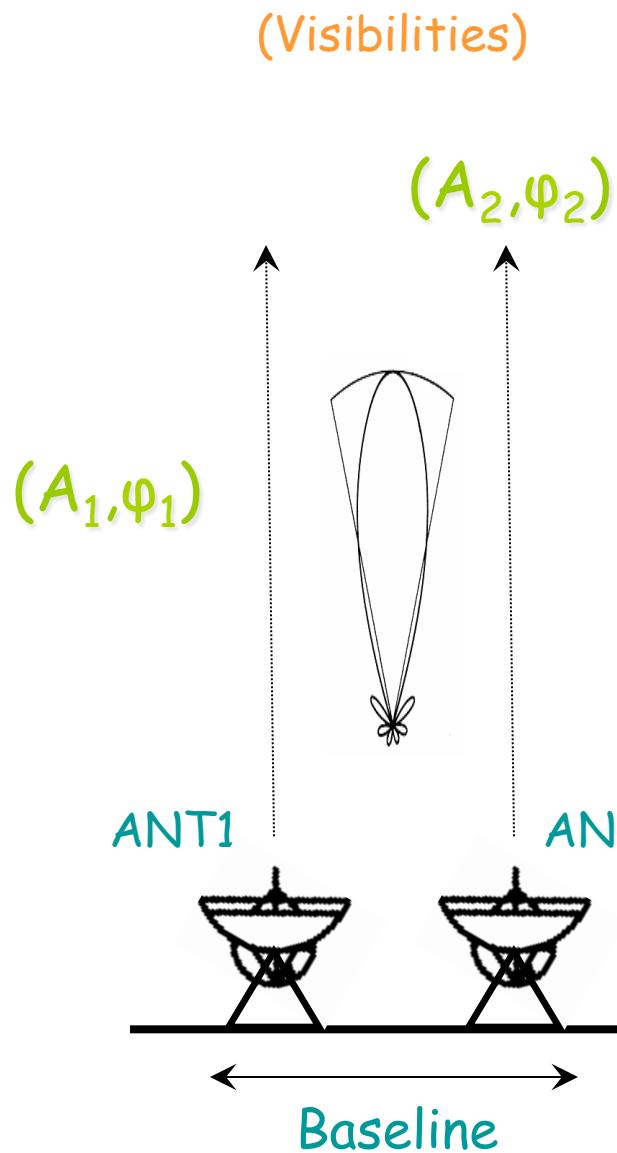


OMC2-FIR4,
Ceccarelli2015.1.00261.S, B3
RMS = 0.15 mJy/(2.9x2.0'')

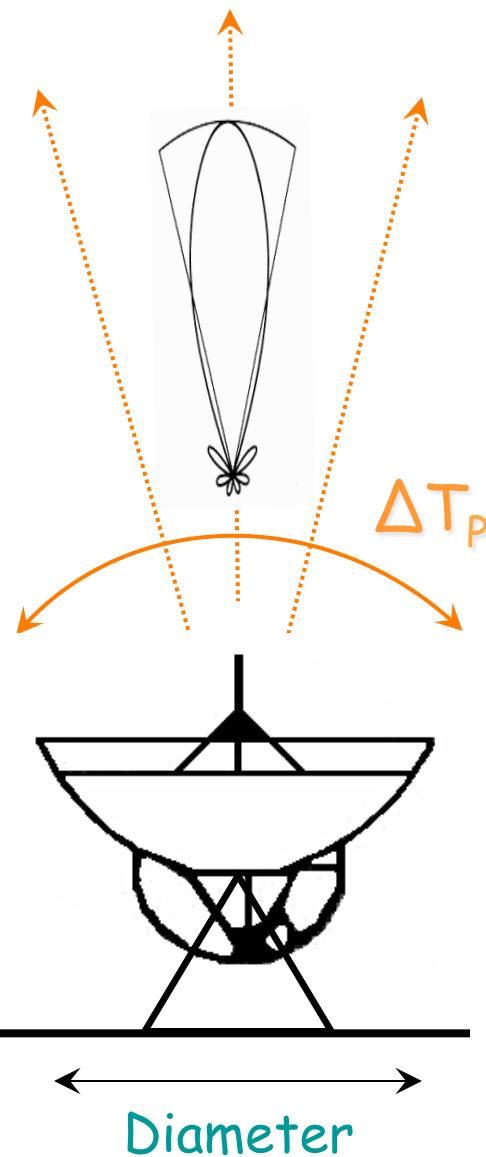
position considerations



INTERFEROMETER

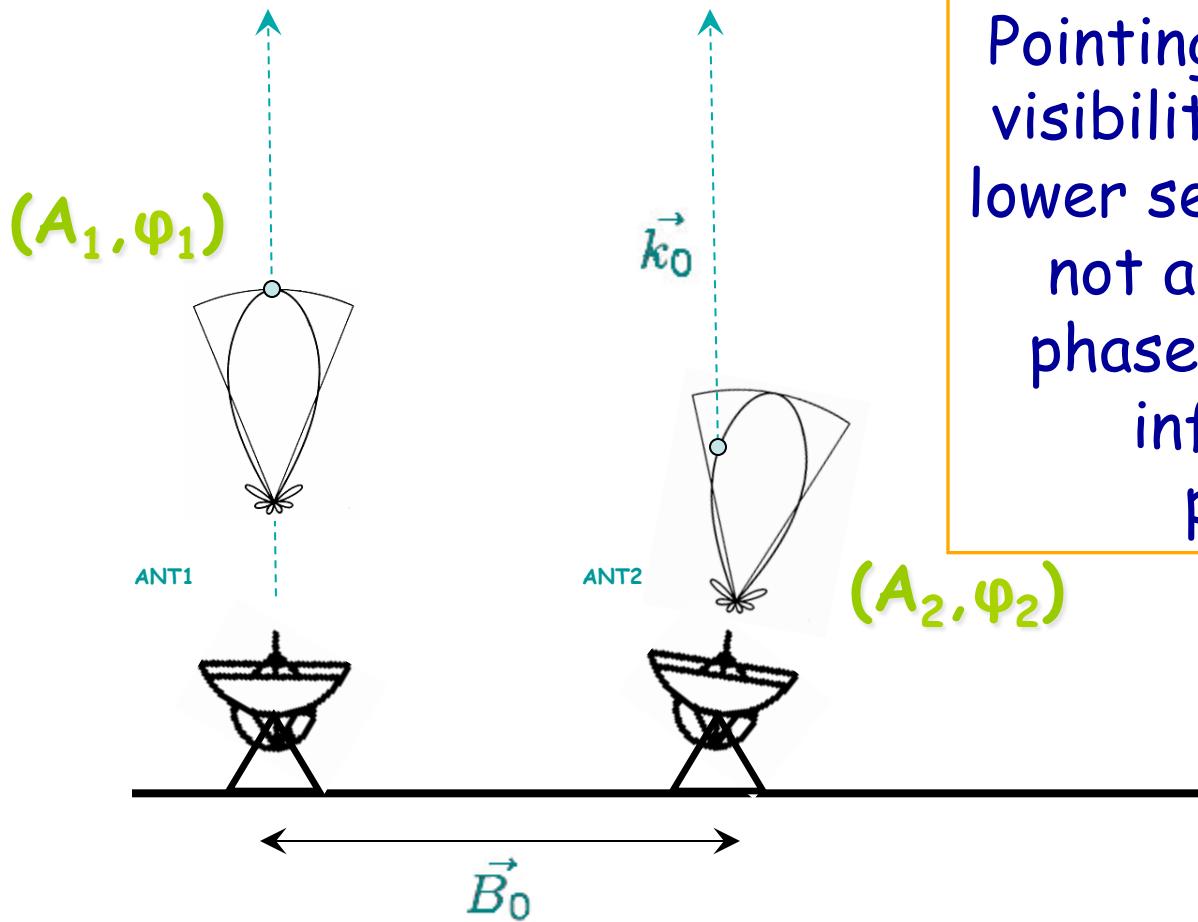


SINGLE-DISH (Total Power)



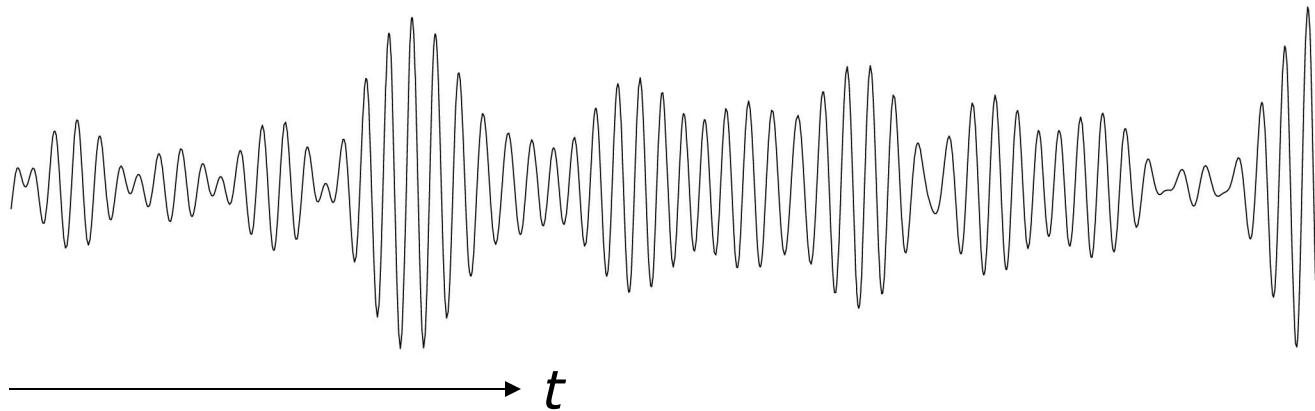
INTERFEROMETER

(Visibilities)



Pointing offsets modify visibility amplitudes (\Rightarrow lower sensitivity) BUT do not affect visibility phases (\Rightarrow positional information is preserved)

Temporal coherence function

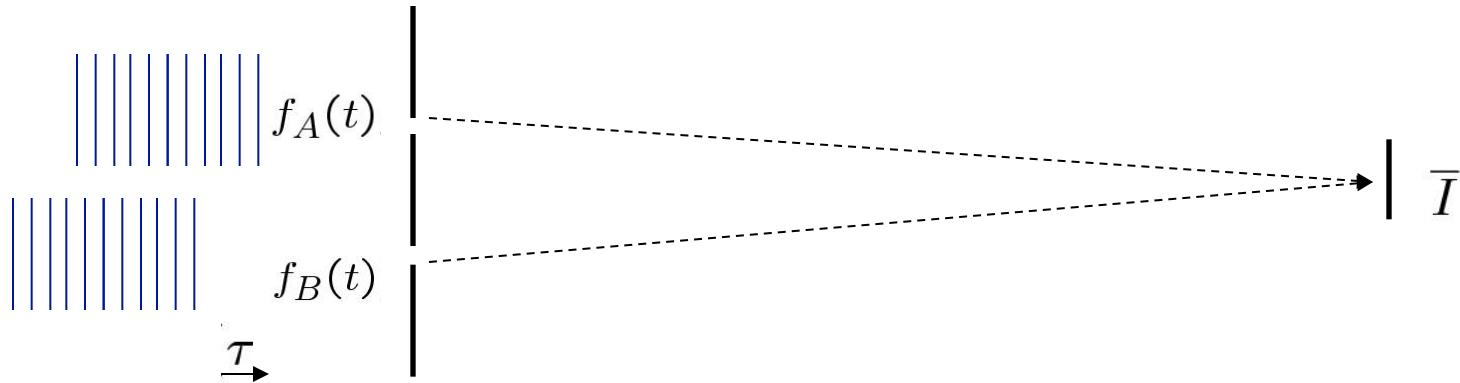


Correlation coefficient:

$$\gamma(\tau) = f(t)f^*(t + \tau)/\overline{|f(t)|^2}$$

$$f(t) = A e^{i\omega t} \quad \Rightarrow \quad \gamma(\tau) = e^{-i\omega\tau} \quad \Rightarrow \quad |\gamma(\tau)| = 1$$

