

# Calibration principles



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# Data calibration

## Outline

- **Introduction**
- **Formalism**                      deriving antenna gains
- **Bandpass**                      phase and amplitude vs freq
- **Phase**                              phase vs time
- **Amplitude**                      amplitude vs time
- **Flux**                                absolute flux scale



# Introduction

## Calibrations

- Pointing
- Focus
- IF filters band pass
  
- Atmospheric calibration ( $T_a^*$ )
- Antenna positions
- Delay
  
- Atmospheric phase correction

Real-time  
calibrations

Done real-time but  
new values can be  
entered off-line if  
necessary

Done real-time but  
uncorrected data  
are also stored



# Introduction

## Calibrations

- Bandpass (amplitude and phase vs. frequency)
- Phase vs. time
- Amplitude vs. time
- Absolute flux scale

Off-line calibration  
(done/checked by PIs)

- 
- At any time  $t$ , the interferometer provides:
    - $V(\nu, t)$  = spectrum
    - $V(t)$  = continuum data = spectrum average
  - We do **not** consider  $(u, v)$  dependence, only  $t$



# Formalism

## Visibilities

- Calibrate only temporal or frequency effects, do not consider dependence on  $(u,v)$
- True visibility:  $V_{ij}(v,t)$  (baseline  $ij$ )
- Observed visibility:

$$V_{\text{obs}ij}(v,t) = G_{ij}(v,t) V_{ij}(v,t) + \text{noise}$$

- $G_{ij}$  = complex gain (amplitude & phase)
- Scalar description – no polarization



# Formalism

## Gain decomposition

- **Most of the effects are antenna-based**
  - Pointing, Focus, Antenna position, Atmosphere, Receivers noise, Receivers bandpass...
- **Gain decomposition:**  $V_{obs_{ij}} = G_{ij} V_{ij} = g_i g_j V_{ij}$
- Baseline-based effect?
  - Correlator bandpass → real-time calibration
  - Time and frequency averaging → **decorrelation**



# Formalism

## Antenna-based gains

- Observation of a **point source** of flux  $S$ :

$$V_{\text{obs}} = G_{ij} V \quad V = S \quad \rightarrow \quad V_{\text{obs}} = G_{ij} S$$

- Antenna –based gains:  $V_{\text{obs}} = g_i g_j S$

- • Can solve for antenna gains with 3 antennas

$$(g_1)^2 = \frac{V_{\text{obs}}_{12} V_{\text{obs}}_{31}}{S V_{\text{obs}}_{23}}$$



# Formalism

## Antenna-based gains

- Observation of a **point source** of flux  $S$ :

$$V_{\text{obs}} = G_{ij} V \quad V = S \quad \rightarrow \quad V_{\text{obs}} = G_{ij} S$$

- Antenna –based gains:

$$V_{\text{obs}} = g_i g_j S$$



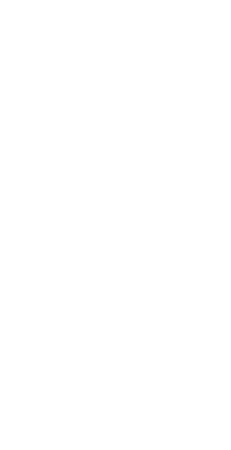
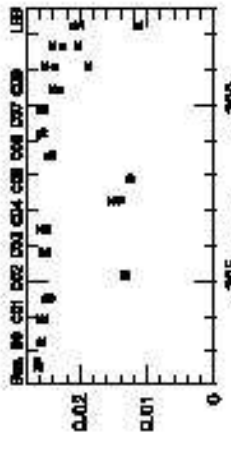
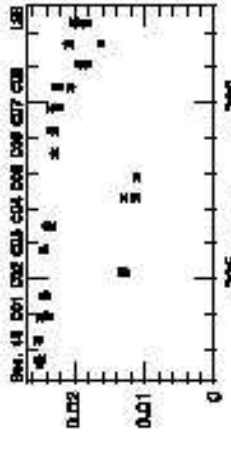
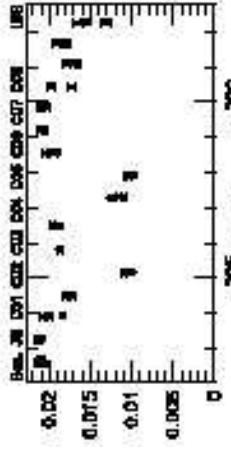
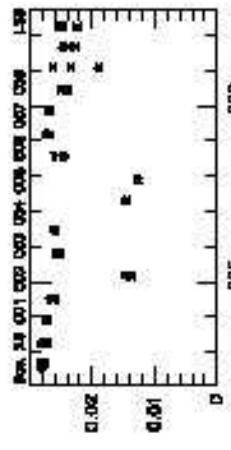
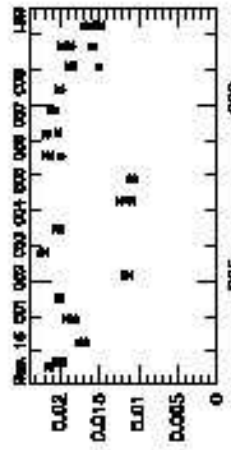
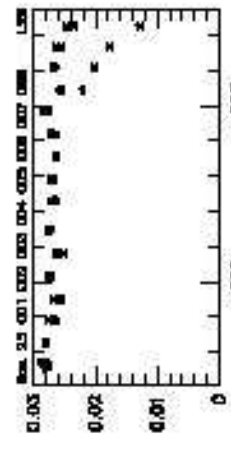
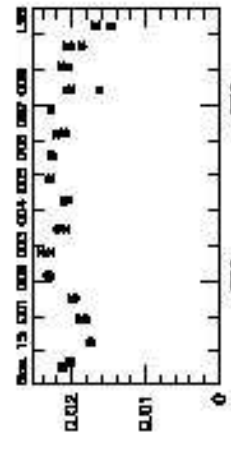
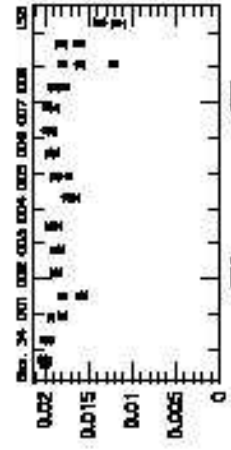
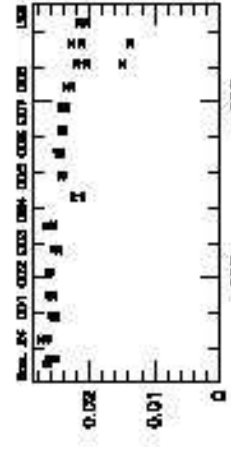
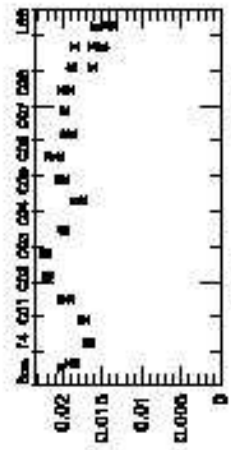
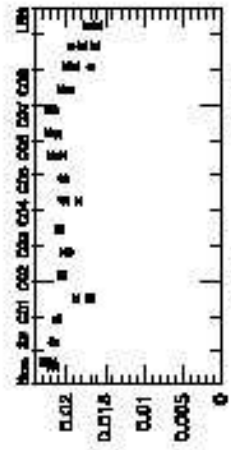
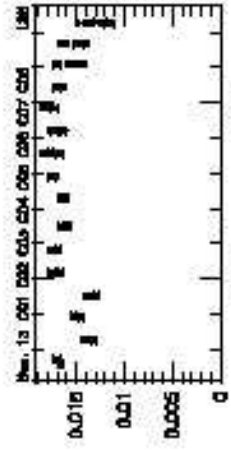
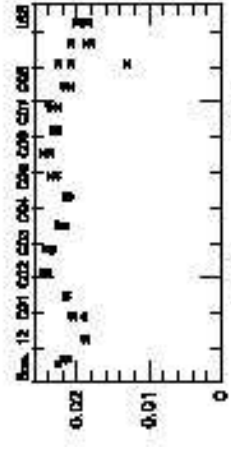
- $N$  complex unknown (one  $g_i$  per antenna)
- $N(N-1)/2$  equations (one per baseline)
- **System is over-determined** and may be solved by a method of **least squares**



RF: Uncond.  
Arr: Abs.  
Ph: Abs.

CLIC - 04-OCT-2010 20:56:49 - gueth@dhcp - W27E04E68N46N29E24 6Aq  
TAS F 12CO(2-1 230.538GHz B3 Q3(160,320,320)V Q3(160,320,320,320)H  
Ph: (157 7275 P CORR) - (1116 8050 P CORR) 23-JAN-2010 14:33-00:16

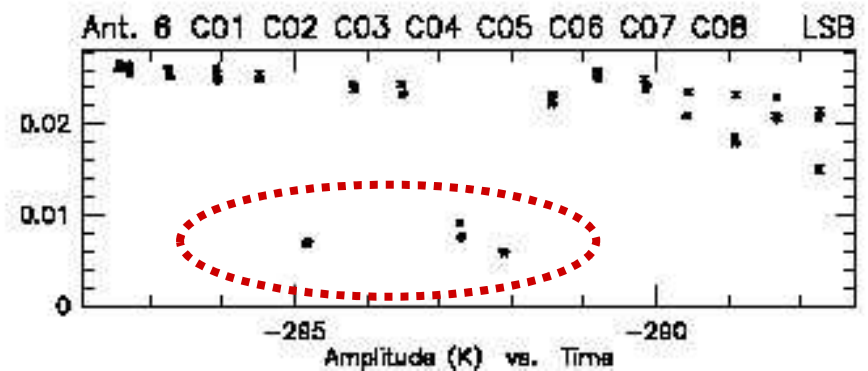
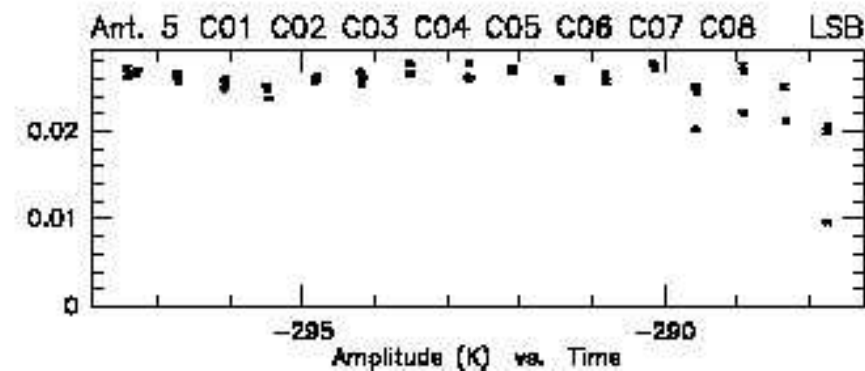
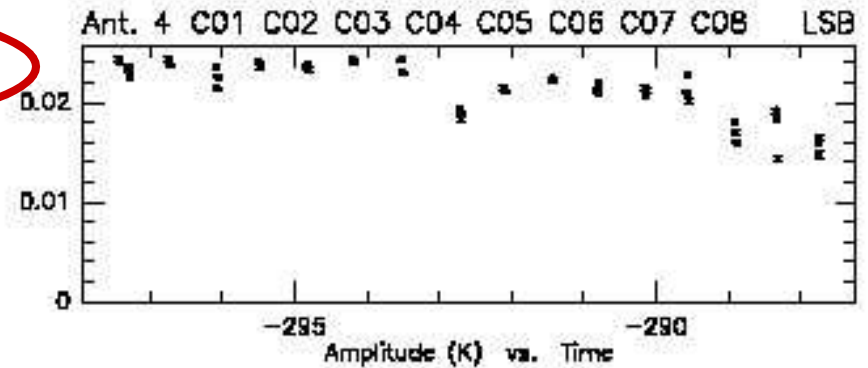
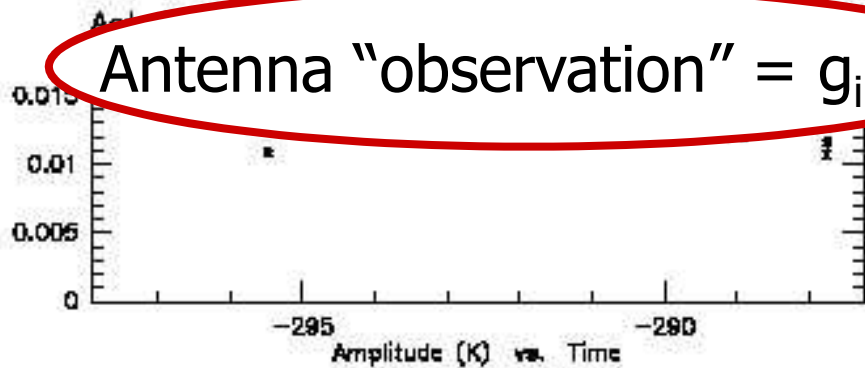
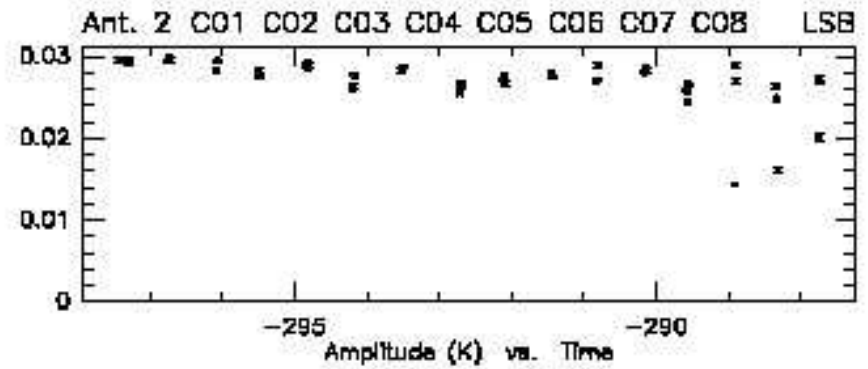
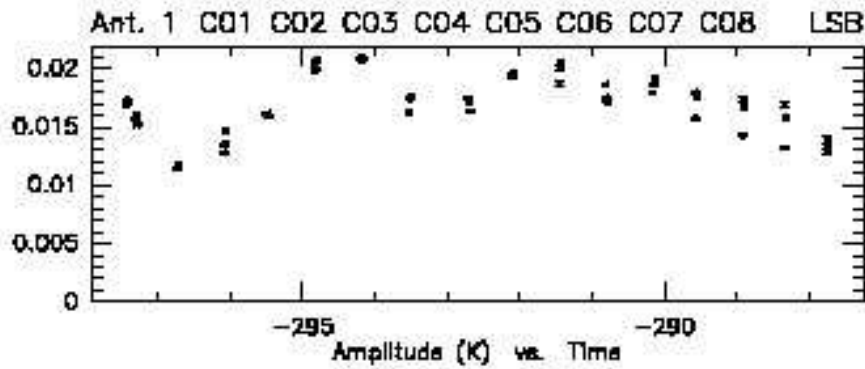
Scan Avg.



RF: Uncal.  
Am: Abs.  
Ph: Abs.

CLIC - 04-OCT-2010 20:57:06 - gueth@dhcp-gueth W27E04E68N46N29E24 6Aq  
TA5F 12CO(2-1 230.538GHz B3 Q3(160,320,320,320)V Q3(160,320,320,320)H  
( 157 7275 P CORR)-(1116 B050 P CORR) 23-JAN-2010 14:33-00:16

Scan Avg.

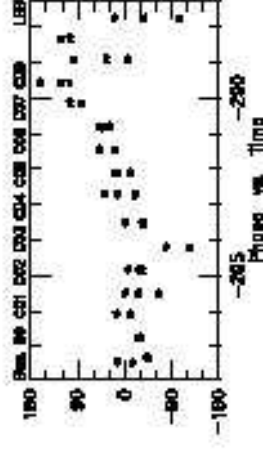
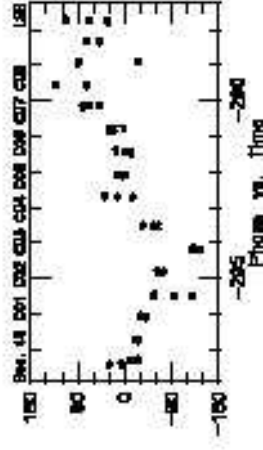
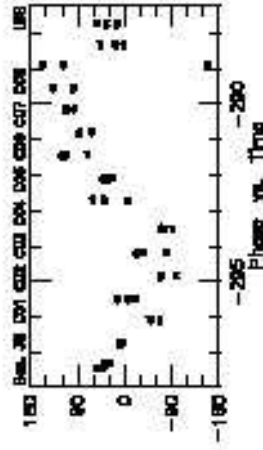
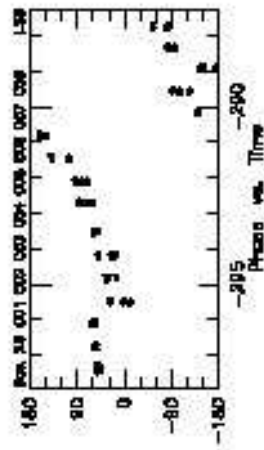
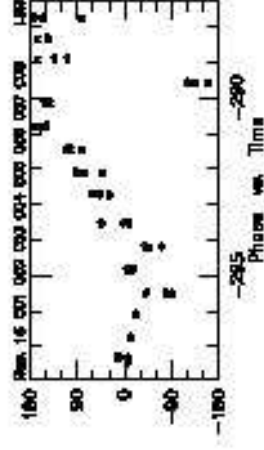
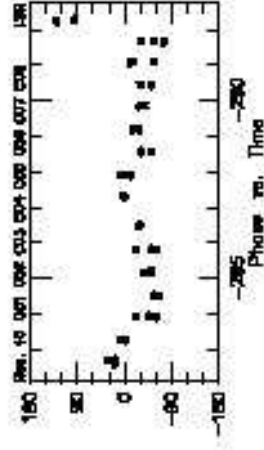
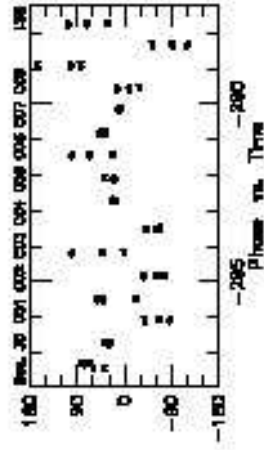
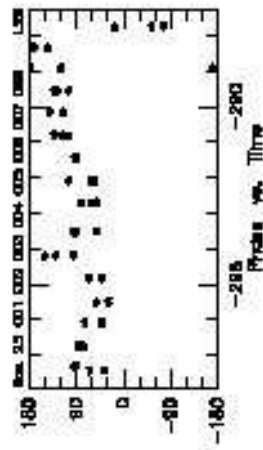
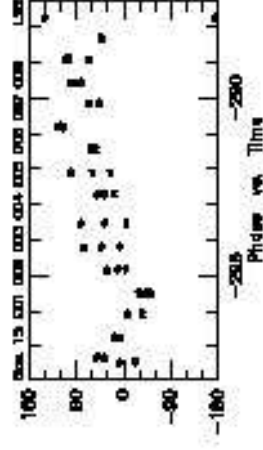
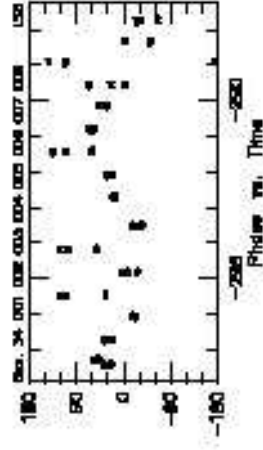
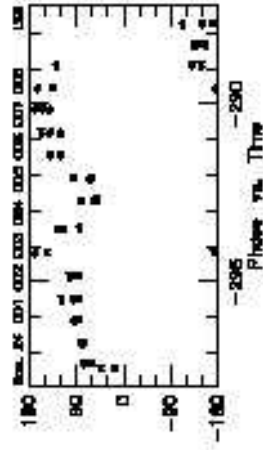
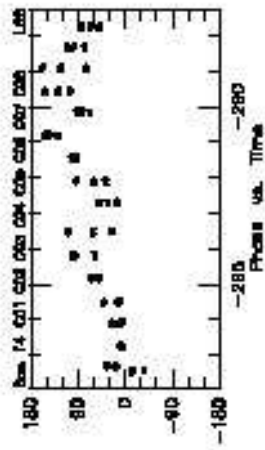
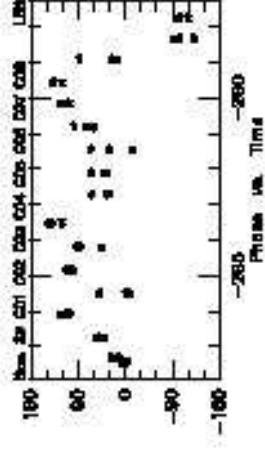
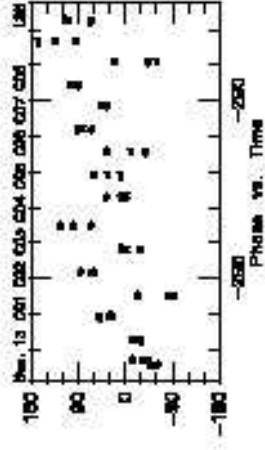
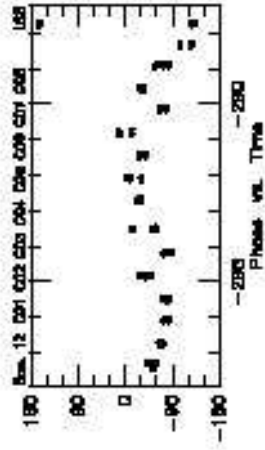


Antenna "observation" =  $g_i \sqrt{S}$

RF: Uncal.  
Am: Abs.  
Ph: Abs.

CLIC - 04-OCT-2010 20:57:35 - gueth@dhcp-gueth W27E04E68N46N29E24 BAq  
TASF 1200(2-1 230.538GHZ B3 Q3(160,320)V Q3(160,320,320,320)H  
( 157 7275 P CORR)-(1116 B050 P CORR) 23-JAN-2010 14:33-00:16

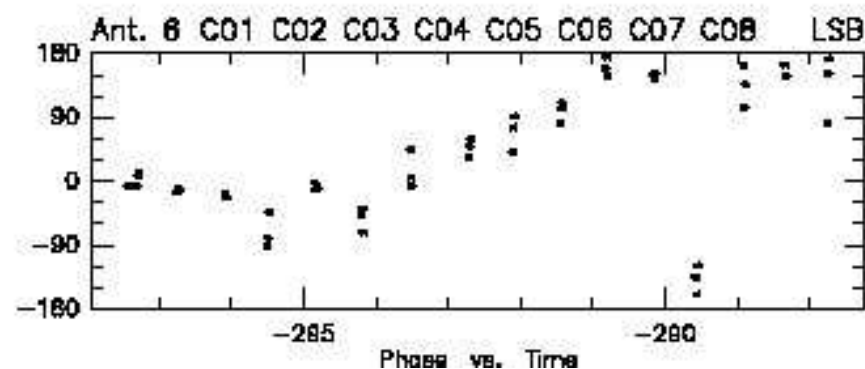
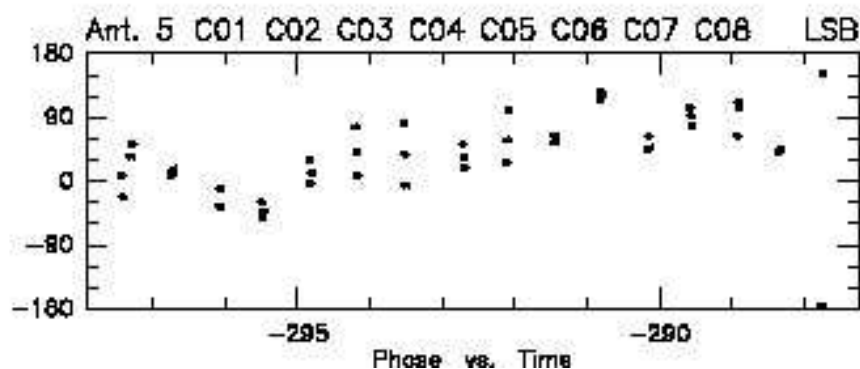
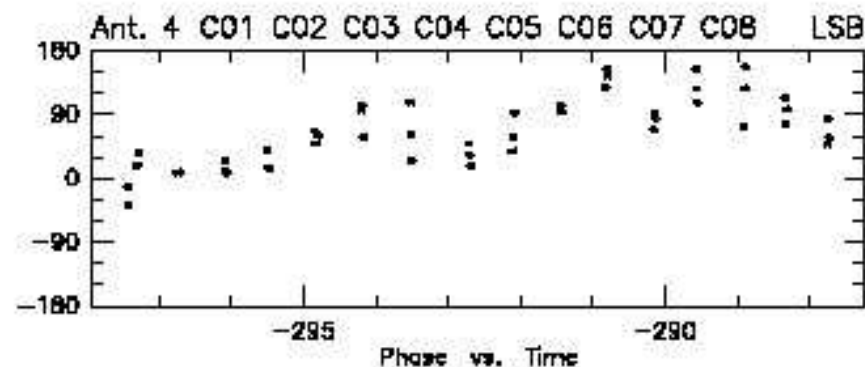
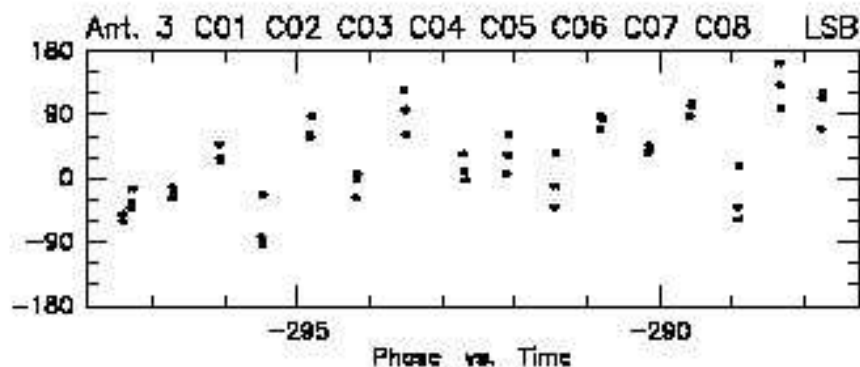
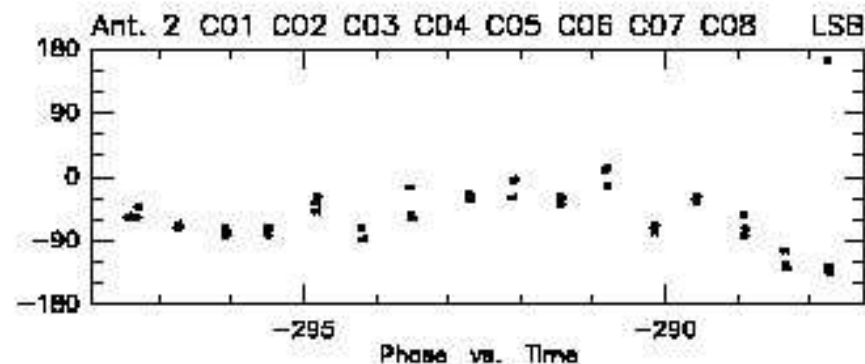
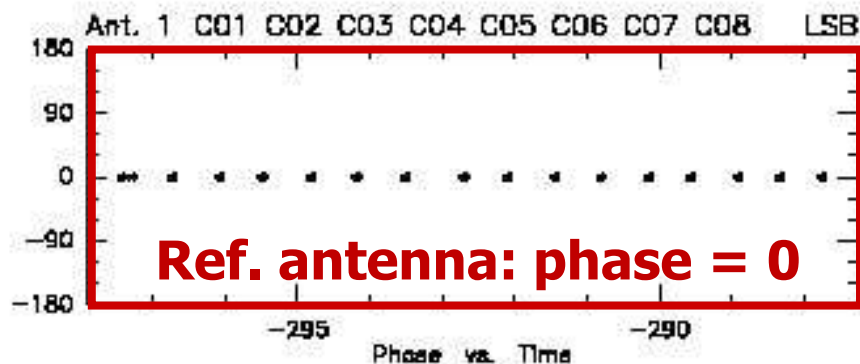
Scan Avg.



RF: Uncal.  
Am: Abs.  
Ph: Abs.

CLIC - 04-OCT-2010 20:57:23 - gueth@dhcp-gueth W27E04E6BN46N29E24 6Aq  
TA5F 12CO(2-1 230.538GHz B3 Q3(160,320,320,320)V Q3(160,320,320,320)H  
( 157 7275 P CORR)-(1116 B050 P CORR) 23-JAN-2010 14:33-00:16

Scan Avg.





# Formalism

## Gain decomposition

Advantages of using the antenna-based gains:

1. most of the effects are **truly antenna-based**  
example: pointing, focus, ...
2. precision to which antenna gains are determined is **improved by a factor  $\sqrt{N}$**  over the precision of the measurement of baseline gains



# Formalism

## Closure relations

- Phase closure relation (point source):
  - Antenna-based decomposition:  $\varphi_{12} = \varphi_2 - \varphi_1$
  - Phase closure:  **$\varphi_{12} + \varphi_{23} + \varphi_{31} = 0$**
- Very useful relation when phases are too unstable to be directly measured (VLBI, optics)
- Similar relations exist for amplitude ratios
- **The decomposition in antenna-based gains implicitly takes into account the closure relations**



# Formalism

## Closure relations

- Phase closure relation (point source):
  - Antenna-based decomposition:  $\varphi_{12} = \varphi_2 - \varphi_1$
  - Phase closure:  $\varphi_{12} + \varphi_{23} + \varphi_{31} = 0$
- **The decomposition in antenna-based gains implicitly takes into account the closure relations**
- Closure not respected if there is a **baseline-based** phase (e.g. decorrelation) → antenna-based calibration not possible in that case



# Data calibration

## Time/Frequency

- **Basic assumption: time- and frequency-variations are decoupled**
- Quite robust:
  - Frequency response mostly due to receivers; stable until retuning
  - Time variations (atmosphere, antennas, ...) mostly achromatic

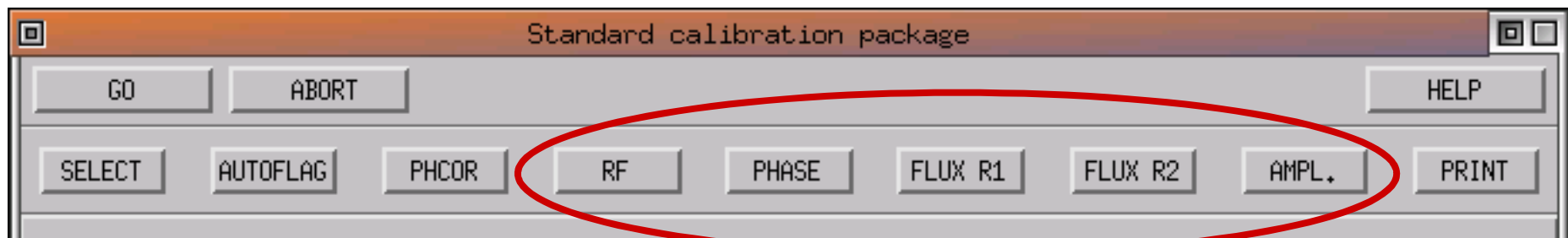




# Data calibration Steps

## Millimeter interferometers

- **Bandpass** (amplitude and phase vs. frequency)
- **Phase** vs. time
- **Flux** scale
- **Amplitude** vs. time





# Bandpass calibration

## The problems

- Frequency dependence of the interferometer response arises from:
  - Receivers intrinsic response
  - Delay offsets (slope on phase)
  - Coaxial cables attenuation
  - Antenna chromatism
  - Atmosphere (O<sub>2</sub>, O<sub>3</sub> lines)
  - ...



# Bandpass calibration Method

- A strong quasar is observed at the beginning of each project
- **Phase should be zero** (point source)  
**Amplitude vs. frequency should be constant** (continuum source)
- Potential problem: spectral index of quasars over large bandwidth

RF: Uncal.