Temporal coherence



Correlation coefficient:

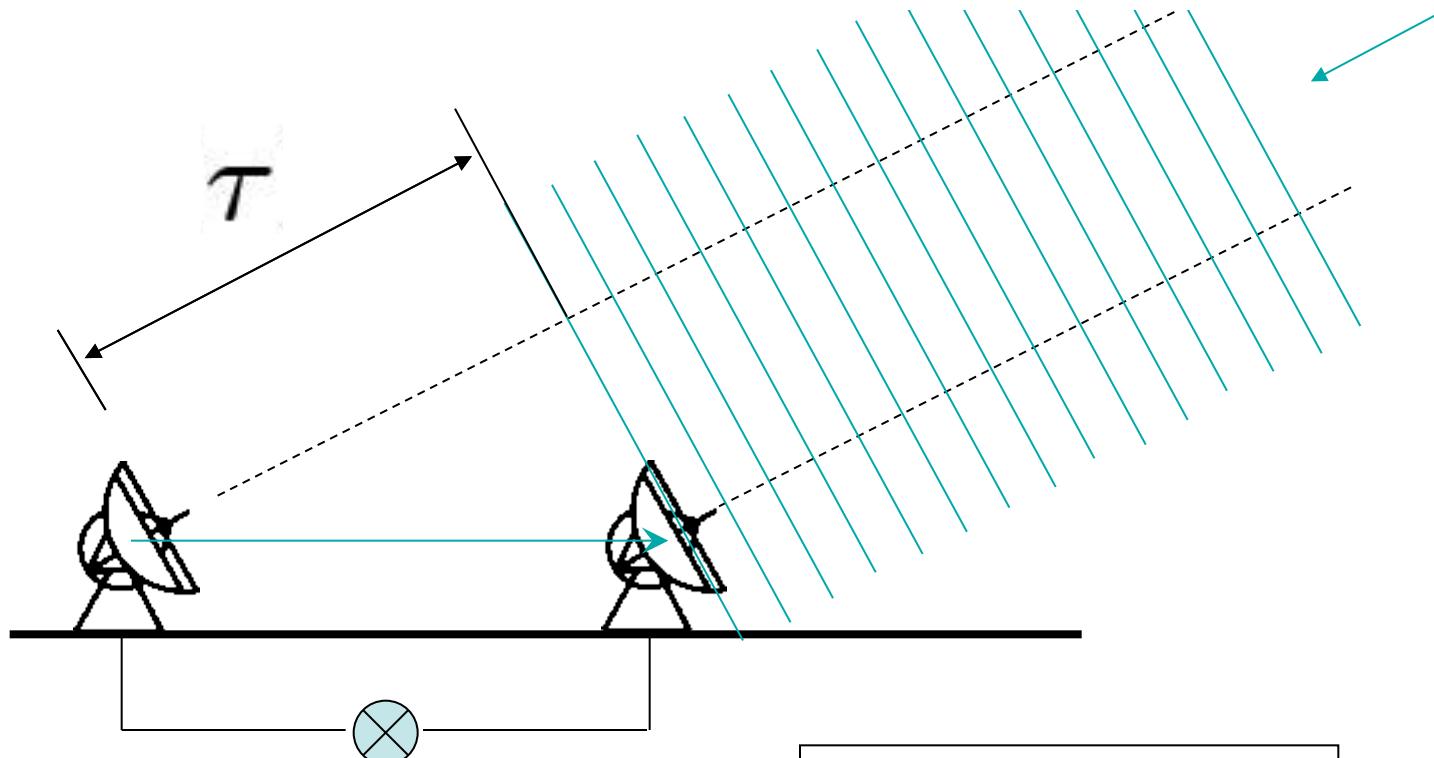
$$\gamma_{AB} = f_A(t)f_B^*(t + \tau) / (\overline{|f_A(t)|^2} \overline{|f_B(t)|^2})^{1/2}$$

$$V = \frac{I_{\max} - I_{\min}}{I_{\max} + I_{\min}} = 2|\gamma_{AB}|(\bar{I}_A \bar{I}_B)^{1/2} / (\bar{I}_A + \bar{I}_B)$$

$$\bar{I}_A = \bar{I}_B \quad \Rightarrow \quad$$

$$V = |\gamma_{AB}|$$

An interferometer
measures the temporal coherence of the
incoming wavefront



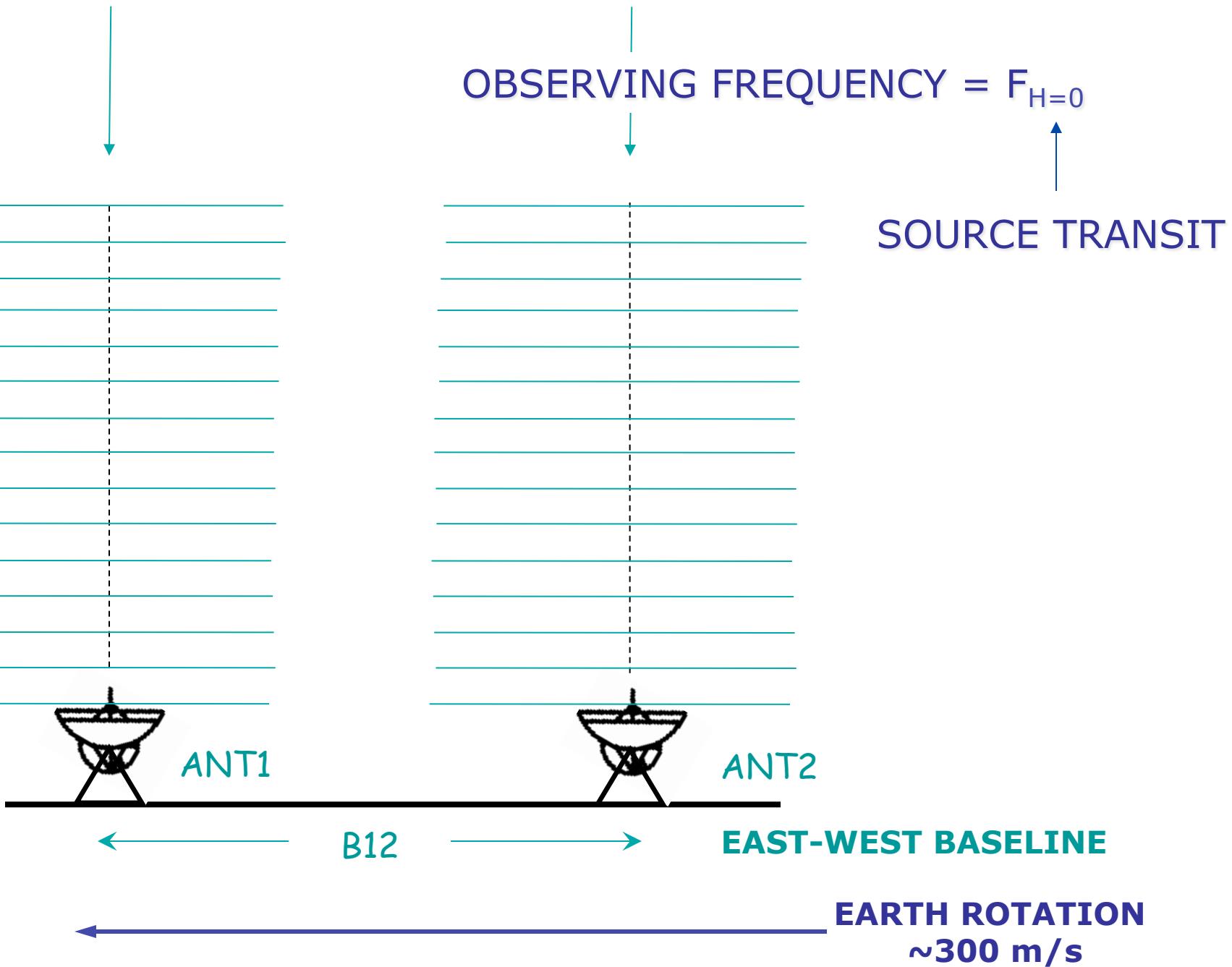
Correlator



$$V = \gamma(\tau)$$

Scan types:

- **IFPB**: auto- and cross-correlations on white noise → backend calibration.
- **AUTO**: auto-correlations on the sky → backend calibration.
- **CALI**: auto-correlations (total power measurements) on a cold load (15K), table (290K) and on the sky → interferometer temperature scale.
- **CORR**: on-target cross-correlations → complex visibilities (K) in the uv-plane.
- **POIN = CORR** → antenna pointing ($Az\pm$, $EI\pm$)
- **FOCU = CORR** → antenna focus (ΔF)
- **GAIN = CORR** → receiver image to signal sideband calibration → interferometer temperature scale.
- **FLUX = CORR** → visibility flux density calibration scale ($W/m^2/Hz/K$)

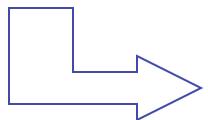


SOURCE TRANSIT

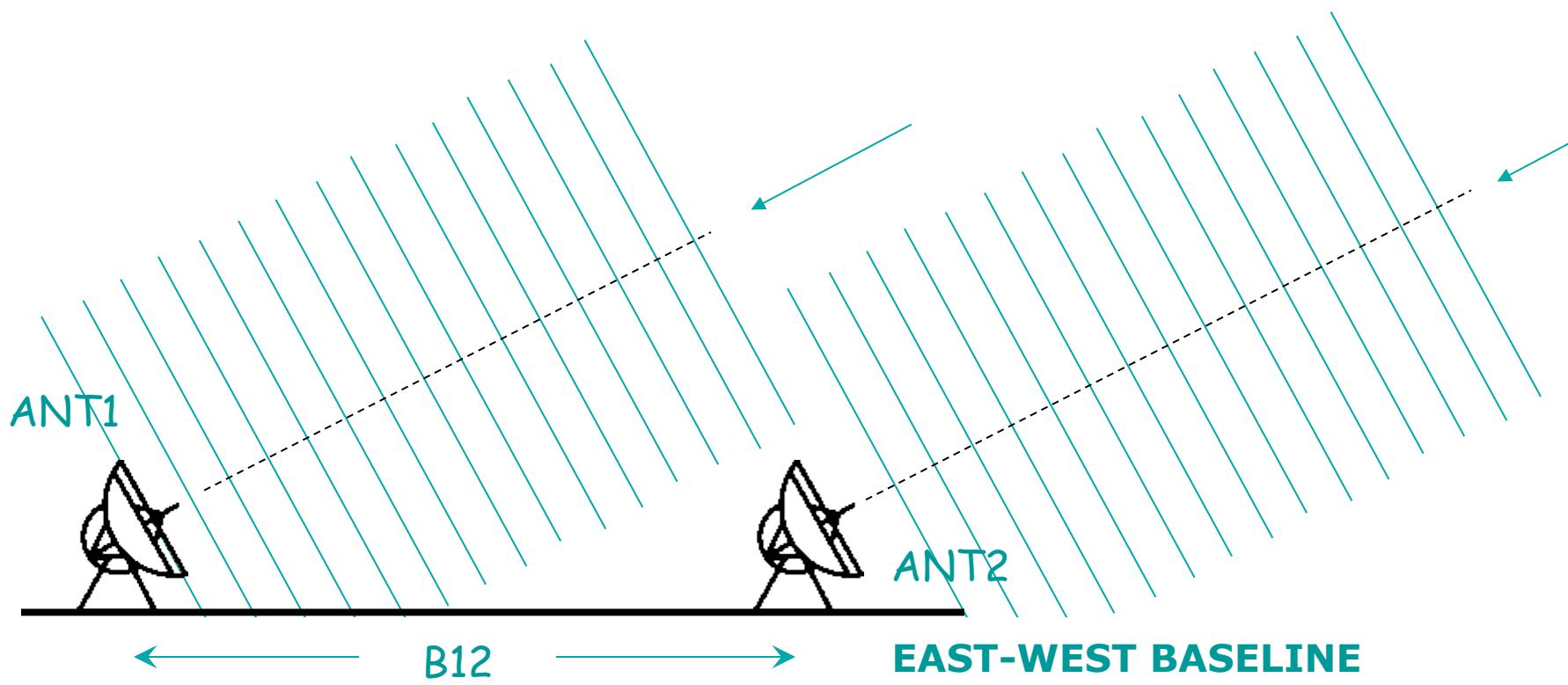
SOURCE RISES

$$F_{H<0} > F_{H=0} > F_{H>0}$$

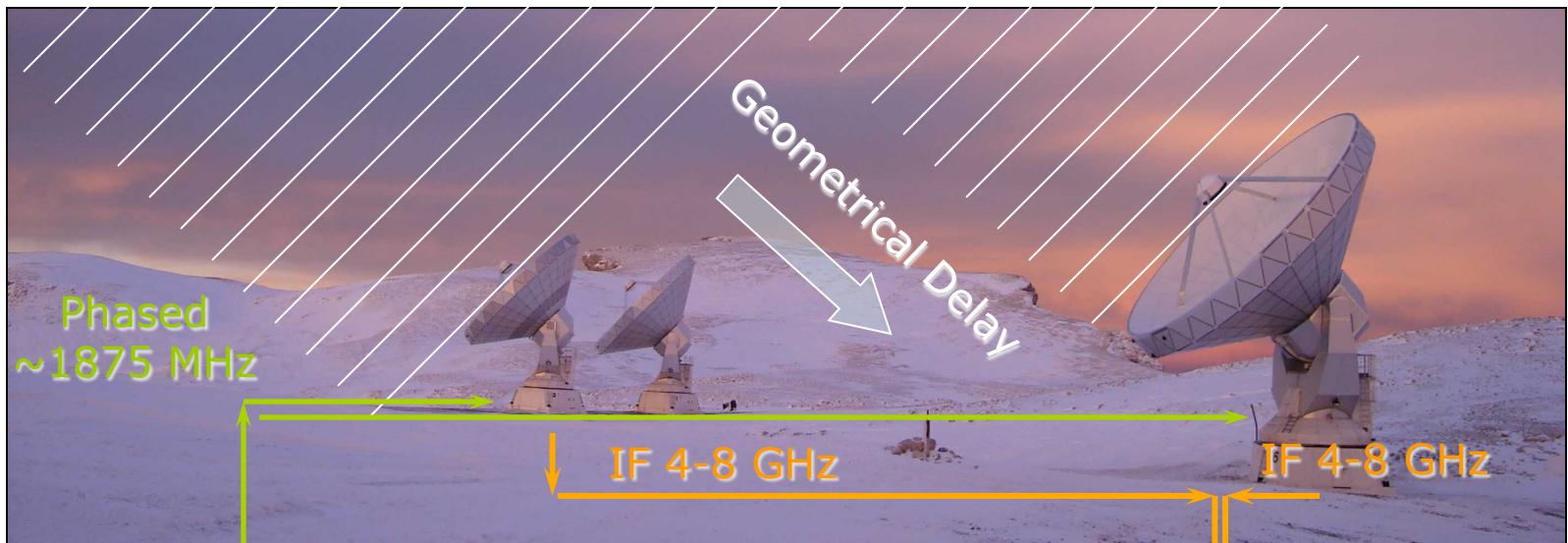
SOURCE SETS



DEPENDS ON THE SKY POSITION



EARTH ROTATION
~300 m/s



HiQ Coax

Master Frequency

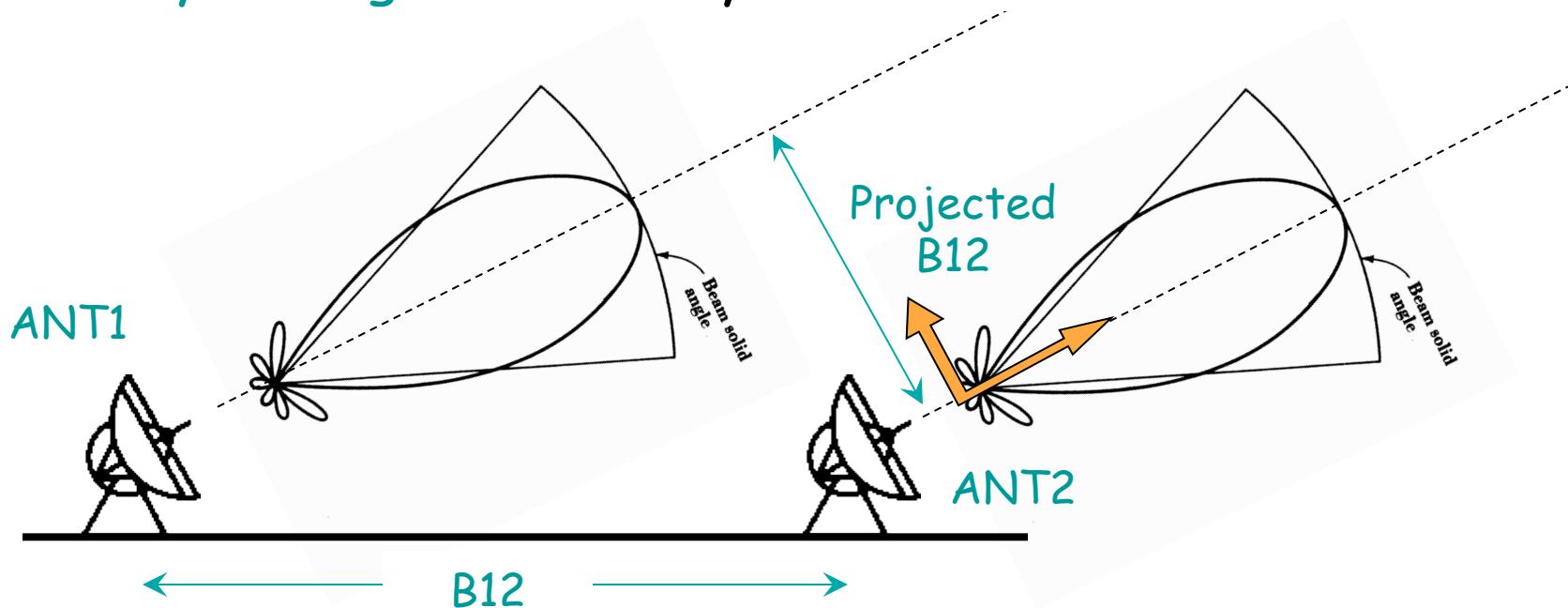
Optical Fiber

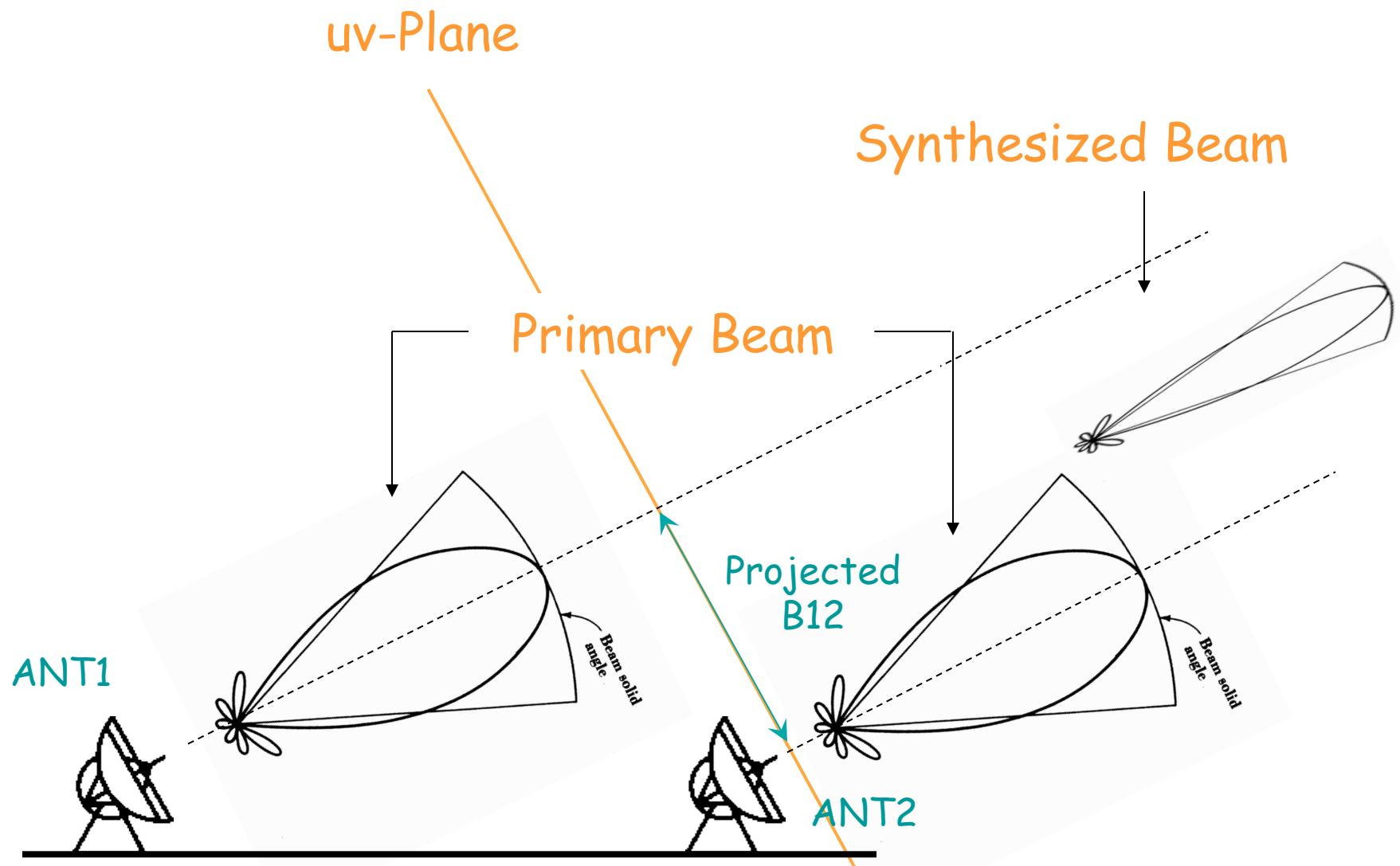


Baseline B_{ij} : distance between two antennas

Projected Baseline B_{ij} : distance between two antennas as seen from the sky

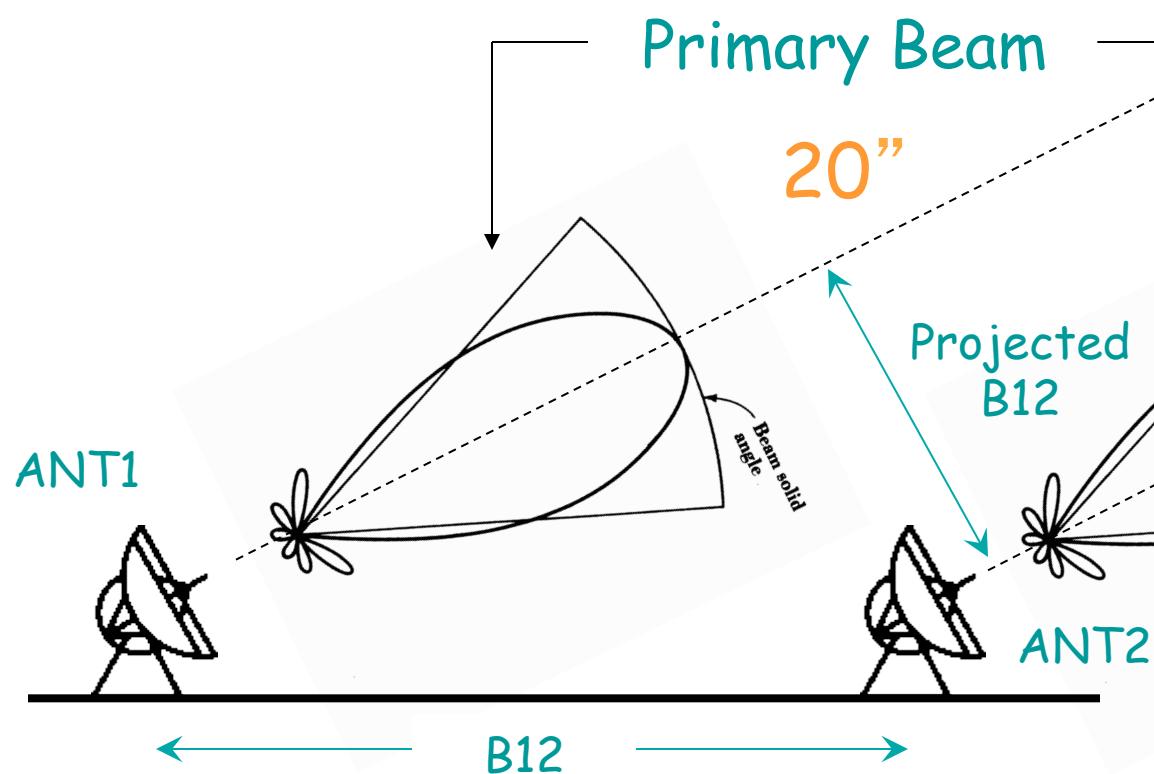
Array Configuration : layout of the antenna stations