Abs. 26 1361

Ph: 36 1371

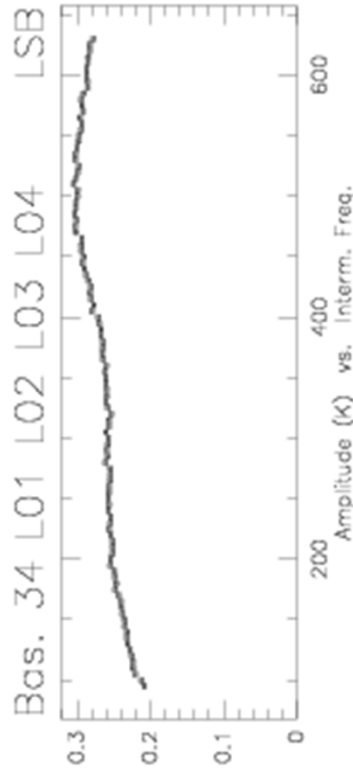
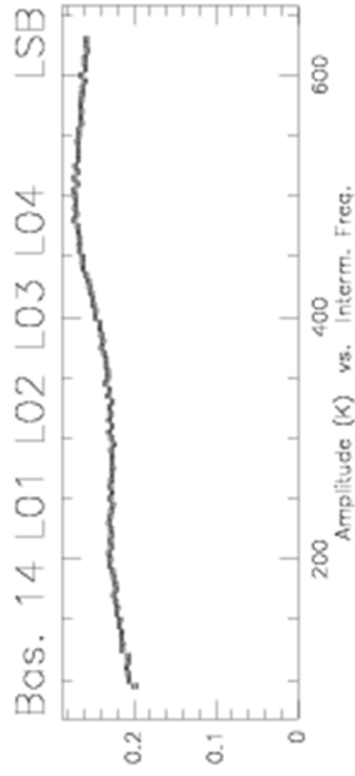
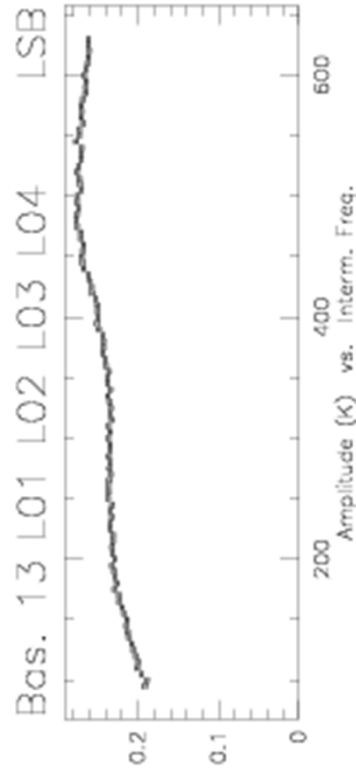
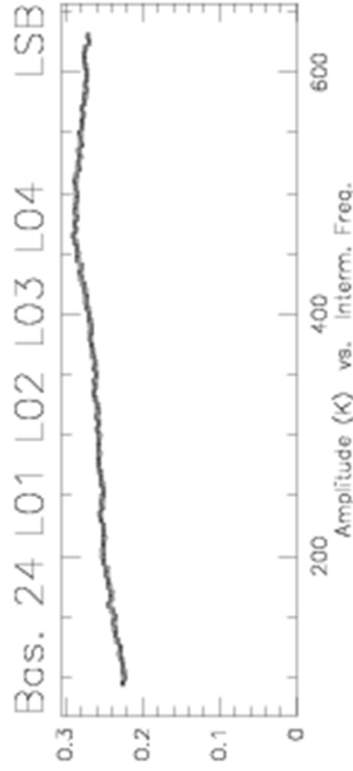
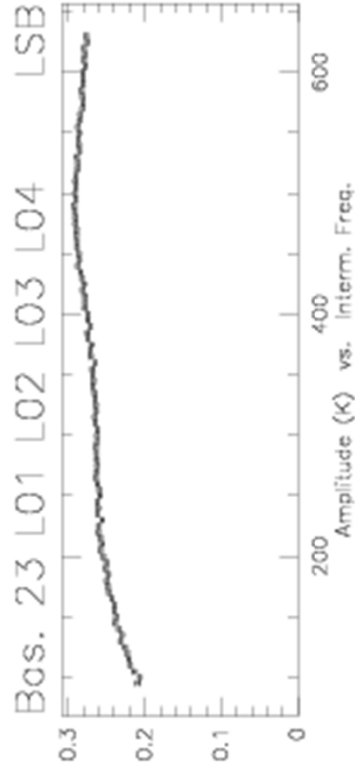
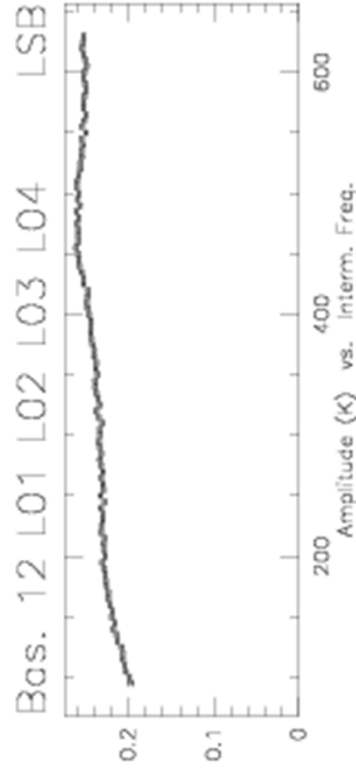
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26 1361 KG5A 3C345 P FLUX 12CO(4-3 5D-N05 01-JUN-2001 23:14 -0.4

36 1371 KG5A 3C345 P CORR 12CO(4-3 5D-N05 01-JUN-2001 23:24 -0.2

Scan Avg-

Vect.Avg-



RF: Uncal.

Am: Abs.

Ph: Rel.(A) Atm.

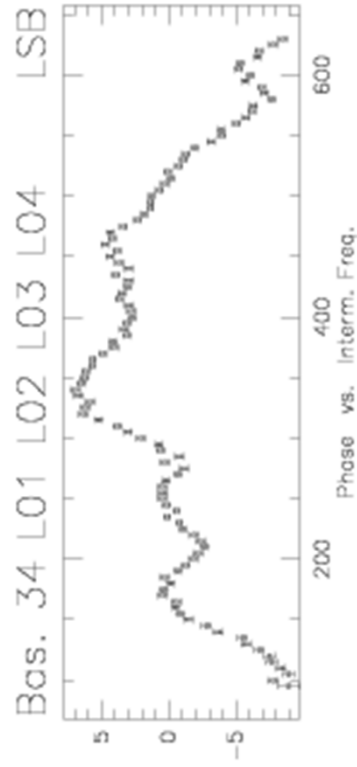
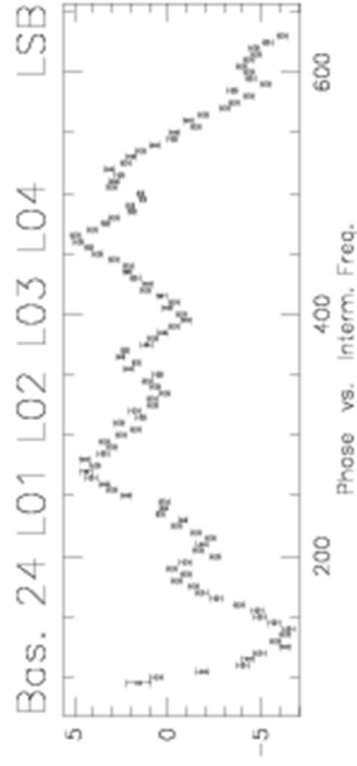
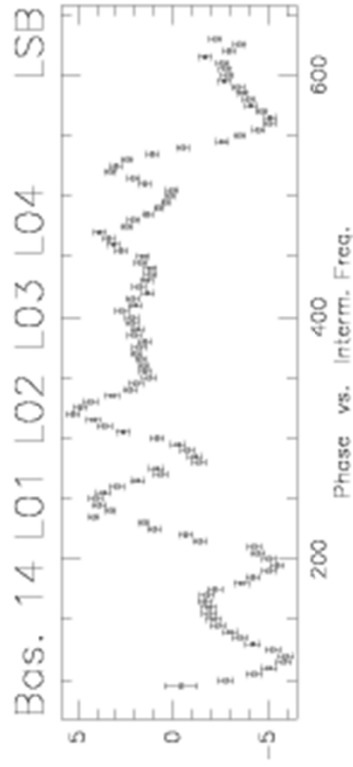
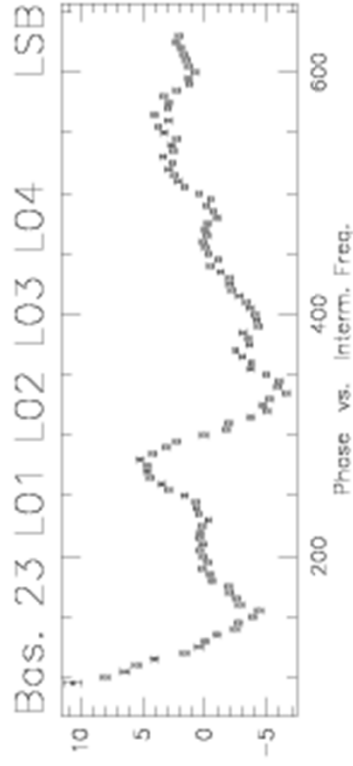
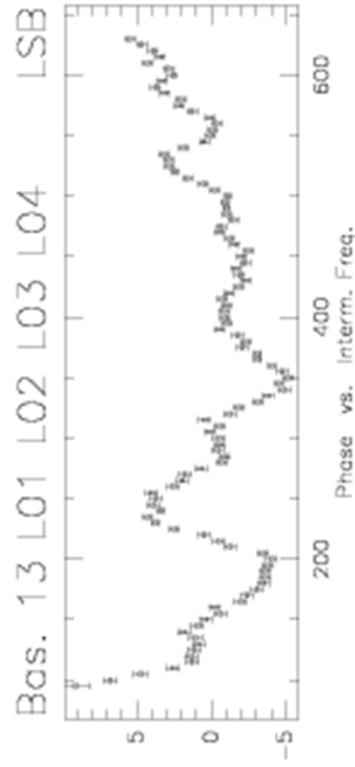
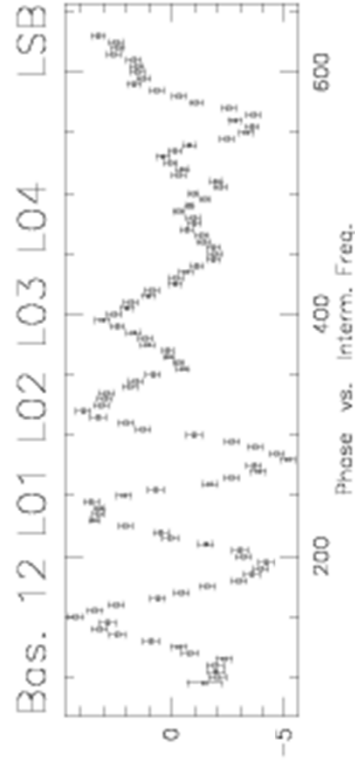
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36 1371 KG5A 3C345 P CORR 12CO(4-3 5D-N05 01-JUN-2001 23:24 -0.2

Scan Avg-

Vect.Avg-





# Bandpass calibration Method

- Time calibration + average (improve the SNR)
- **Solve for antenna-based gains**
- **Fit as a function of frequency** (polynom)
- NB: gains defined such that integral = 1
- Apply the bandpass to all data
  
- Assume bandpass is constant with time
- Must be recalibrated if receivers are retuned



# Bandpass calibration Accuracy

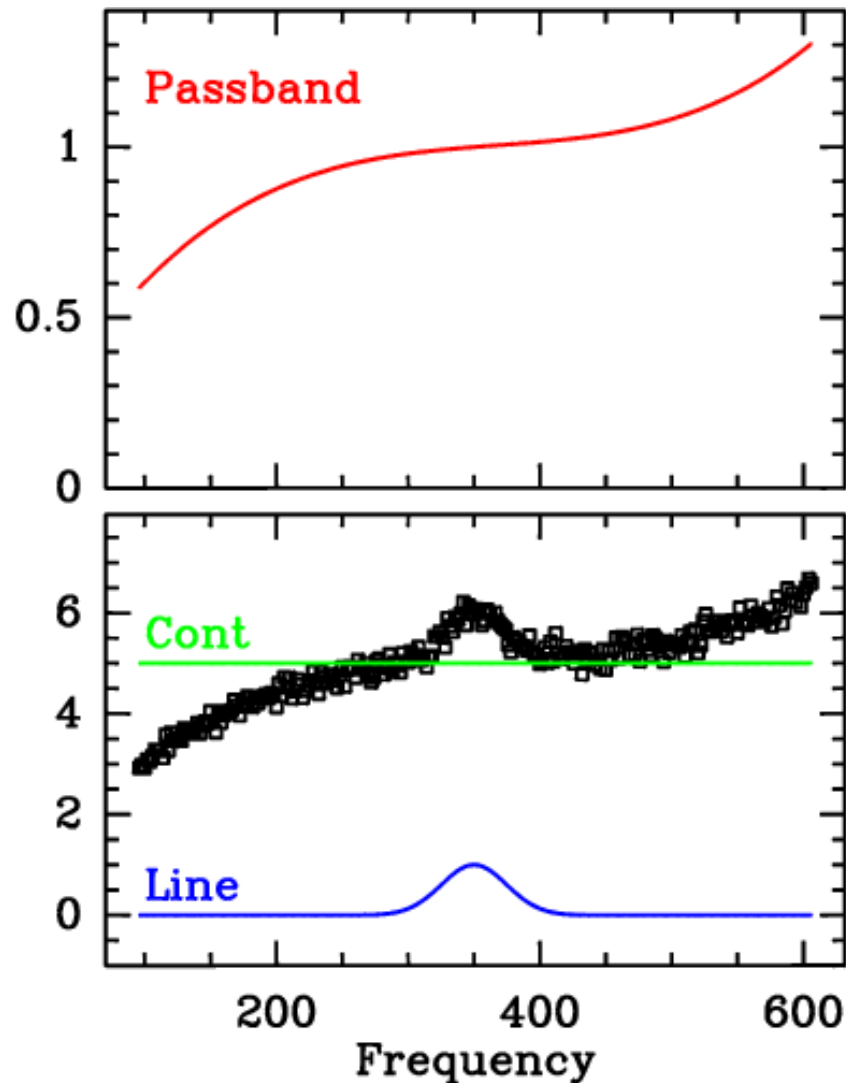
- RF bandpass phase accuracy → uncertainty on relative positions of spectral features
- Rule of thumb:

$$\text{Position error / Beam} = \Delta\Phi / 360$$

- **1" resolution observations,  $\Delta\Phi = 5$  deg, error = 0.015"**



# Bandpass calibration Accuracy



- RF bandpass amplitude accuracy → may be important to detect **weak line on a strong continuum**
- Bandpass curve is a multiplicative factor

$$\Delta T = C / R$$





# Phase calibration

## The problems

- **Short-term time variation** of the phase is caused by the atmosphere
- **Long-term** time variation:
  - Antenna position errors (period 24 h)
  - Atmosphere up to  $\sim 1$ h
  - Antenna/electronics drifts

**Phase calibration critical for final image quality**



# Phase calibration

## Fast component

- Timescale of phase fluctuations: seconds to hours
- Need **real-time correction** of fluctuations during basic integration time ( $< 1$  min) to avoid
  - loss of amplitude = **decorrelation** by  $\exp(-\sigma^2/2)$
  - “**seeing**” (phase  $\leftrightarrow$  position)
- This is conceptually similar to **piston correction** in adaptative optics in optical/IR domain



# Phase calibration

## Fast component

- Predict amount of water from **water line at 22 GHz (NOEMA) or 183 GHz (ALMA)** using dedicated receivers (Water Vapor Radiometers = WVR)
- Measurement → Atmospheric **model** → Water vapor content → Path delay → Atmospheric phase → Real-time correction
- Done **every few second** at NOEMA
- Keep both corrected and not corrected data