NOEMA @ 1mm

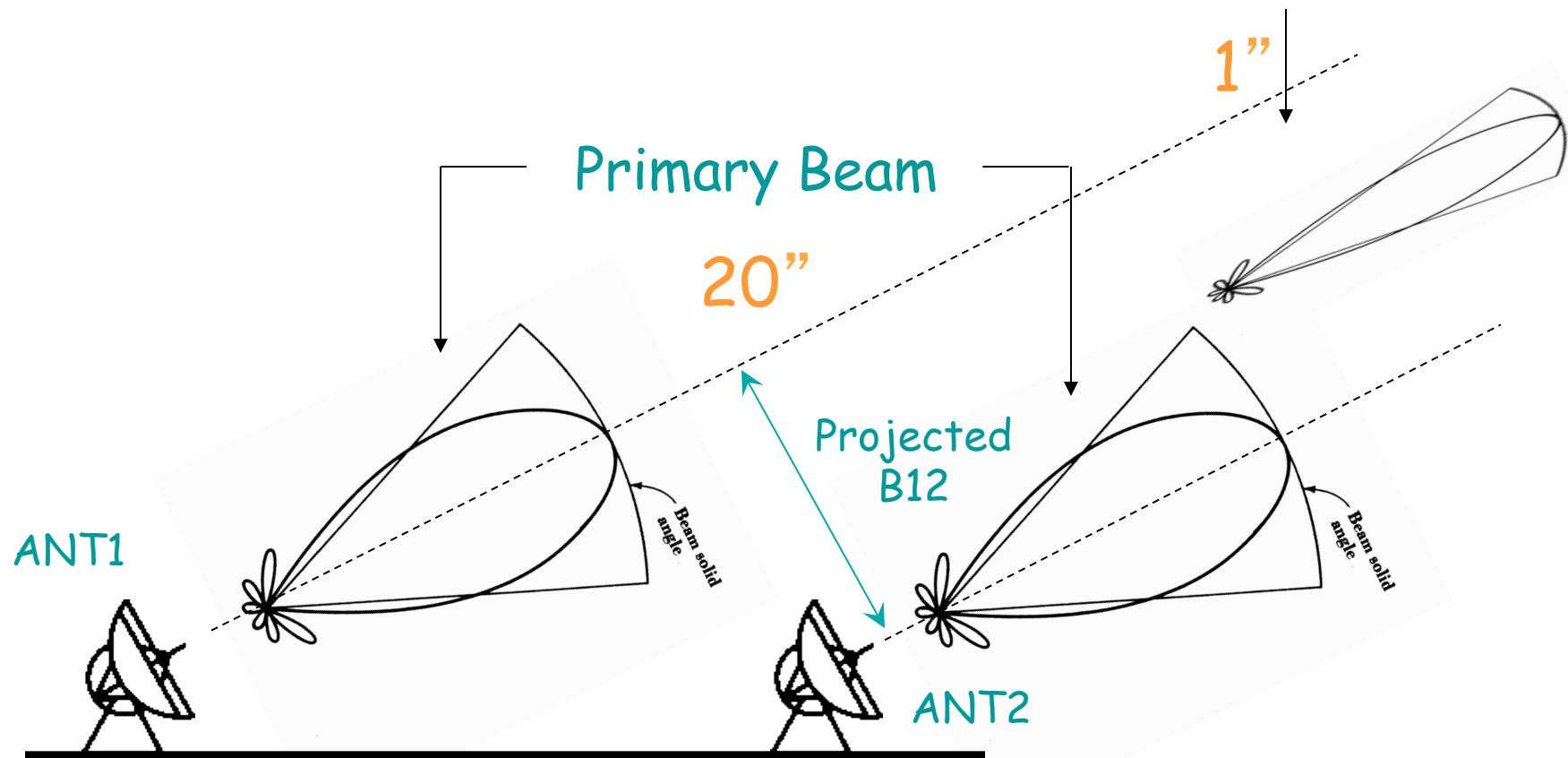
Synthesized Beam



C configuration = 200m

NOEMA @ 1mm

Synthesized Beam



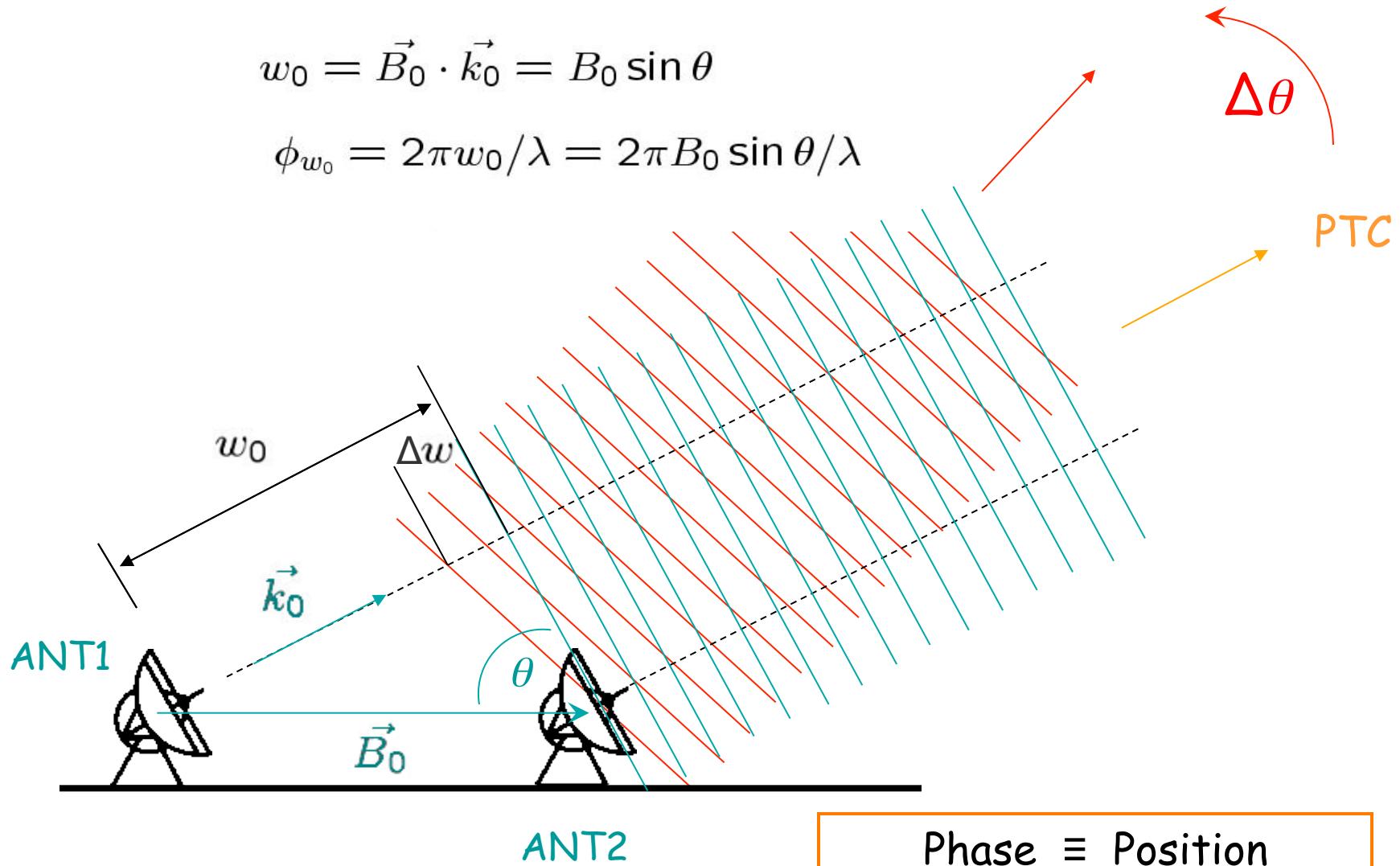
Minimum projected baseline = 15m

SHORT SPACINGS \rightarrow 30m Telescope

The phase equation

$$w_0 = \vec{B}_0 \cdot \vec{k}_0 = B_0 \sin \theta$$

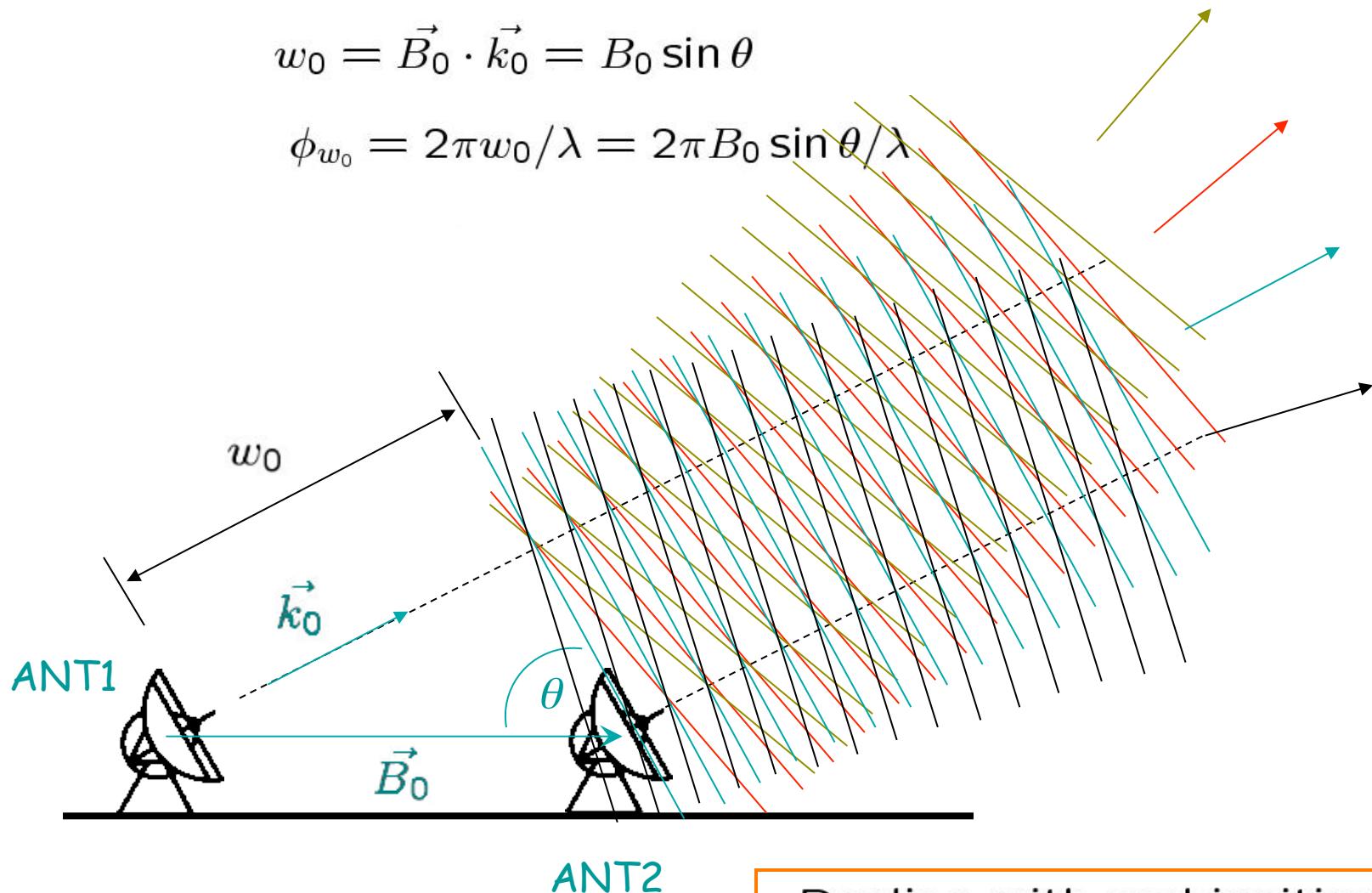
$$\phi_{w_0} = 2\pi w_0 / \lambda = 2\pi B_0 \sin \theta / \lambda$$



The phase equation

$$w_0 = \vec{B}_0 \cdot \vec{k}_0 = B_0 \sin \theta$$

$$\phi_{w_0} = 2\pi w_0 / \lambda = 2\pi B_0 \sin \theta / \lambda$$