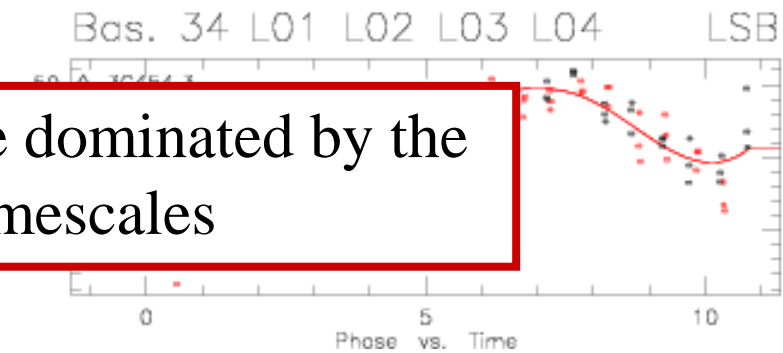
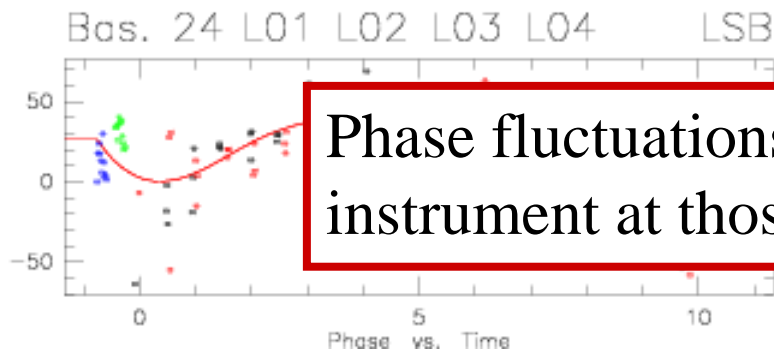
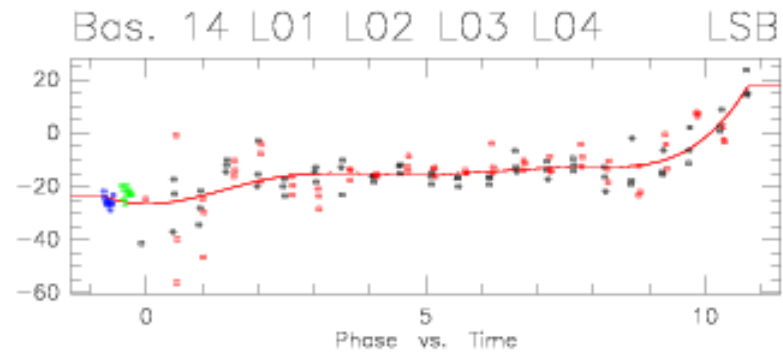
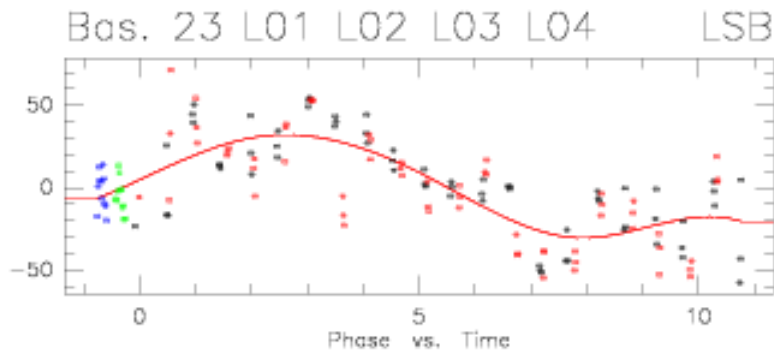
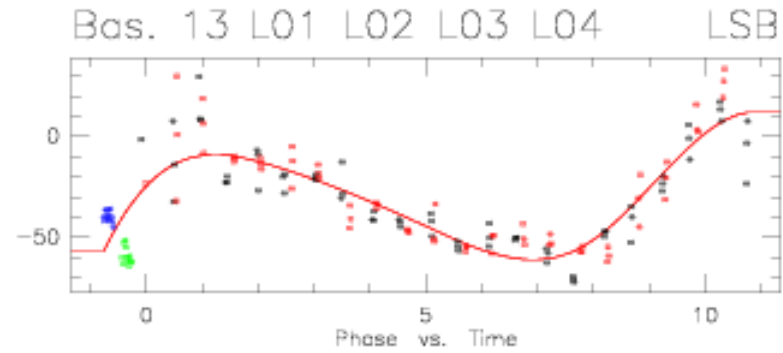
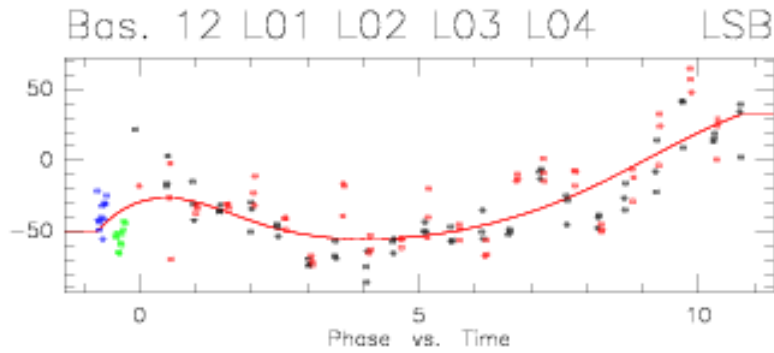
# Phase calibration Method

- Calibration of slow component of phase fluctuation
  - A point source (quasar) is observed every few min
  - **Its phase must be zero**
  - **Solve for antenna-based gains**
  - **Fit as a function of time** (spline)
  - Better: use two calibrators
  - Apply to all data
  - Plot per baseline: measurements + combination of antenna-based fits

RF: Fr.(A)  
Am: Scaled  
Ph: Abs. Atm.

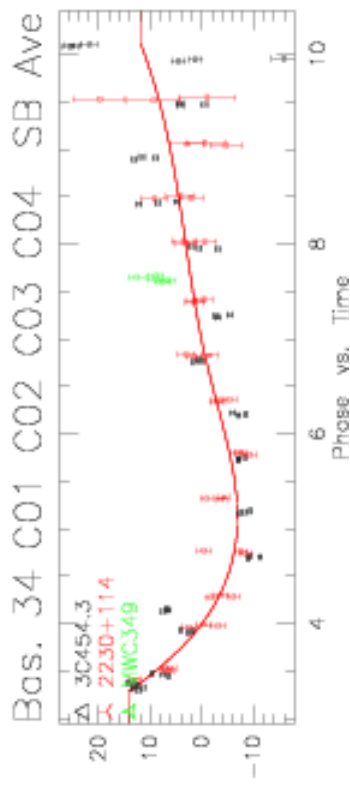
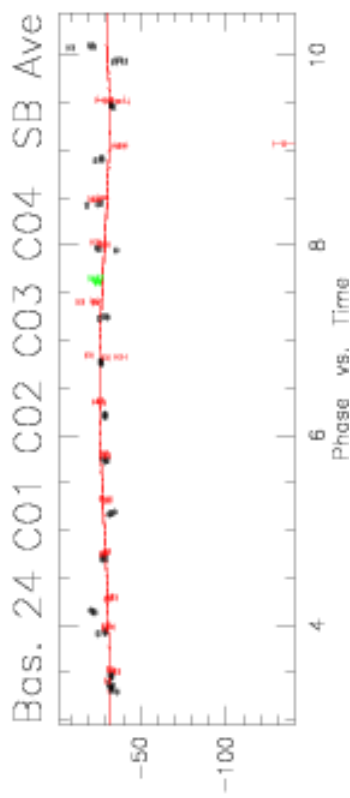
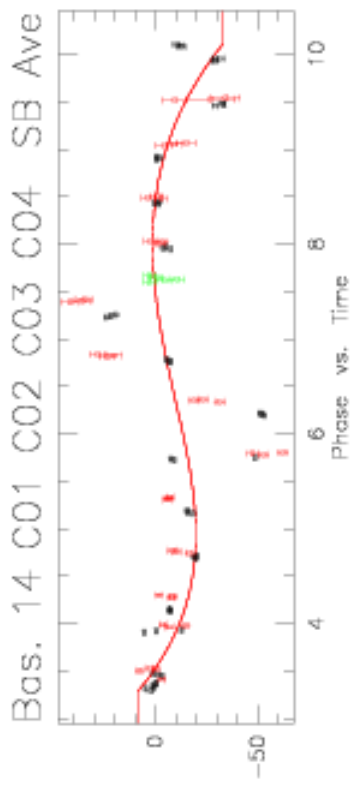
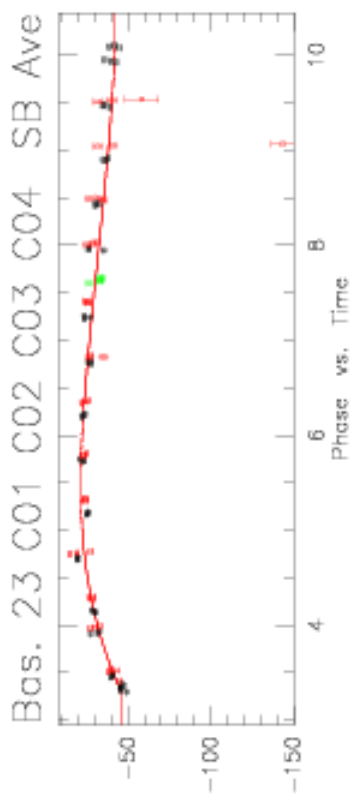
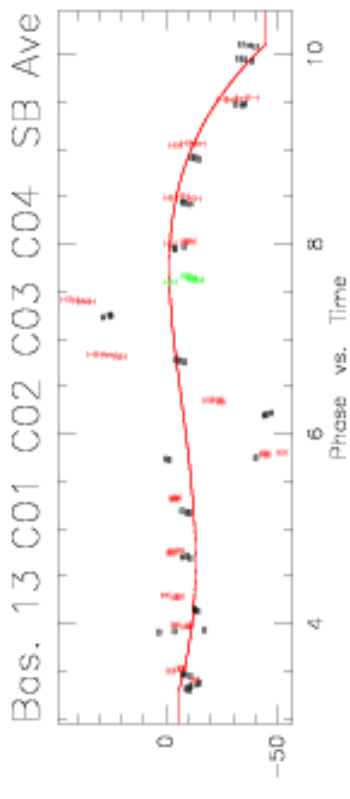
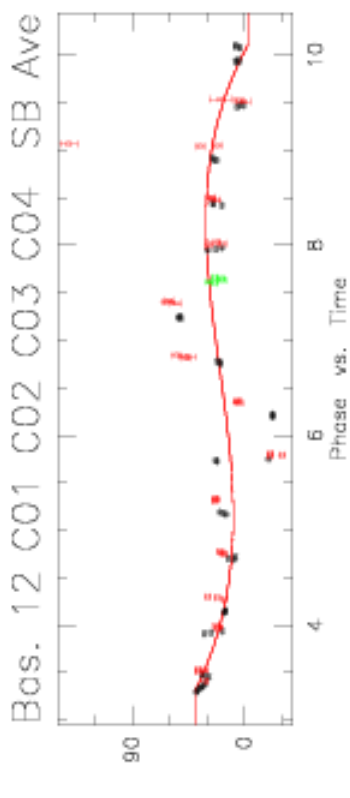
CLIC - 19-NOV-2004 10:37:08 - visitor W00N09W05E03  
26 1361 KG5A 3C345 P FLUX 12CO(4-3 5D-N05 01-JUN-2001 23:14 -0.4  
923 2098 KG5A 3C454.3 P CORR 12CO(4-3 5D-N05 02-JUN-2001 10:45 5.0

Scan Avg.  
Vect.Avg.

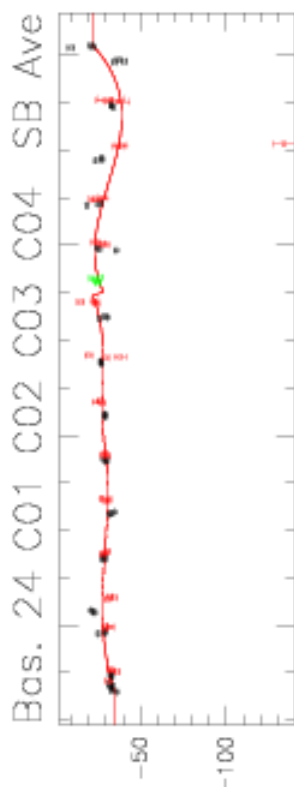
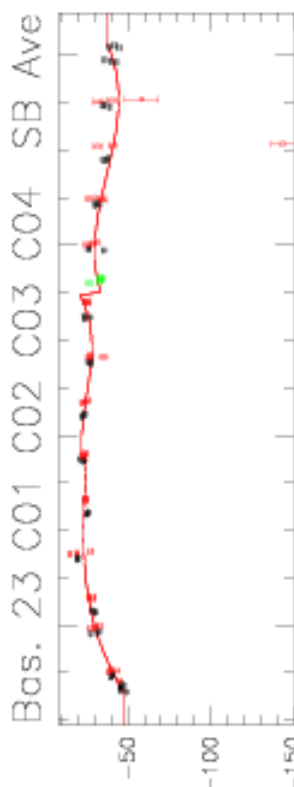
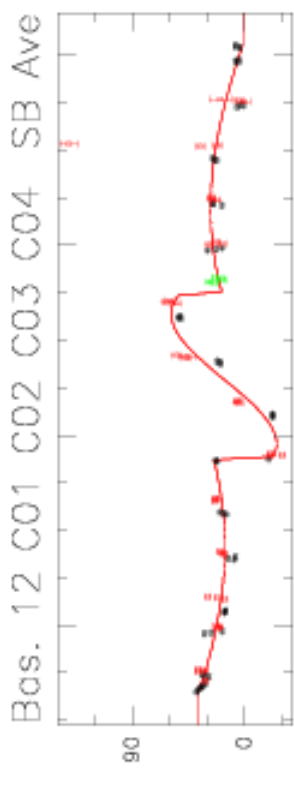
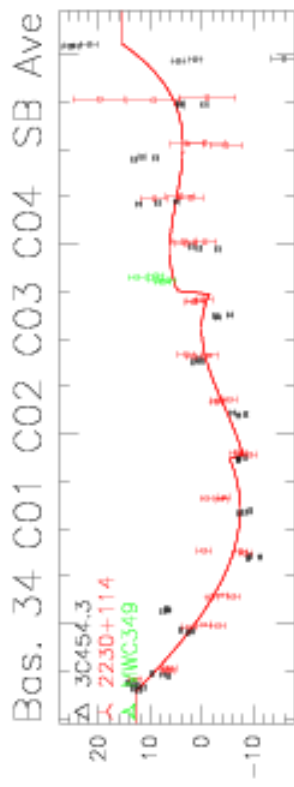
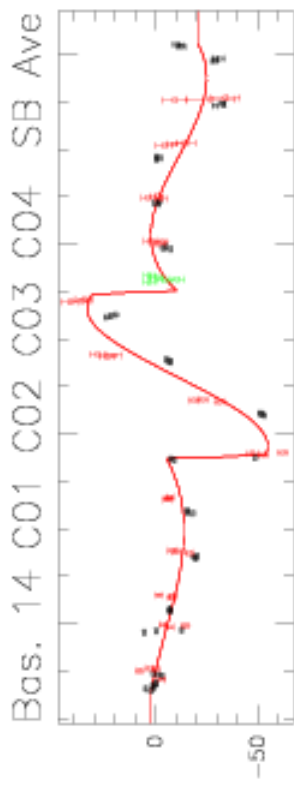
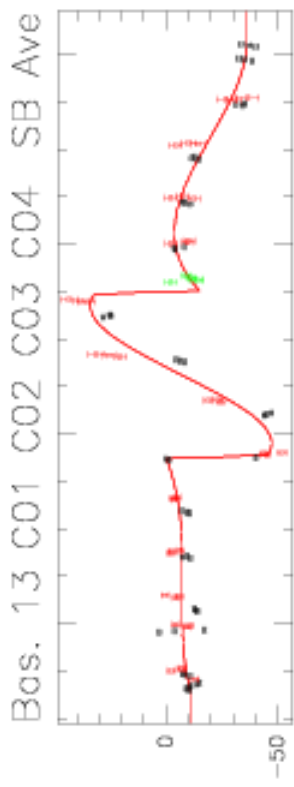


Phase fluctuations are dominated by the instrument at those timescales

RF: Fr.(A) CLIC - 22-NOV-2004 11:24:13 - visitor W00N09W05E03 Scan Avg.  
 Am: 697 5856 L--1 3C454.3 P FLUX 12CO(109 5D-N05 19-JUN-2001 03:17 -1.4 Vect.Avg.  
 Ph: Abs. Atm. Ext.1265 6304 L--1 3C454.3 P CORR 12CO(109 5D-N05 19-JUN-2001 10:06 5.4



RF: Fr.(A) CLIC - 22-NOV-2004 11:24:32 - visitor W00N09W05E03 Scan Avg.  
 Am: 697 5856 L--1 3C454.3 P FLUX 12CO(109 5D-N05 19-JUN-2001 03:17 -1.4 Vect.Avg.  
 Ph: Abs. Atm. Ext.1265 6304 L--1 3C454.3 P CORR 12CO(109 5D-N05 19-JUN-2001 10:06 5.4





# Phase calibration

## Phase transfer

- Atmosphere and most of the instrumental fluctuations **scale with frequency**
- **Phase transfer:**
  1. use low-frequency data (highest SNR) to derive phase curve
  2. scale according to frequency ratio
  3. correct the high frequency data