Dealing with ambiguities ...

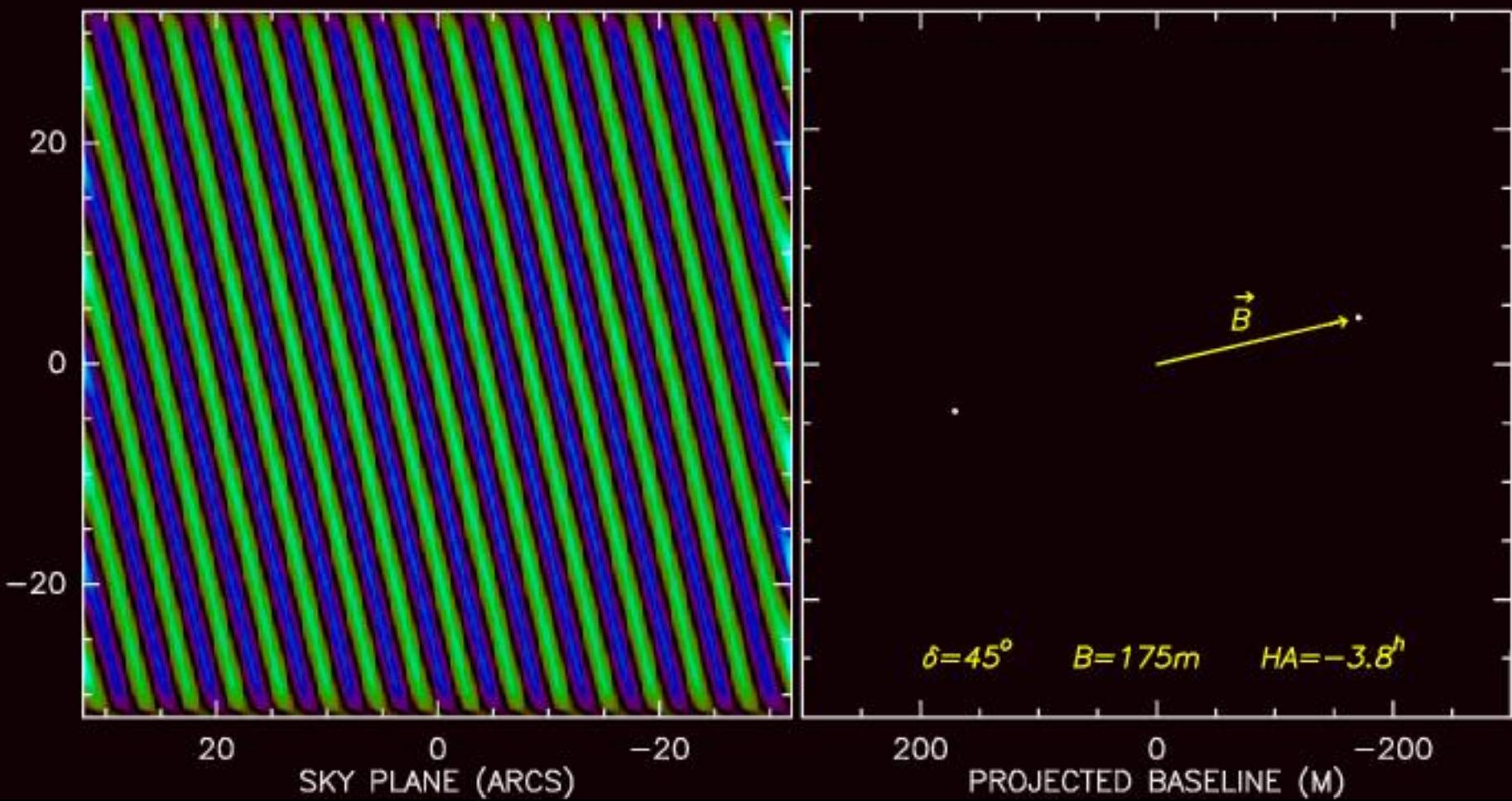
Dealing with $\omega_0 = \vec{k}_0 \cdot \vec{B}_0$

$$\rightarrow 2\pi\omega_0/\lambda = 2\pi B_0 \sin \theta/\lambda = \pm 2\pi N$$

Ex: with $B_0 = 300 \text{ m}$ and $\lambda = 3 \text{ mm}$, the positional ambiguity on the skyplane becomes:

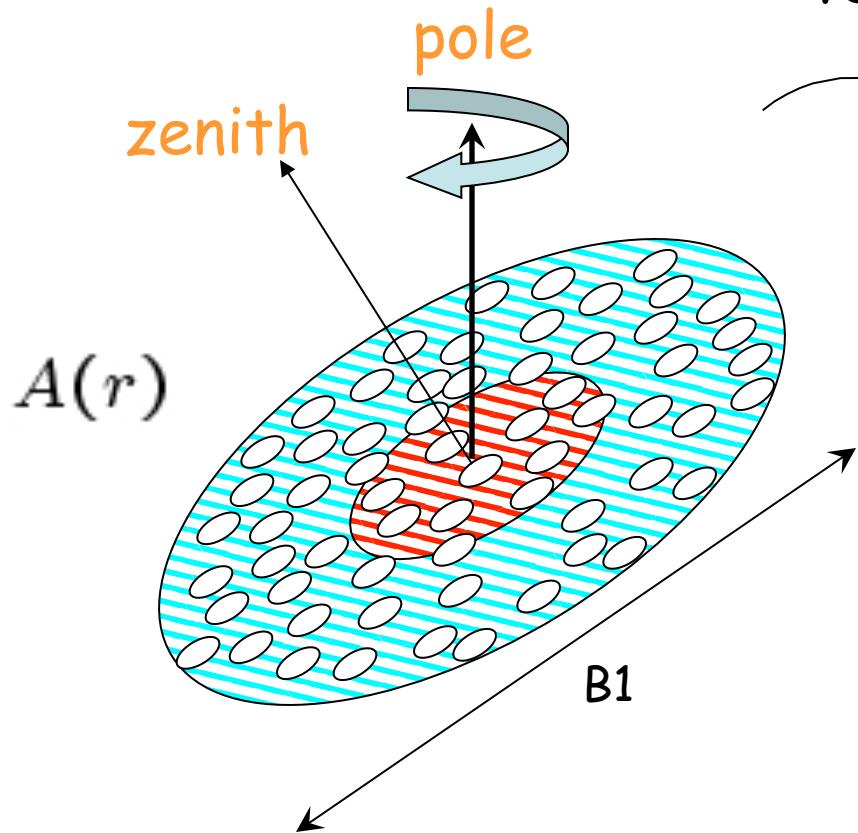
$$\theta_N = \lambda/B_0 \times N = \pm 2'' \times N$$

Ex: a source displaced by a single beam $\theta = \lambda/B_0$ shows an offset of 360° in the signal phase.