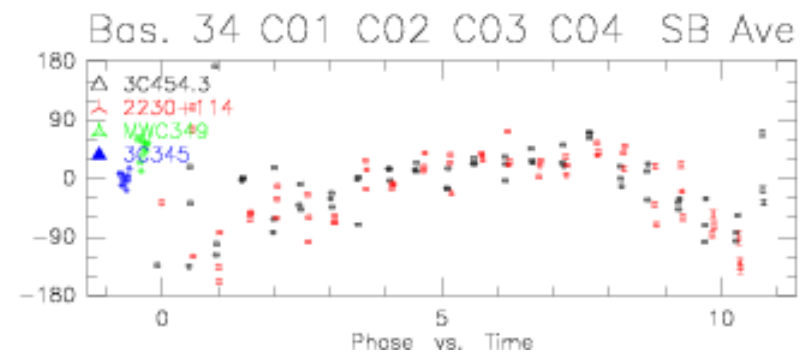
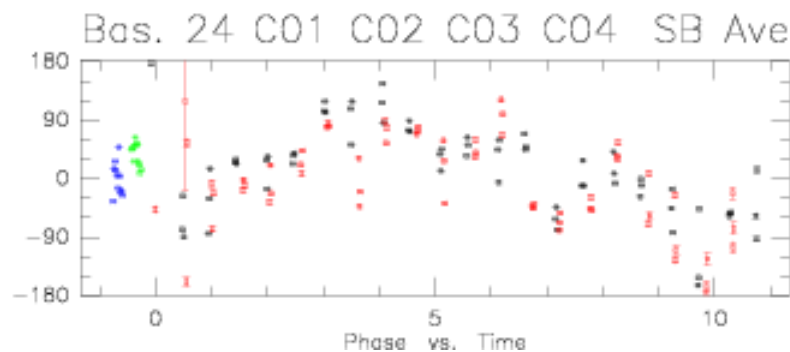
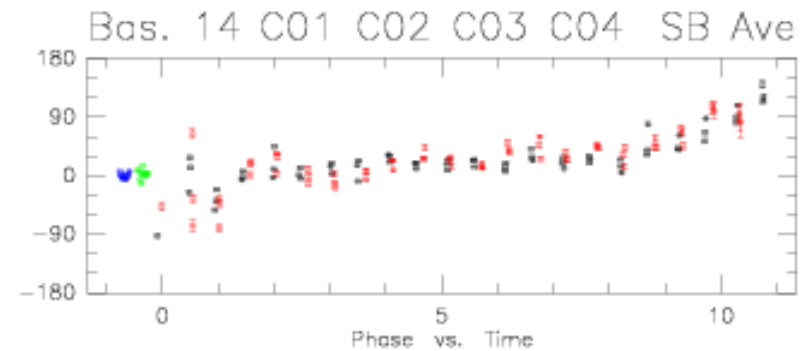
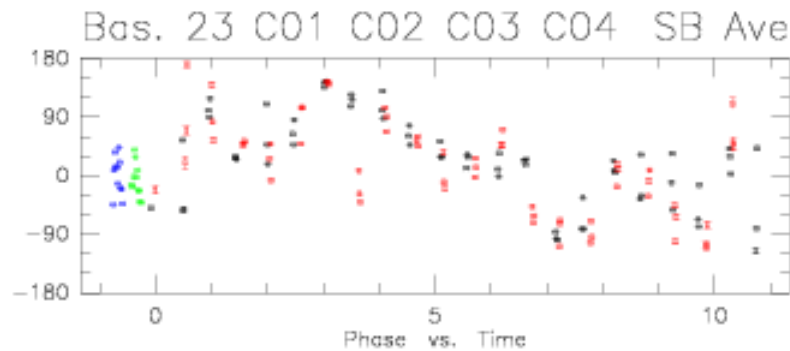
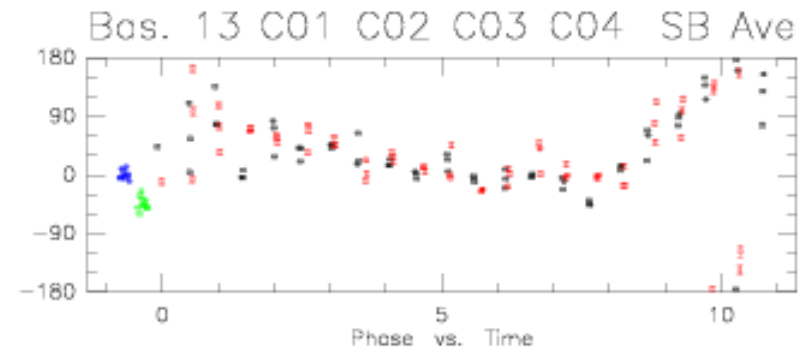
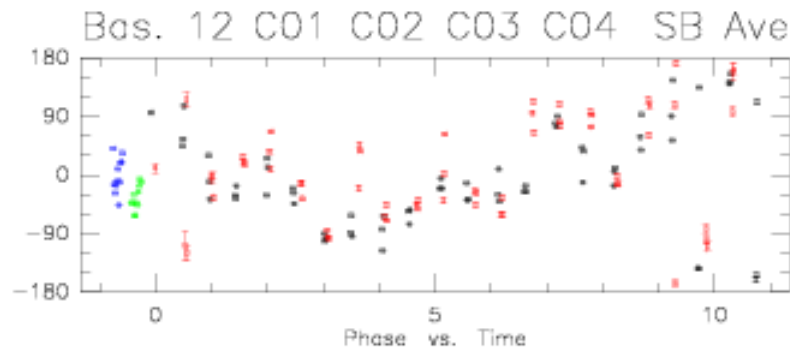


# 230 GHz data, no phase transfer

RF: Fr.(A)  
 Am: Abs.  
 Ph: Abs. Atm.

CLIC - 26-AUG-2005 08:39:55 - gueth W00N09W05E03  
 956 1361 KG5A 3C345 P FLUX CONTINUU 5D-N05 01-JUN-2001 23:14 -0.4  
 1853 2098 KG5A 3C454.3 P CORR CONTINUU 5D-N05 02-JUN-2001 10:45 5.0

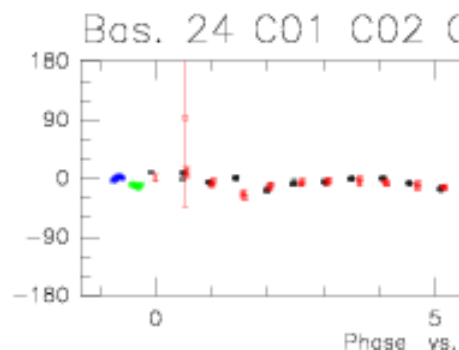
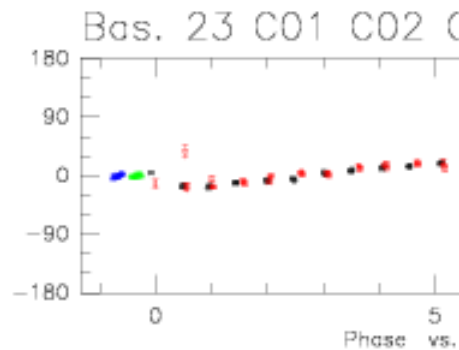
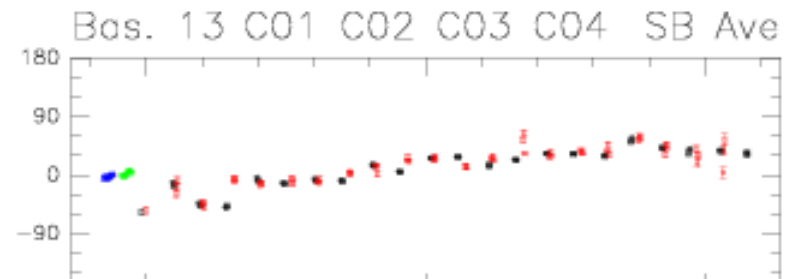
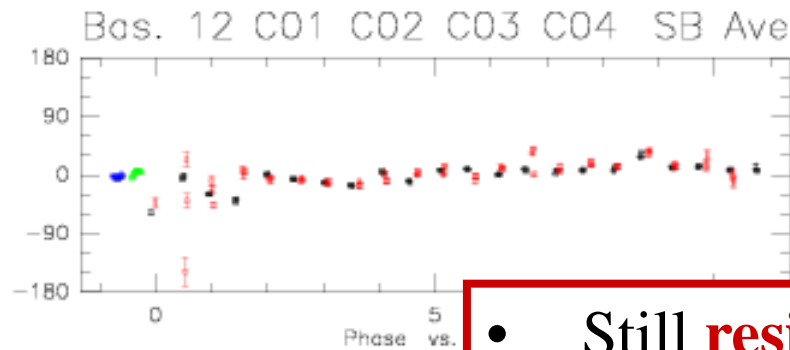
Scan Avg.  
 Vect.Avg.



## 230 GHz, with phase transfer

RF: Fr.(A) CLIC - 26-AUG-2005 08:40:10 - gueth W00N09W05E03  
Am: Abs. 956 1361 KG5A 3C345 P FLUX CONTINUU 5D-N05 01-JUN-2001 23:14 -0.4  
Ph: Abs. Atm. Ext. 1853 2098 KG5A 3C454.3 P CORR CONTINUU 5D-N05 02-JUN-2001 10:45 5.0

Scan Avg.  
Vect.Avg.



- Still **residual phase** – most certainly due to the LO phase drifts, different between the two receivers – need final calibration
- Routinely used with old PdBI receivers. Planned for NOEMA (dual-band observations)
- Planned for ALMA high frequency receiver bands, but more problematic in submm domain (atmosphere)



# Phase calibration Strategies

## Phase calibration strategies:

effect of the noise on calibrators measurements?  
interpolation from calibrators to source?

### **Fits**

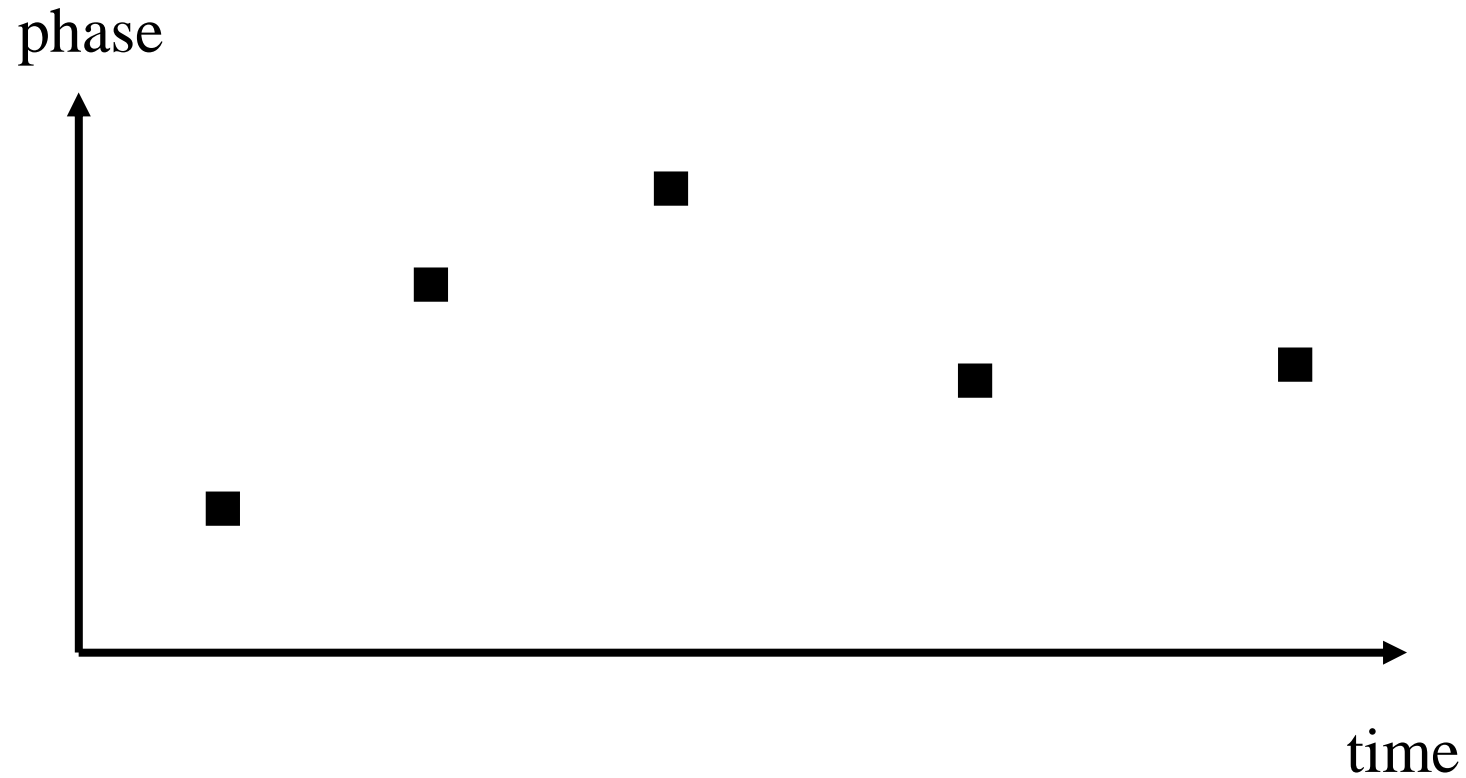
1. Derive antenna phase
2. Fit continuous curve (e.g. spline)
3. Use that curve to correct source data in between calibrators

### **Points**

1. Derive antenna phase
2. Trust it: use that value as calibration
3. Interpolate between the calibrators

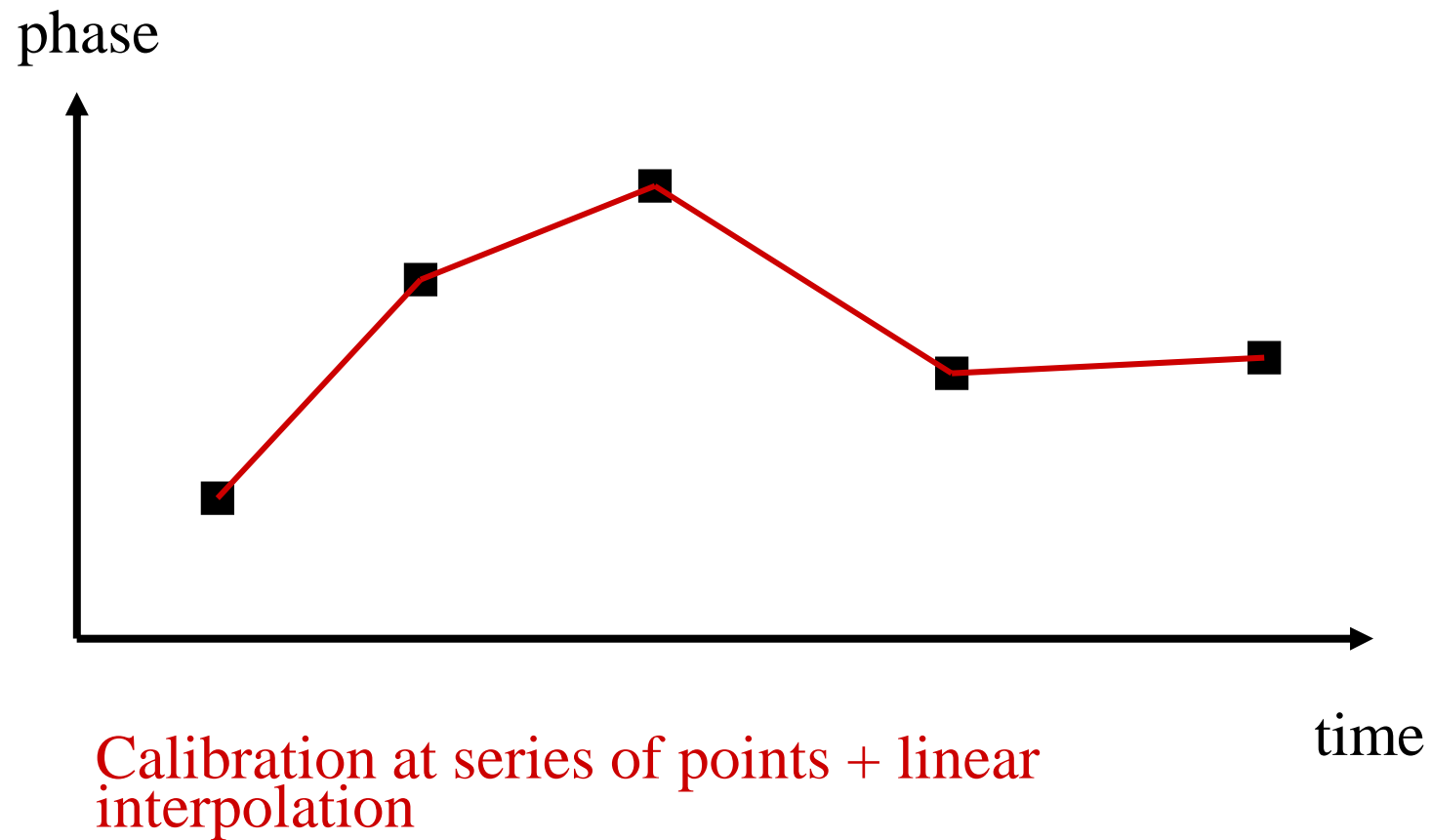


# Phase calibration Strategies



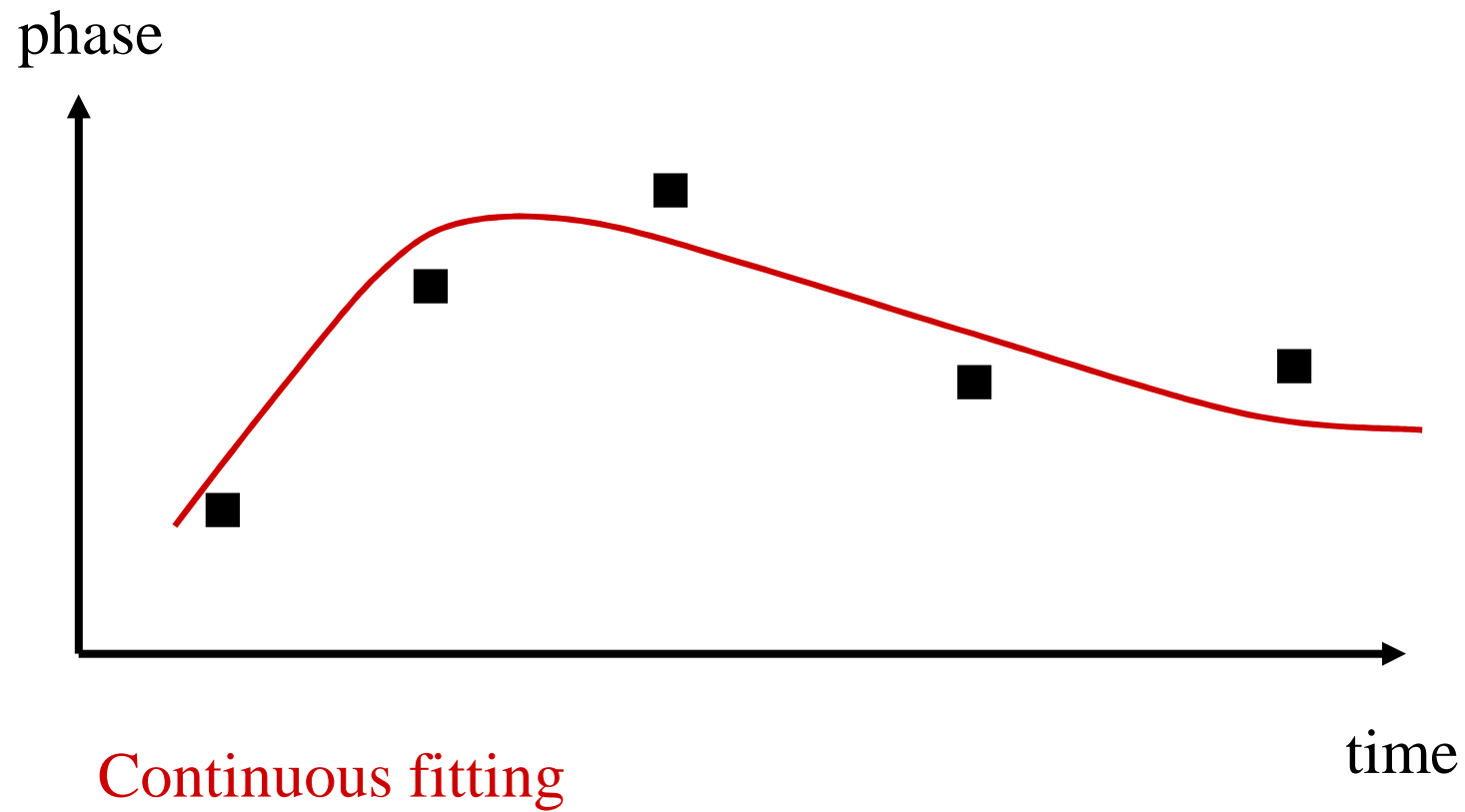


# Phase calibration Strategies



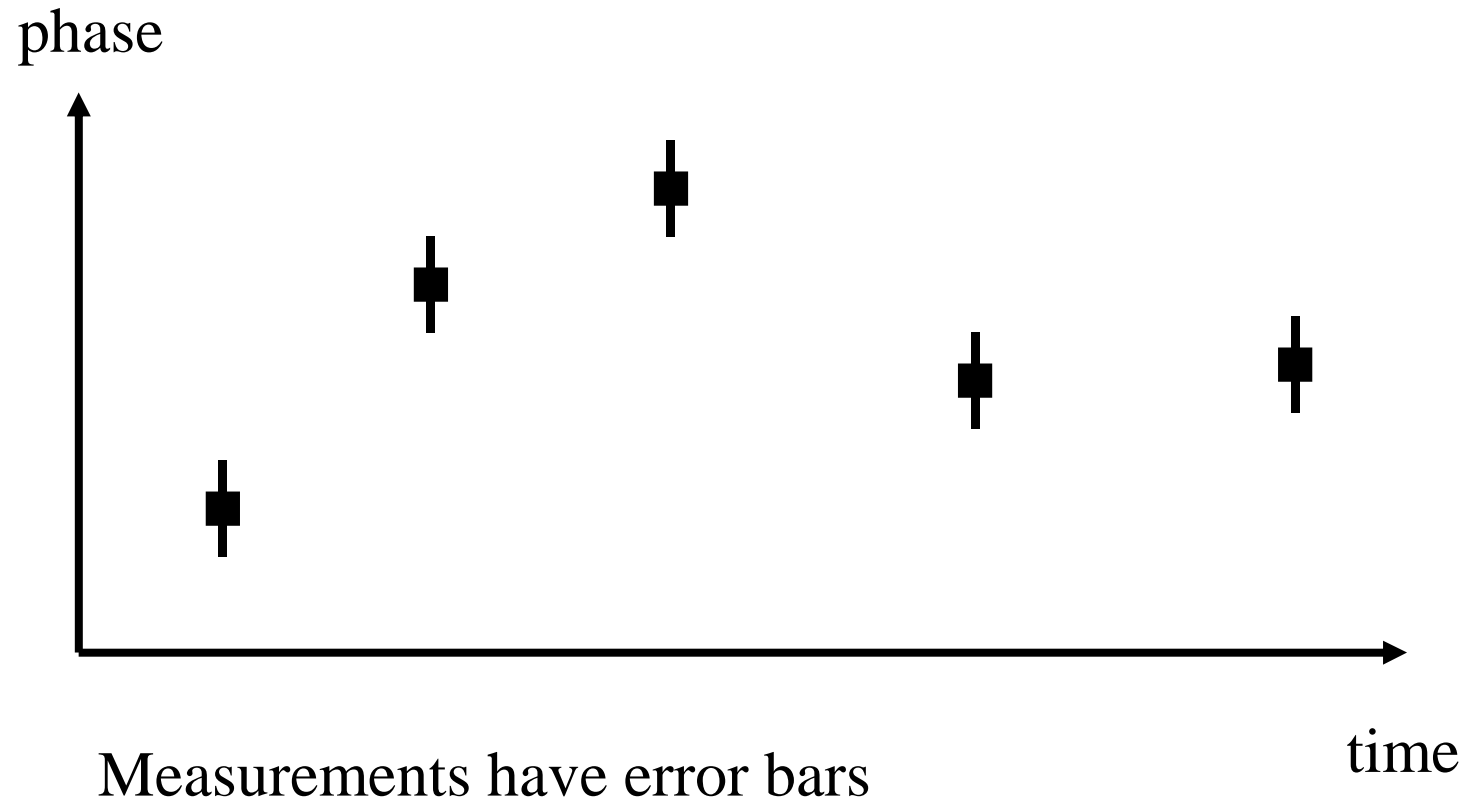


# Phase calibration Strategies



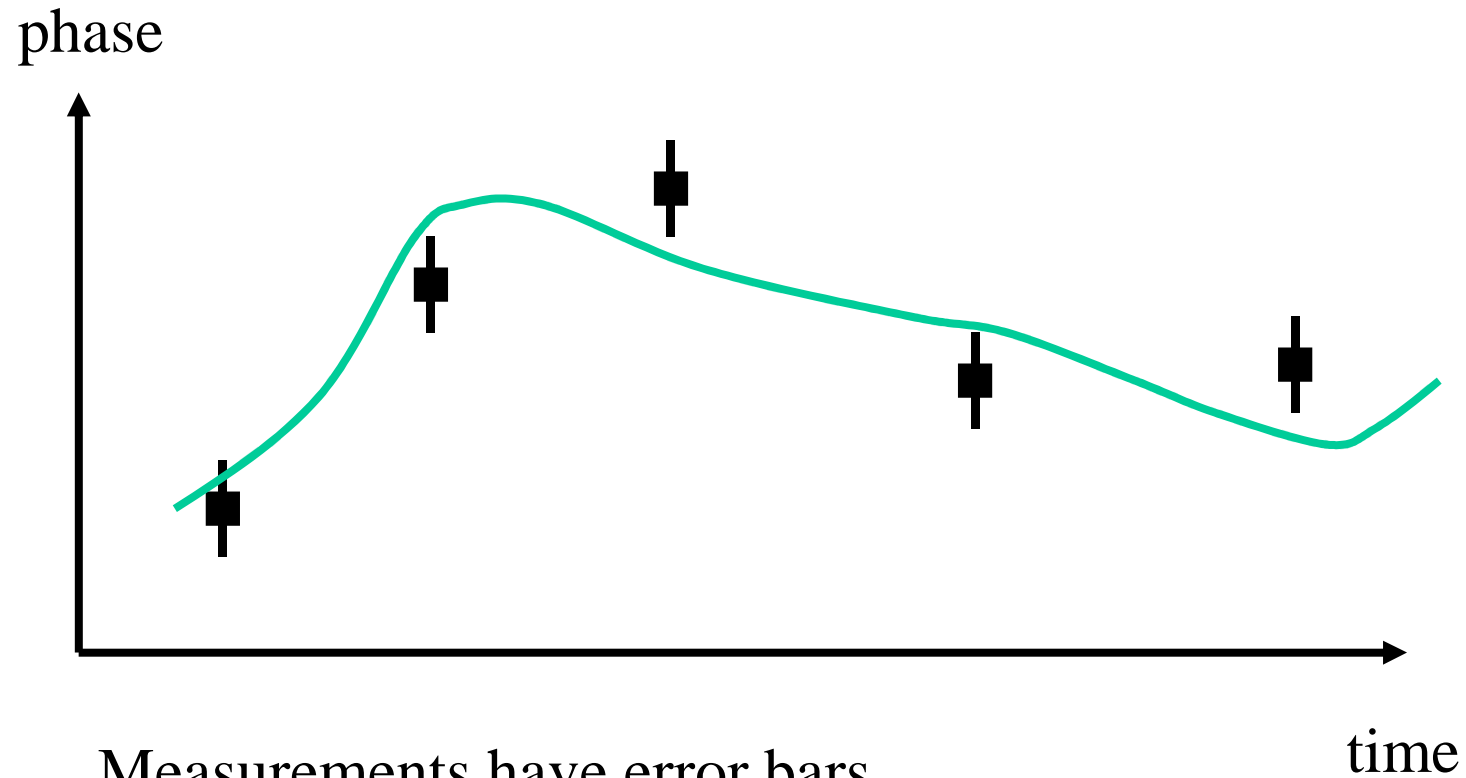


# Phase calibration Strategies





# Phase calibration Strategies



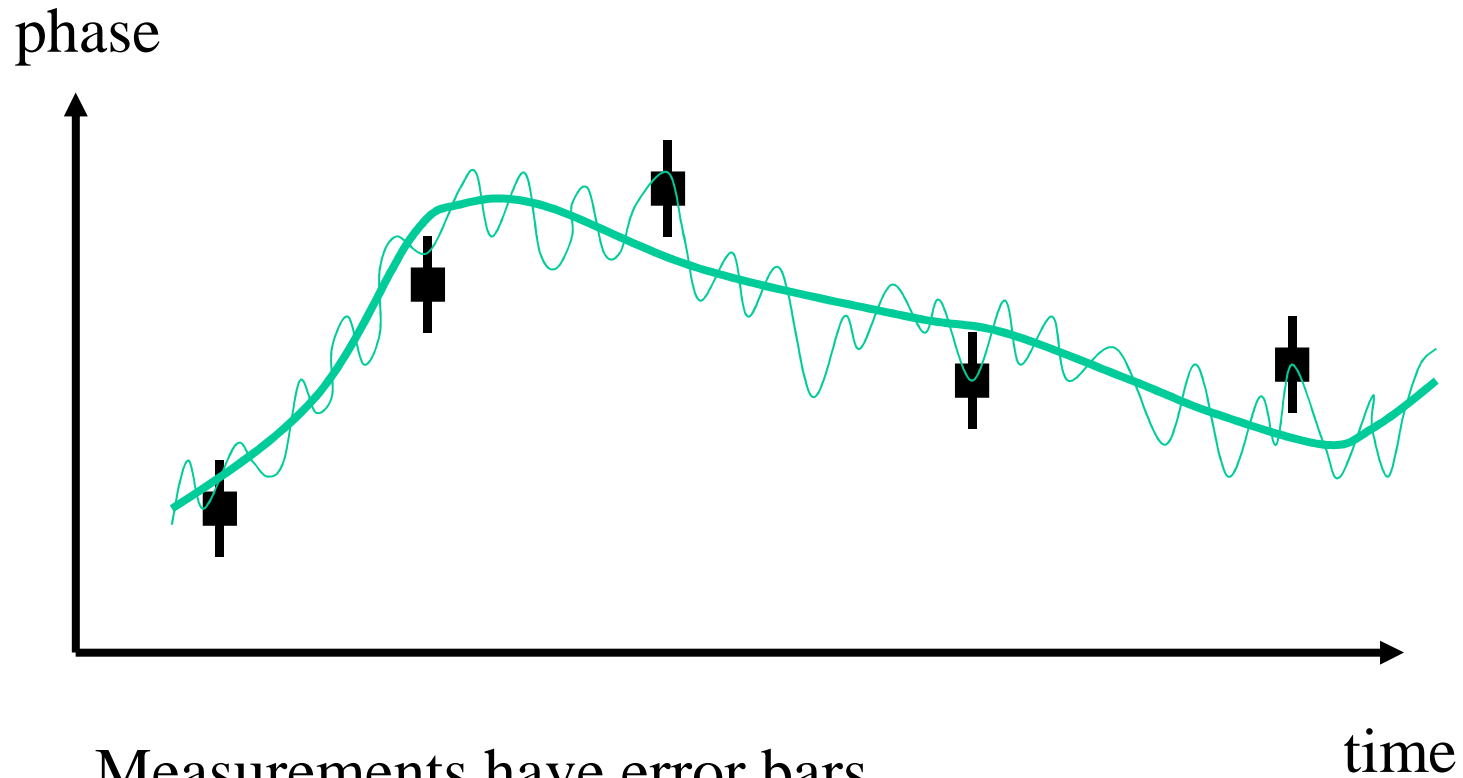
Measurements have error bars

Real phase: slow component





# Phase calibration Strategies

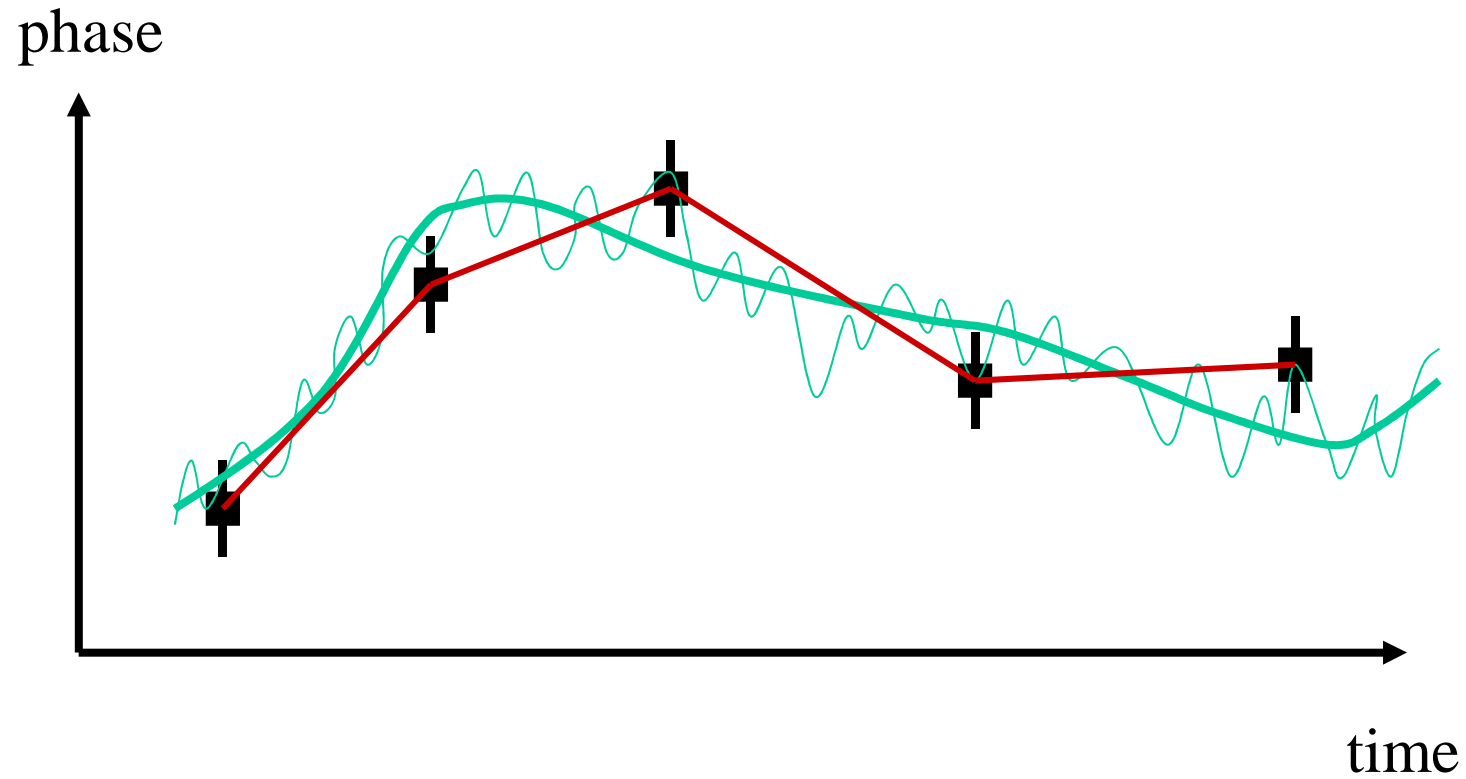


Measurements have error bars

Real phase: slow + fast component

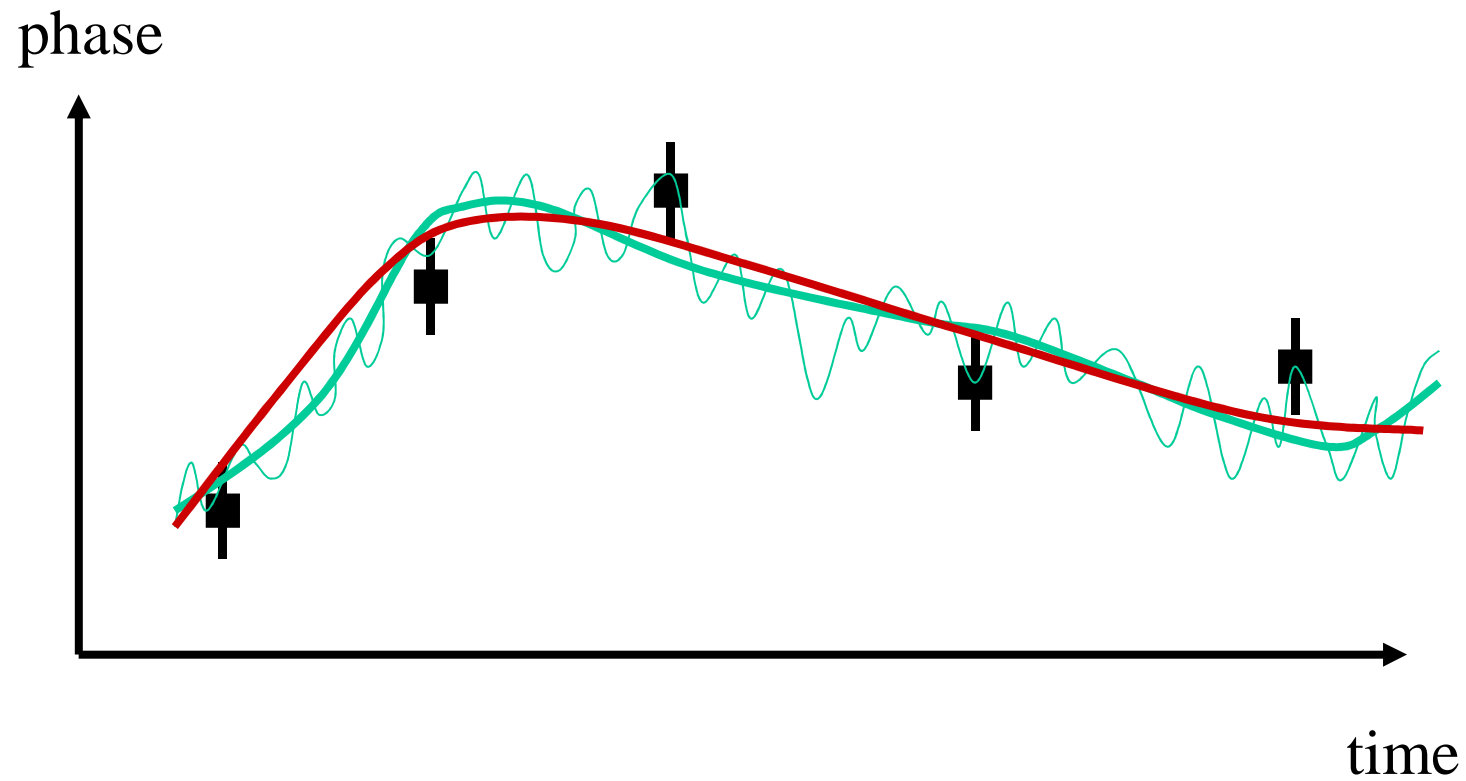


# Phase calibration Strategies



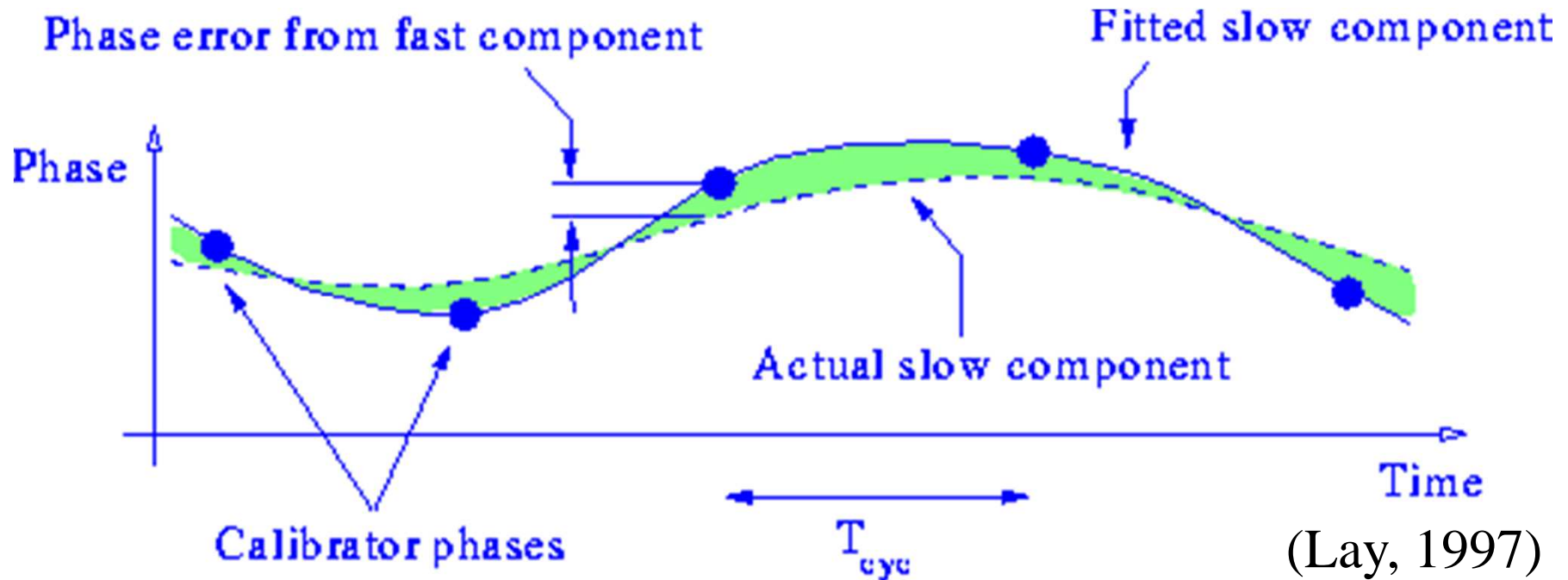


# Phase calibration Strategies





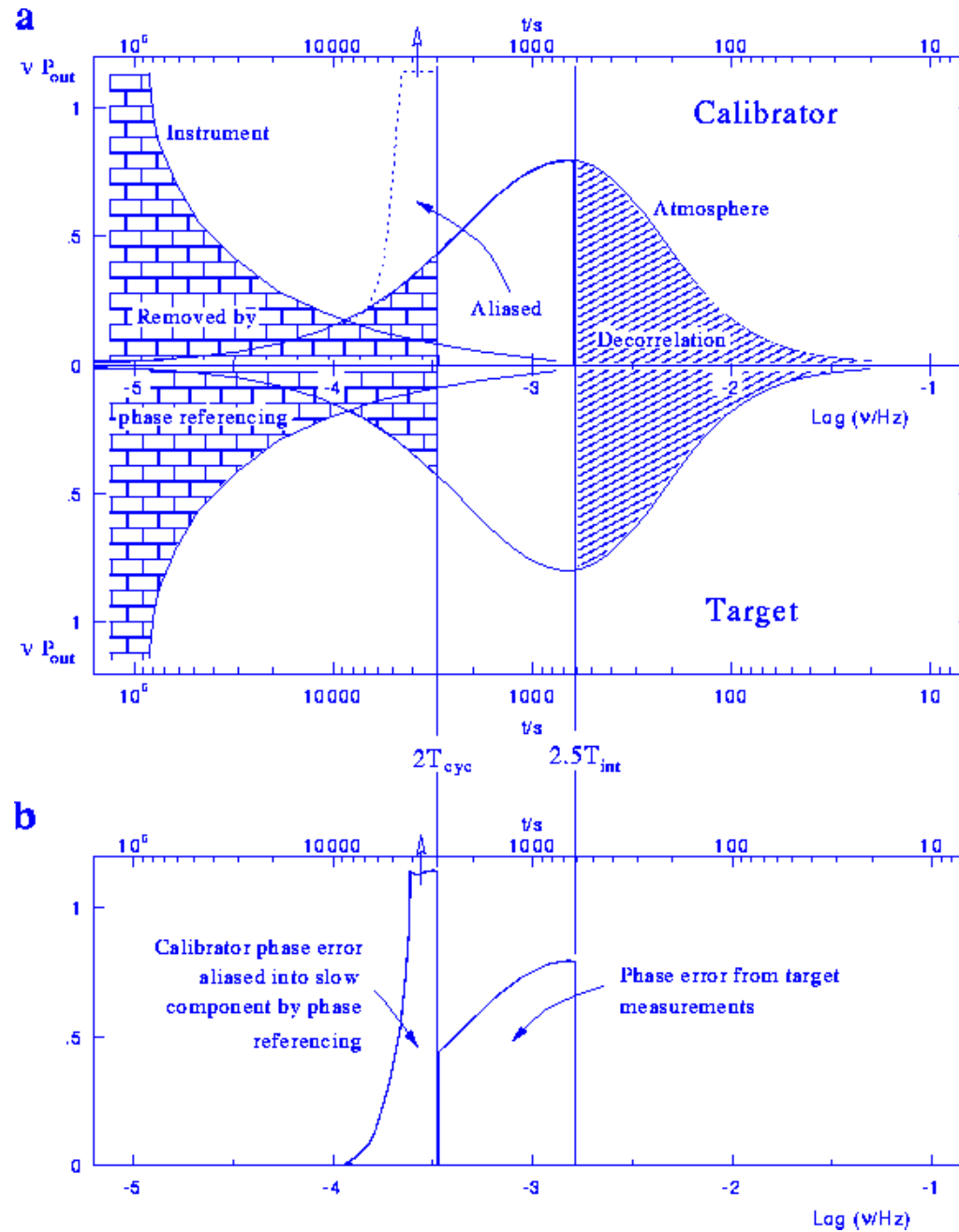
# Phase calibration Strategies



Phase is sampled at intervals  $T_c \rightarrow$  fit is sensitive to errors due to the presence of the fast component ( $< 2T_c$ ), which can be large



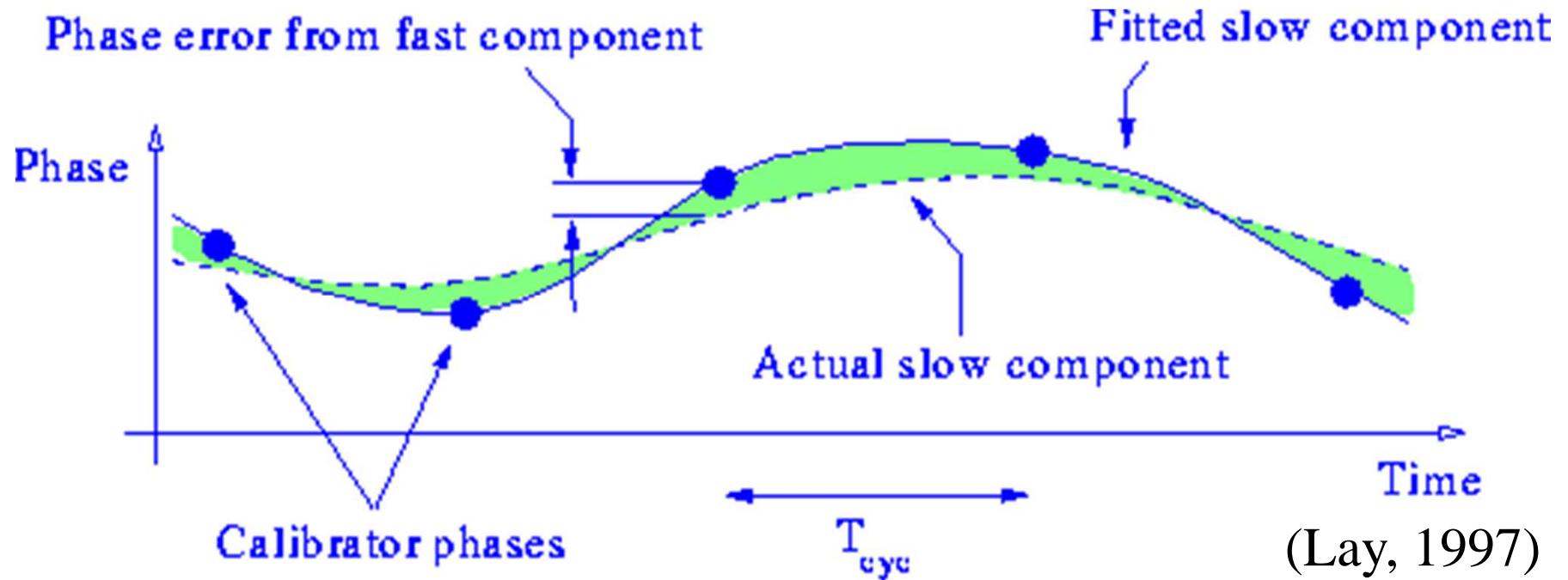
Equivalent to **aliasing** of fast component into slow component



(Lay, 1997)



# Phase calibration Strategies



It is actually recommended to fit a curve that does **not** go through all points