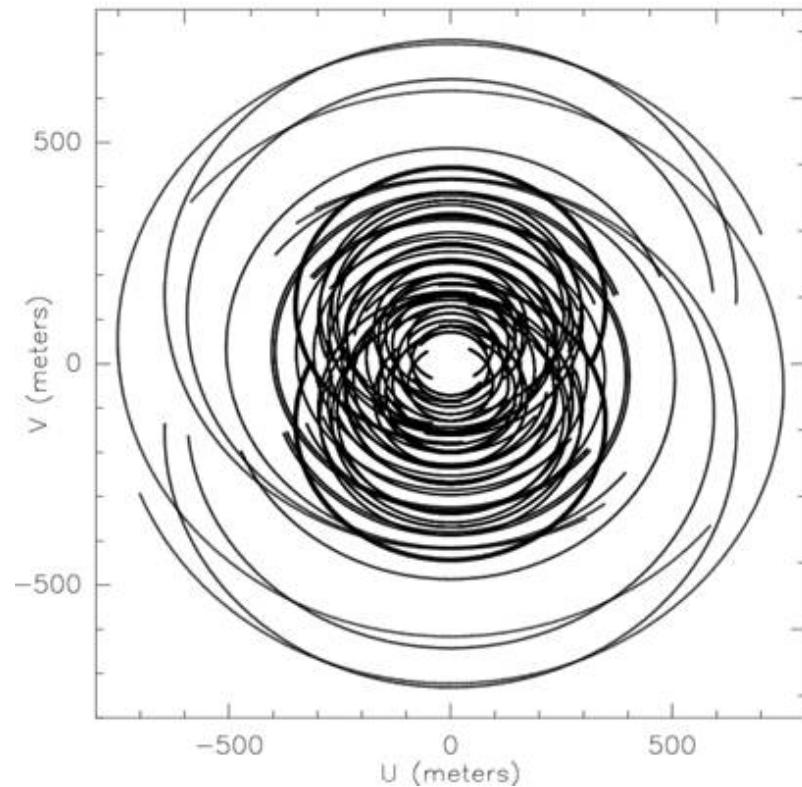


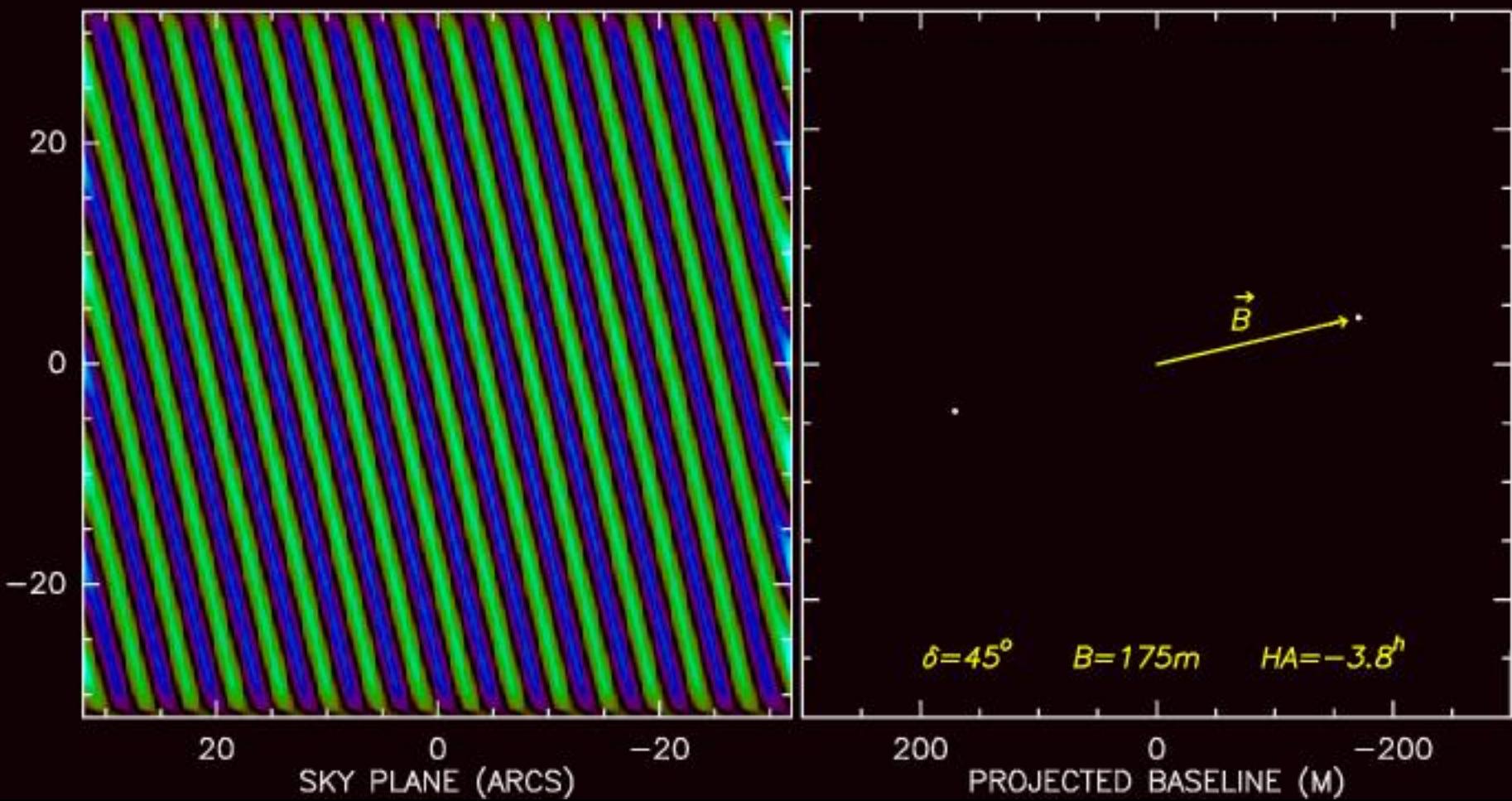
Super-Synthesis or Earth Rotation Synthesis

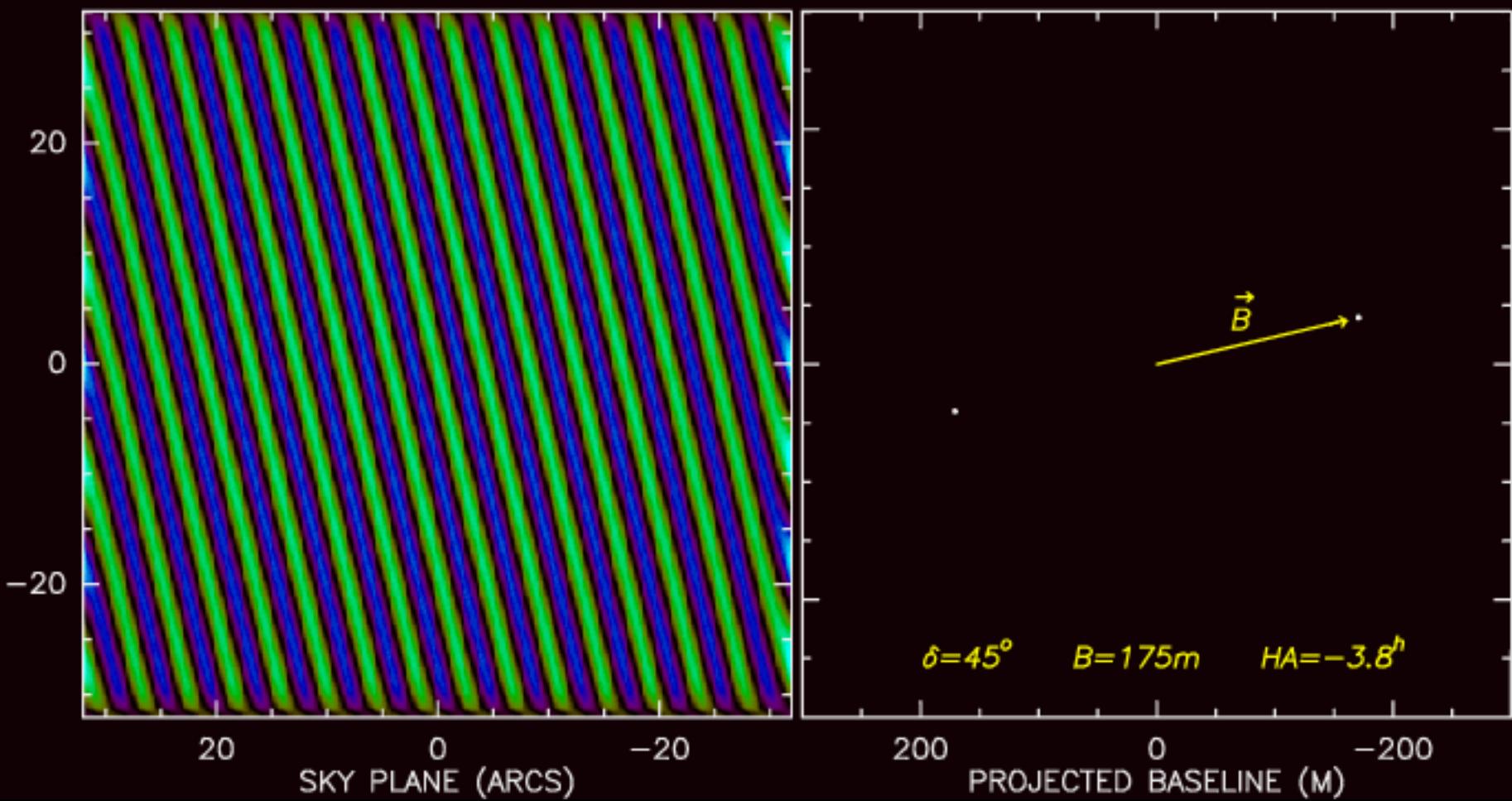
is the technique by which the elements of an interferometer sweep out the aperture of a large telescope