# Phase calibration Strategies

## Phase calibration strategies:

effect of the noise on calibrators measurements?  
interpolation from calibrators to source?

### **Fits**

1. Derive antenna phase
2. Fit continuous curve (e.g. spline)
3. Use that curve to correct source data in between calibrators

### **Points**

1. Derive antenna phase
2. Trust it: use that value as calibration
3. Interpolate between the calibrators



# Phase calibration Strategies

## Phase calibration strategies:

effect of the noise on calibrators measurements?  
interpolation from calibrators to source?

### **Fits**

**Limited SNR & phase noise**

1. Derive antenna phase
2. Fit continuous curve (e.g. spline)
3. Use that curve to correct source data in between calibrators

### **Points**

**OK if excellent SNR & no  
atmospheric phase noise**

1. Derive antenna phase
2. Trust it: use that value as calibration
3. Interpolate between the calibrators





# Phase calibration

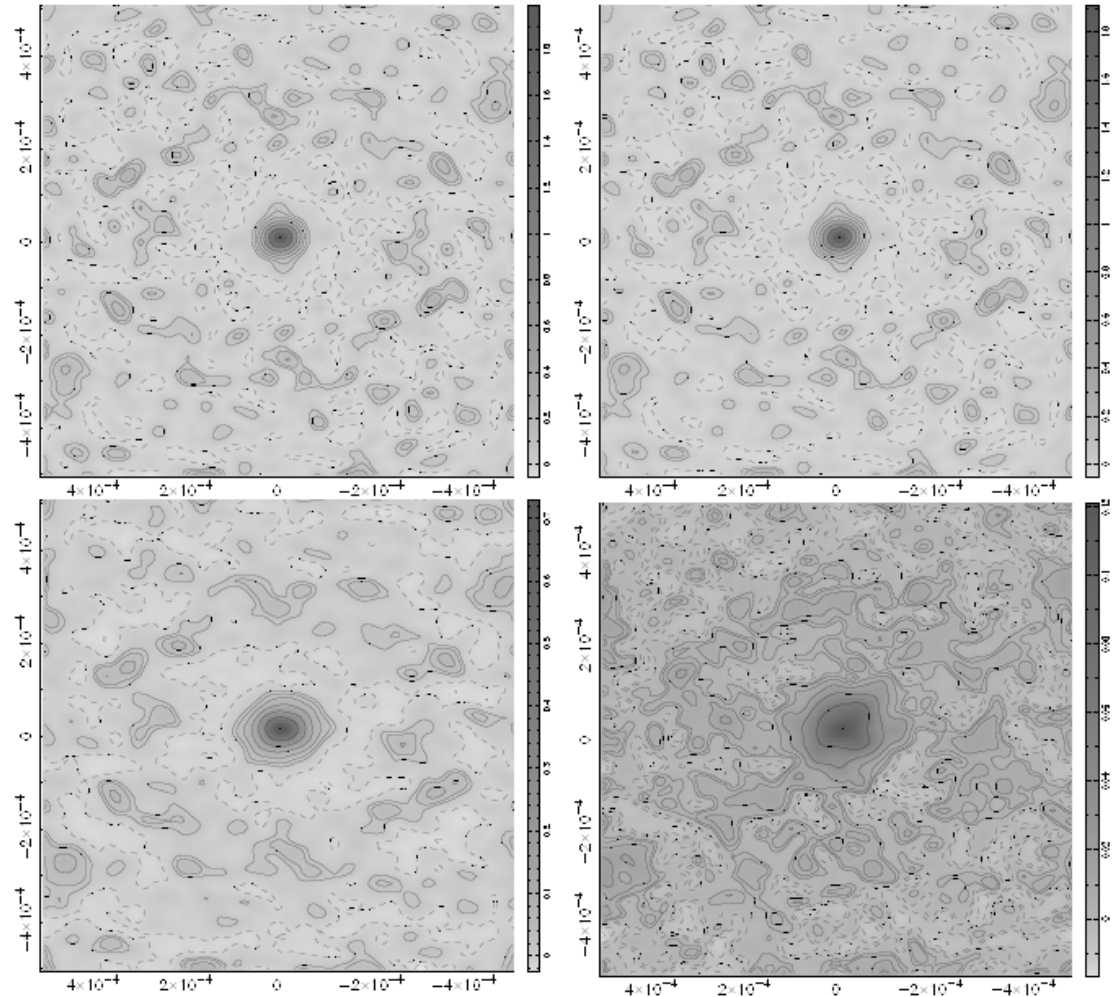
## Radio seeing

- Phase fluctuations timescales:
  - < 1 min      real-time (WVR) phase correction
  - 1 min – 20min      → **not corrected**
  - >20 min      off-line phase calibration
- Can be estimated by rms of phase calibration fit
- Translate into a **radio seeing**  $\sim$  phase rms / baseline
- Can be a fraction of the beam → larger effective beam...