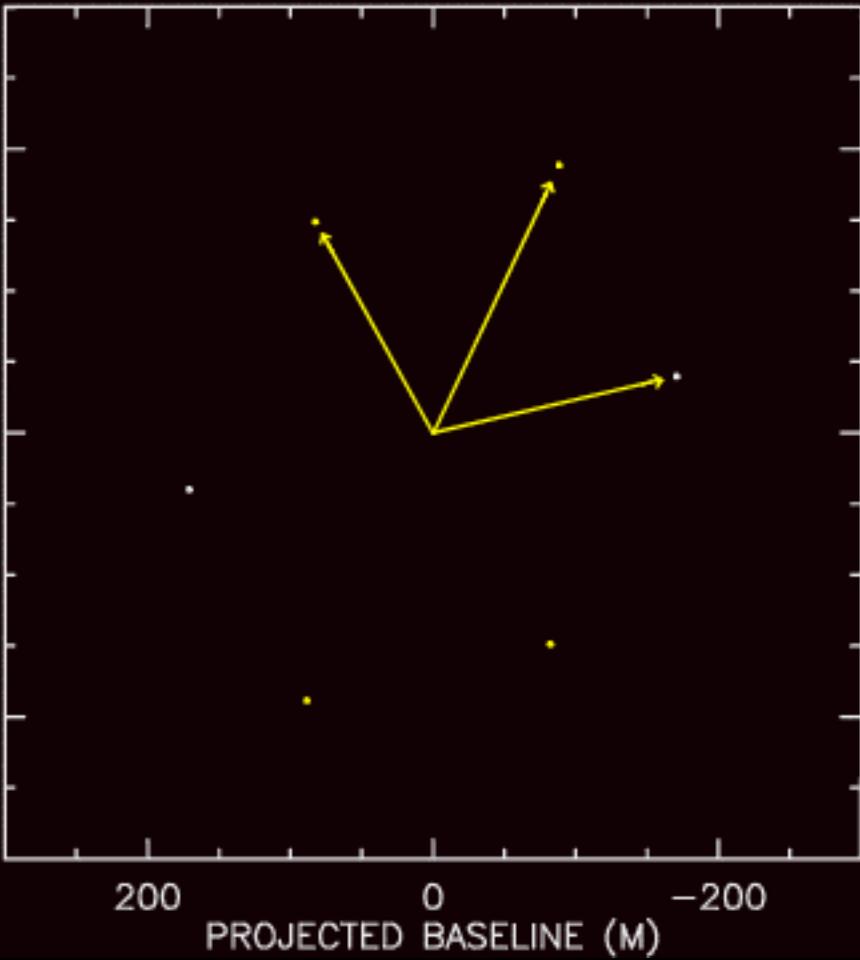
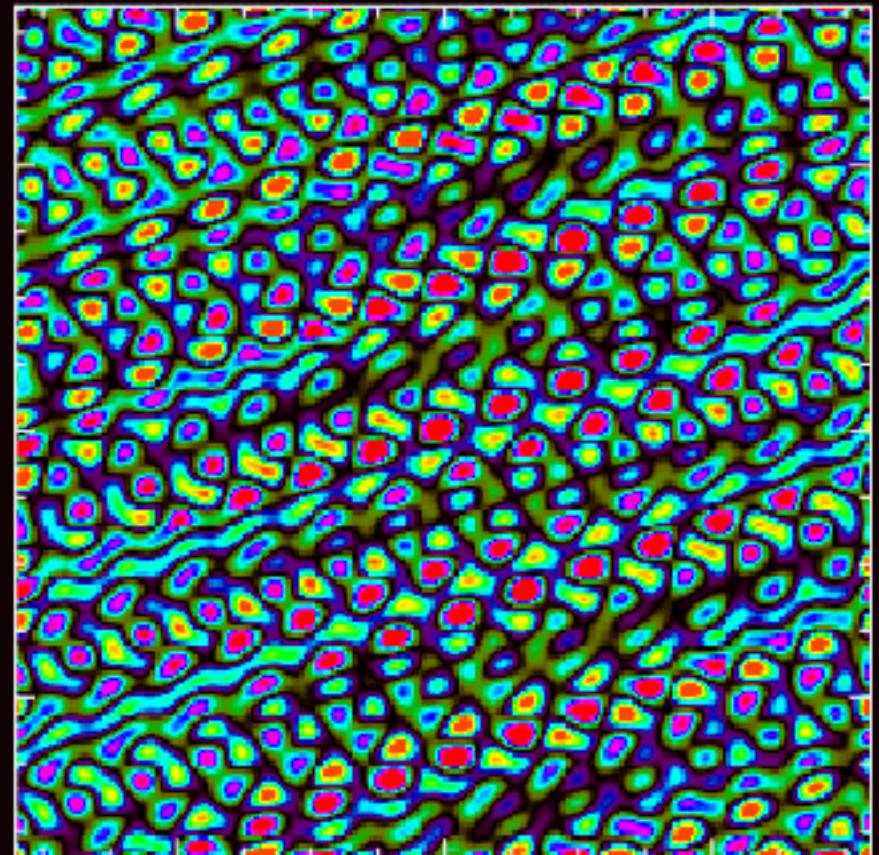


$$\text{OTF} = A(r) \star A(r)$$









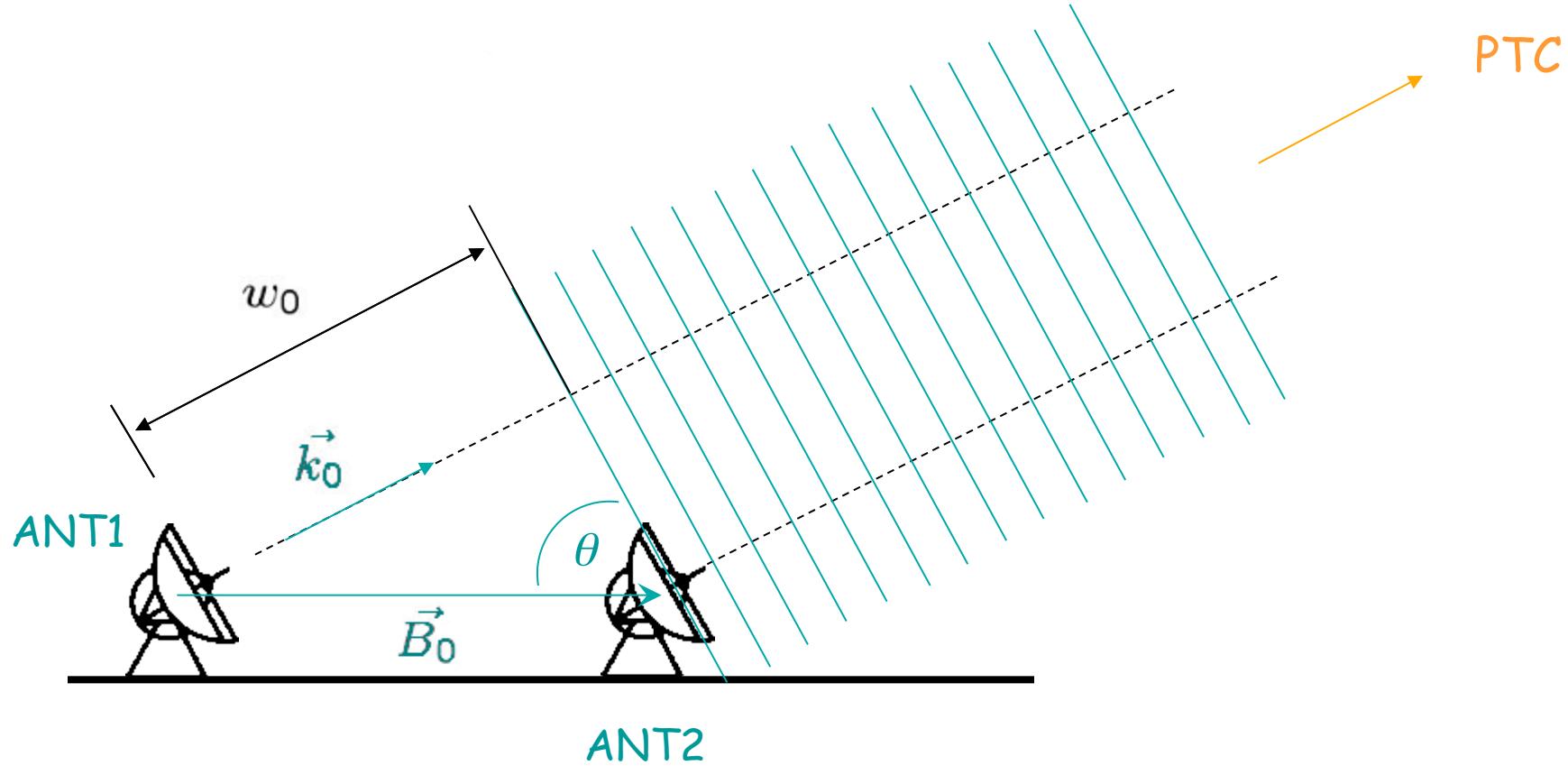
NOEMA - sources of position uncertainty

- mechanical imperfections of an antenna (+subreflector)
- wind effects on the antenna structure
- thermal load on the antenna structure
- atmospheric phase stability
- time and delay errors
- precision in the calibrators absolute position
- SNR of the source
- accuracy of baseline measurements
-

The phase equation

$$w_0 = \vec{B}_0 \cdot \vec{k}_0 = B_0 \sin \theta$$

$$\phi_{w_0} = 2\pi w_0 / \lambda = 2\pi B_0 \sin \theta / \lambda$$



$$\rightarrow \phi_{w_0} = 2\pi (B_x \cos H \cos \delta - B_y \sin H \cos \delta + B_z \sin \delta) / \lambda$$

$$\Delta\phi^{ij} = 2\pi/\lambda \cdot$$

$$[\Delta\alpha \cdot (B_x^{ij} \sin H \cos \delta + B_y^{ij} \cos H \cos \delta) +$$

$$\Delta\delta \cdot (B_y^{ij} \sin H \sin \delta - B_x^{ij} \cos H \sin \delta + B_z^{ij} \cos \delta) +$$

$$(B_x^{ij} \cos H \cos \delta - B_y^{ij} \sin H \cos \delta + B_z^{ij} \sin \delta) +$$

$$(A^i - A^j) \cos \text{EI}]$$

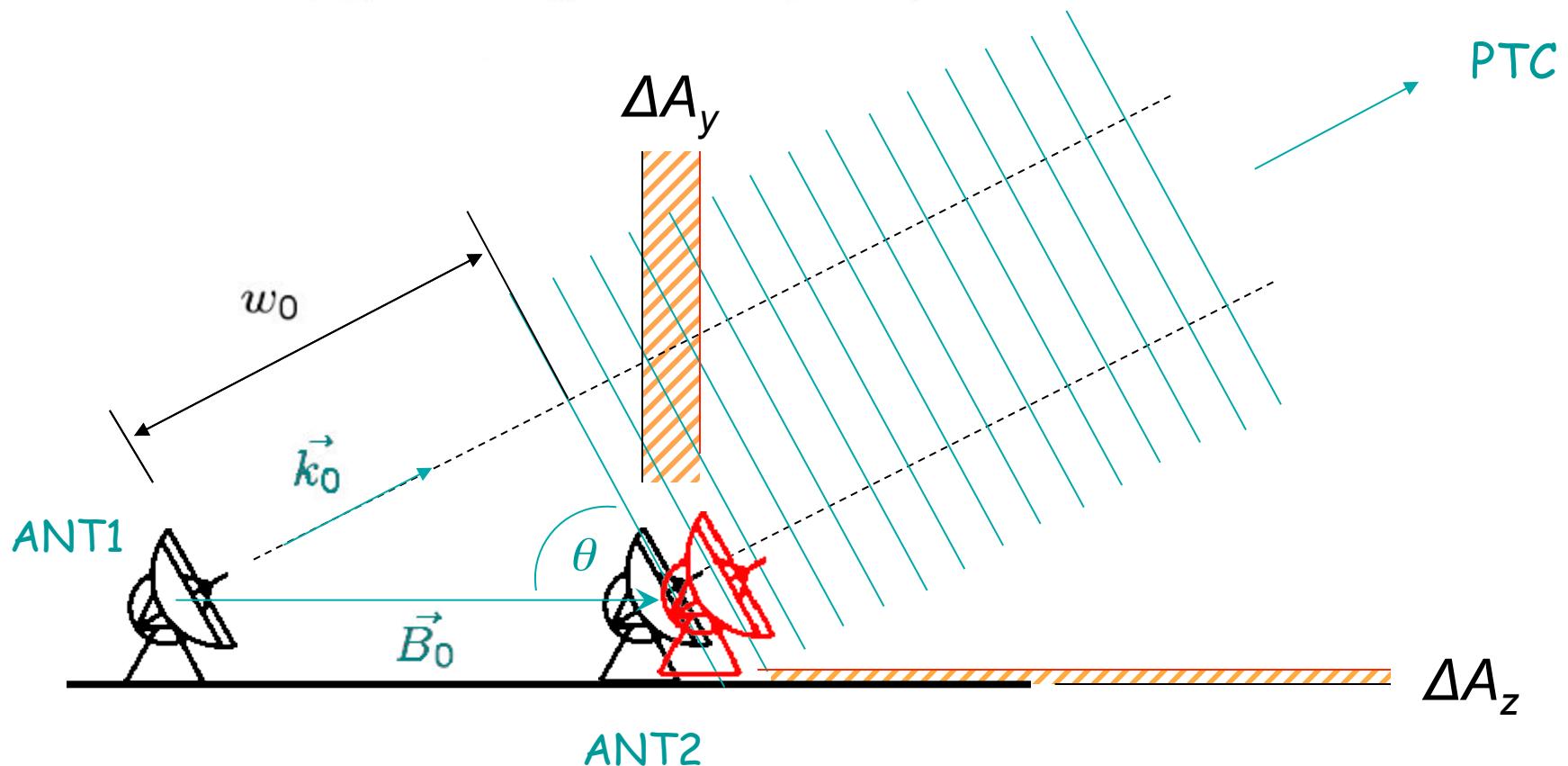
where A is the offset between the azimuth and elevation axis of an antenna.

In practice, an LSQ-analysis is used to derive the unknowns (B_x, B_y, B_z) from the measurements of the many observed $\Delta\phi^{ij}$ at 10 – 15 different hour angles H and declinations δ .

The phase equation

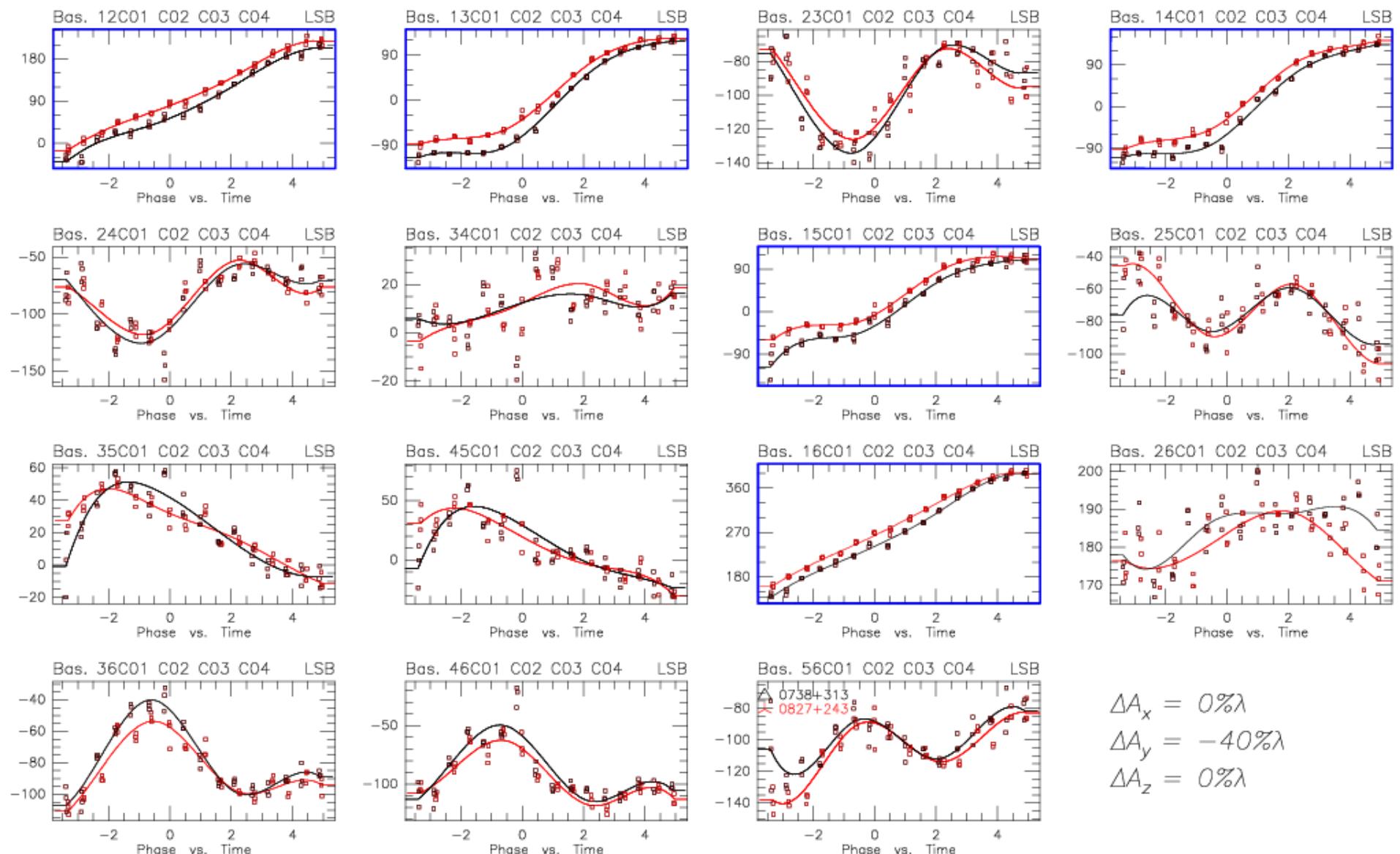
$$w_0 = \vec{B}_0 \cdot \vec{k}_0 = B_0 \sin \theta \simeq B_0 \cdot \theta$$

$$\phi_{w_0} = 2\pi w_0 / \lambda = 2\pi B_0 \sin \theta / \lambda$$

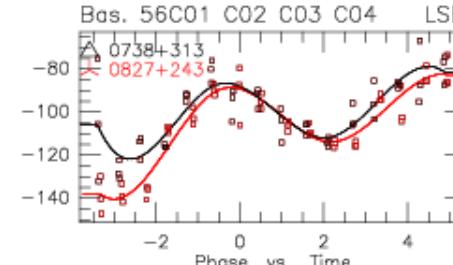


RF: Fr.(A)
 Am: Rel.(A) 100 8052 L058 0827+243 P CORR CO(3-2) 6ant-Special 08-JAN-2002 20:36 -4.3
 Ph: Abs. Atm. 788 8629 L058 0738+313 P CORR CO(3-2) 6ant-Special 09-JAN-2002 04:57 4.9

Scan Avg
Vect.Avg

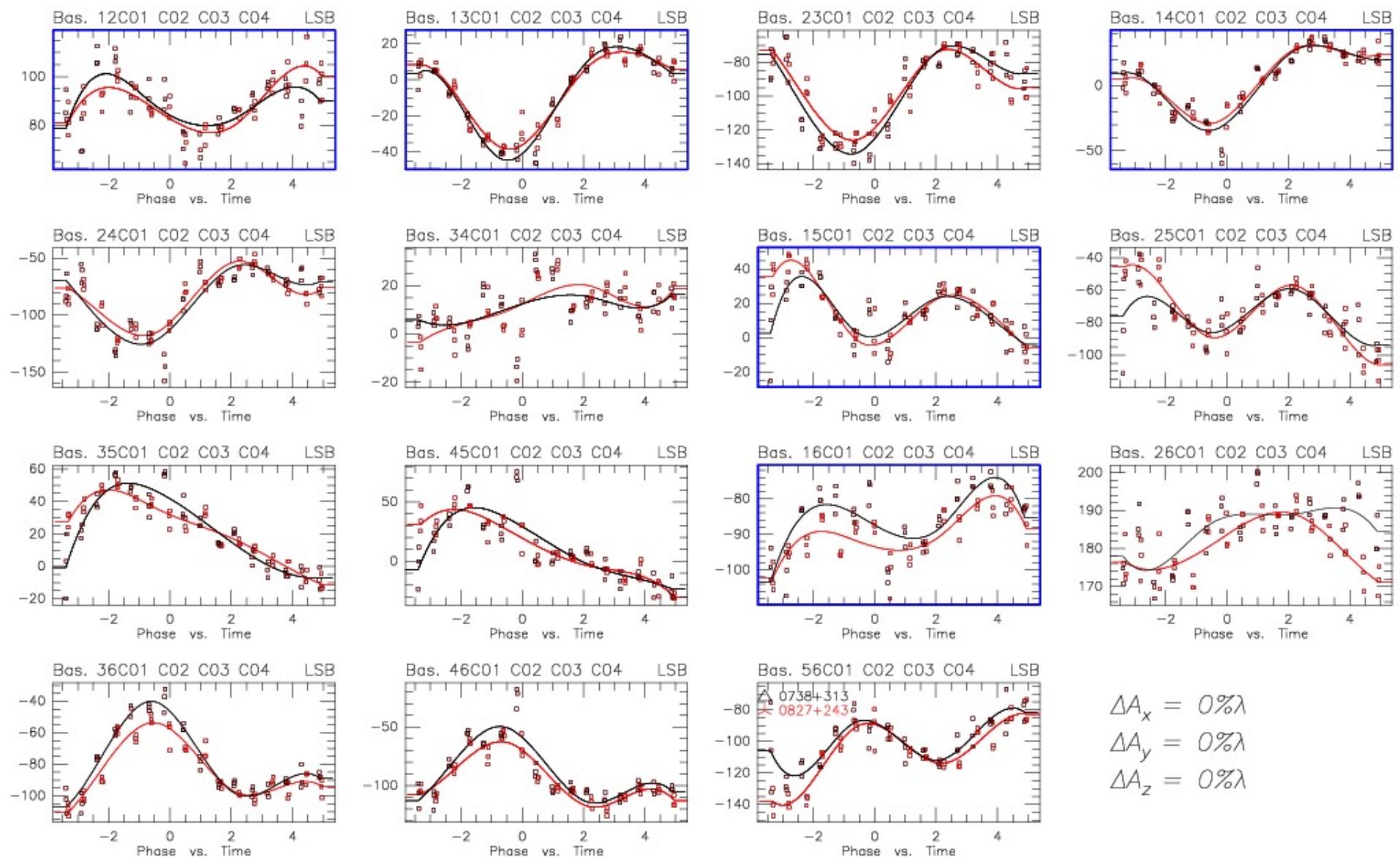


$$\begin{aligned}
 \Delta A_x &= 0\% \lambda \\
 \Delta A_y &= -40\% \lambda \\
 \Delta A_z &= 0\% \lambda
 \end{aligned}$$



RF: Fr.(A) CLIC – 25-SEP-2002 14:28:52 – neri N07N29E04W12E23N17
 Am: Rel.(A) 100 8052 L058 0827+243 P CORR CO(3-2) 6ant-Special 08-JAN-2002 20:36 -4.3
 Ph: Abs. Atm. 788 8629 L058 0738+313 P CORR CO(3-2) 6ant-Special 09-JAN-2002 04:57 4.9

Scan Avg
Vect.Avg



$$\Delta A_x = 0\% \lambda$$

$$\Delta A_y = 0\% \lambda$$

$$\Delta A_z = 0\% \lambda$$

NOEMA - sources of position uncertainty

TELESCOPE	$\Delta\theta$	Calibration
Axes Non-Intersection	$\leq 0.20''$	Yes
AzEl Bearings	$\leq 0.15''$	Yes
OBSERVATION		
Focus Offset	$\leq 0.15''$	Partially
Calibrator Distance	$\leq 8 \cdot 10^{-2} \theta_B$	No
Atmospheric Seeing	$\leq 6 \cdot 10^{-2} \theta_B$	No
Pointing Offset	$\leq 2 \cdot 10^{-2} \theta_B$	Partially

NOEMA - sources of position uncertainty

OBJECT	$\Delta\theta$	Calibration
Source Intensity	$\leq 10^{-1} \theta_B$	No
Calibrator Position	$\leq 0.02''$	No
MISCELLANEOUS		
Bandwidth smearing	$\leq 0.08''$	No
Visibility averaging	$\leq 0.06''$	No
Gravitational lensing	$\leq 0.02''$	No
Primary beam correction	$\leq 0.02''$	No