# Seeing

Simulations:  
increasing the phase  
noise 3:10:50:100  
(Nikolic et al. 2008)





# Phase calibration

## Fast switching

- **Reduce the switching time** calibrator-source down to 10 seconds
- Advantages: Remove a larger part of the atmospheric fluctuations spectrum. Perfect complement to the WVR corrections (second timescale)
- Drawbacks: Observing efficiency is decreased. Puts very strong constraints on the antennas and acquisition system.
- Planned for ALMA?



# Phase calibration

## Auto-calibration

- Simple case where the field **contains a strong point source**
- Can be used to calibrate out almost all phase fluctuations at periods  $>$  integration time (30 sec)
- Excellent results but for **very specific projects**
  - Absorption lines in quasars
  - Stars with strong maser lines



# Phase calibration

## Self-calibration

- **Extended (but simple) bright source?**
  1. Classical calibration with calibrators
  2. Source imaging & deconvolution
  3. Predicted visibilities ("model")
  4. Divide observed source visibilities by model
  5. Calibrate remaining variations
  6. Go to 2
- Can work because  $N_{\text{ant}} < N_{\text{baseline}}$
- Requires enough SNR on source in each individual integration

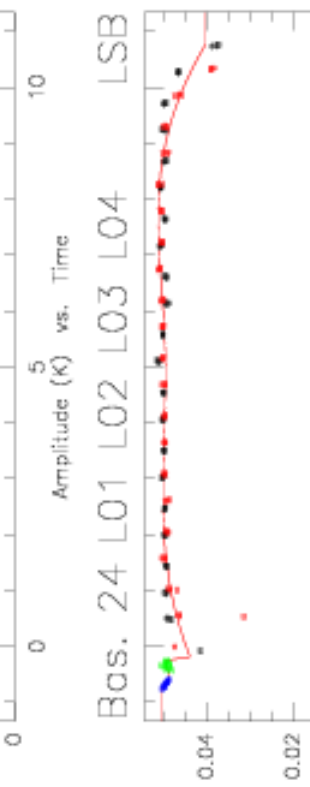
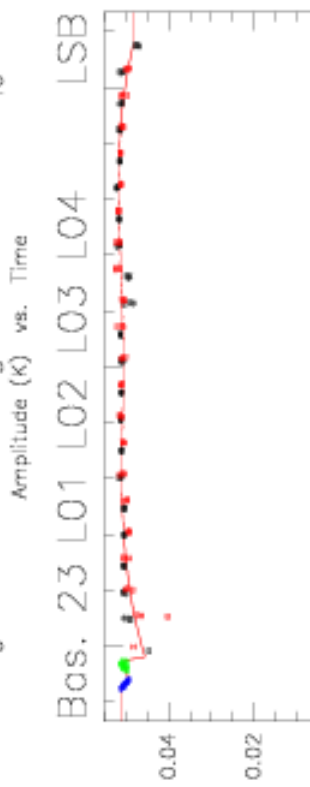
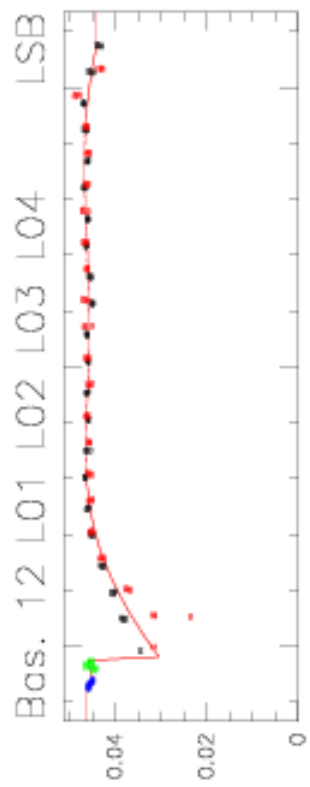
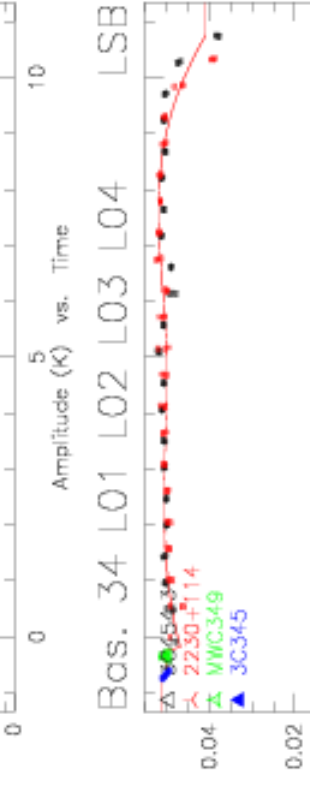
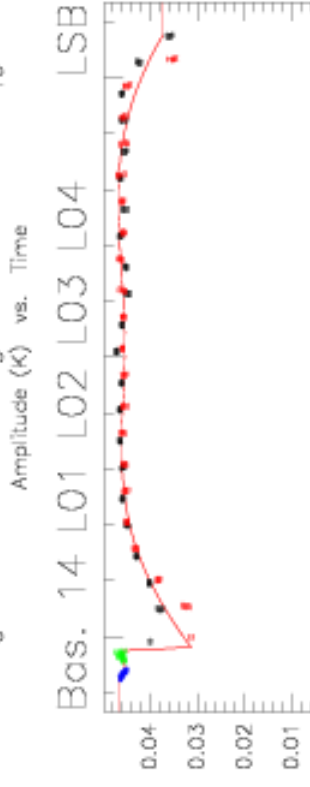
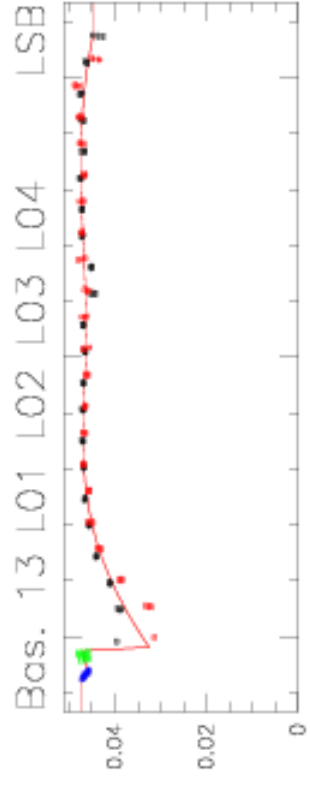


# Amplitude calibration

## The problems

- Temperature (K)  $\rightarrow$  Flux (Jansky)
  - Scaling by **antenna efficiency** (Jy/K)
  - **Not enough for mm-interferometers** because
    - Amplitude loss due to decorrelation
    - Variation of the antenna gain (pointing, focus)
- Need **amplitude referencing to a point source** (quasar) to calibrate out the temporal variation of the antenna efficiency – just like phase calibration

RF: Fr.(A) CLIC - 26-AUG-2005 08:40:56 - gueth W00N09W05E03 Scan Avg.  
 Arr: Scaled 26 1361 KG5A 3C345 P FLUX 12CO(4-3 5D-N05 01-JUN-2001 23:14 -0.4 Vect.Avg.  
 Ph: Rel.(A) Atm. 923 2098 KG5A 3C454.3 P CORR 12CO(4-3 5D-N05 02-JUN-2001 10:45 5.0





# Flux calibration

## The problems

- Problem: **all quasars have varying fluxes** (several 10% in a few weeks) and varying spectral indexes
- **Cannot rely on a priori antenna efficiency** to measure their fluxes (decorrelation...)
- Need to measure the quasar fluxes against
  - Planets
  - Strong quasars (RF)
  - MWC349, CRL618, ...
- Can be **difficult** if a good accuracy is required





Flu  
The

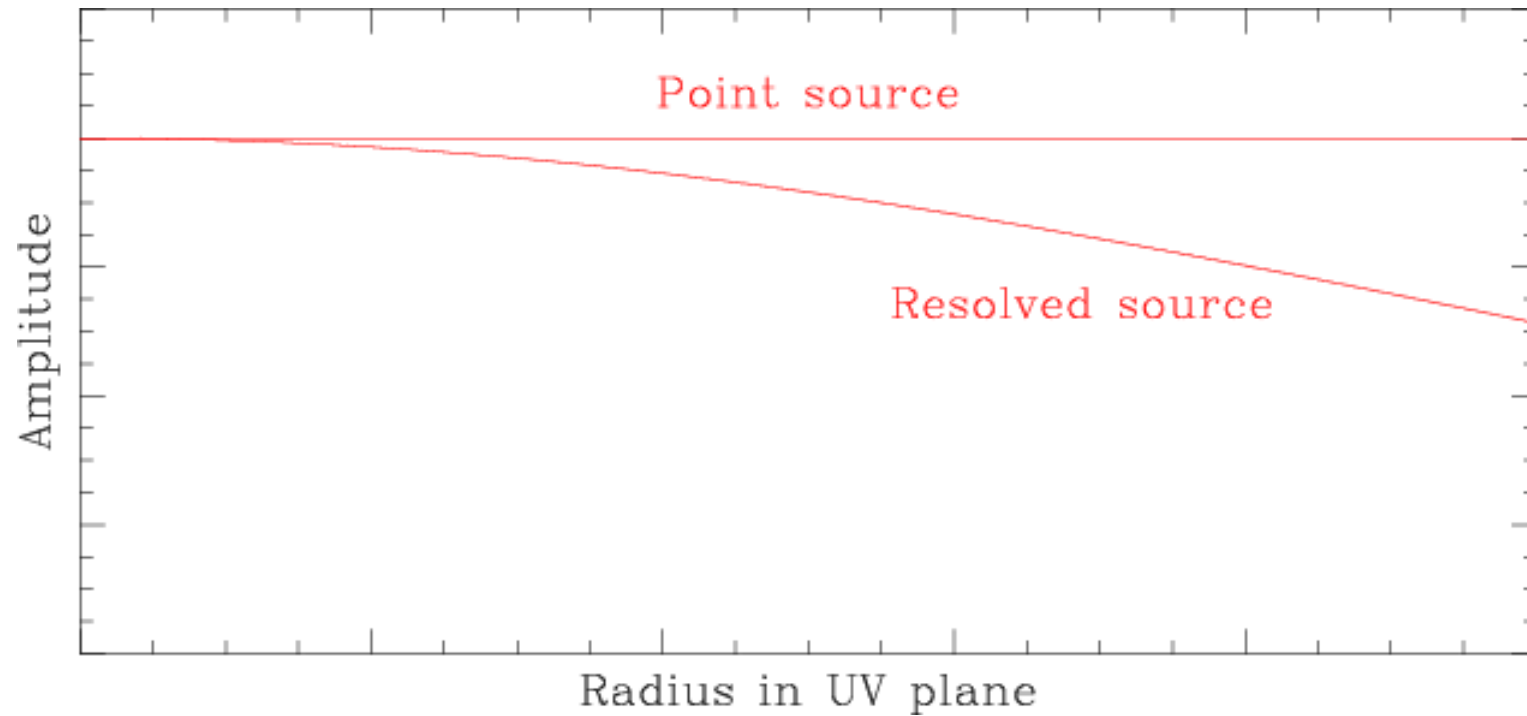
**Caution: terminology  
“(Absolute) Flux calibration”  
vs “Amplitude calibration”**

- Problem: **all quasars have varying fluxes** (several 10% in a few weeks) and varying spectral indexes
- **Cannot rely on a priori antenna efficiency** to measure their fluxes (decorrelation...)
- Need to measure the quasar fluxes against
  - Planets
  - Strong quasars (RF)
  - MWC349, CRL618, ...
- Can be **difficult** if a good accuracy is required



# Flux calibration

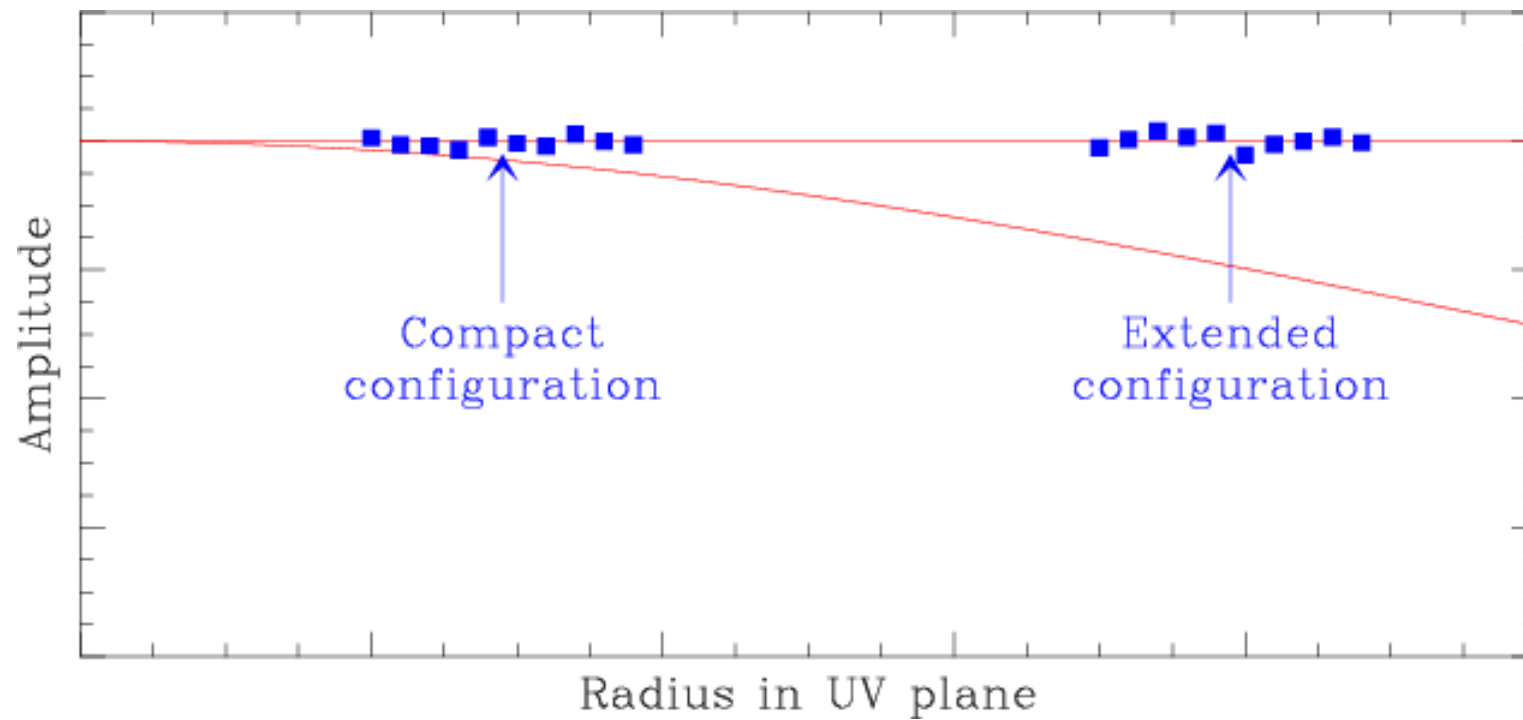
## Not a simple x factor





# Flux calibration

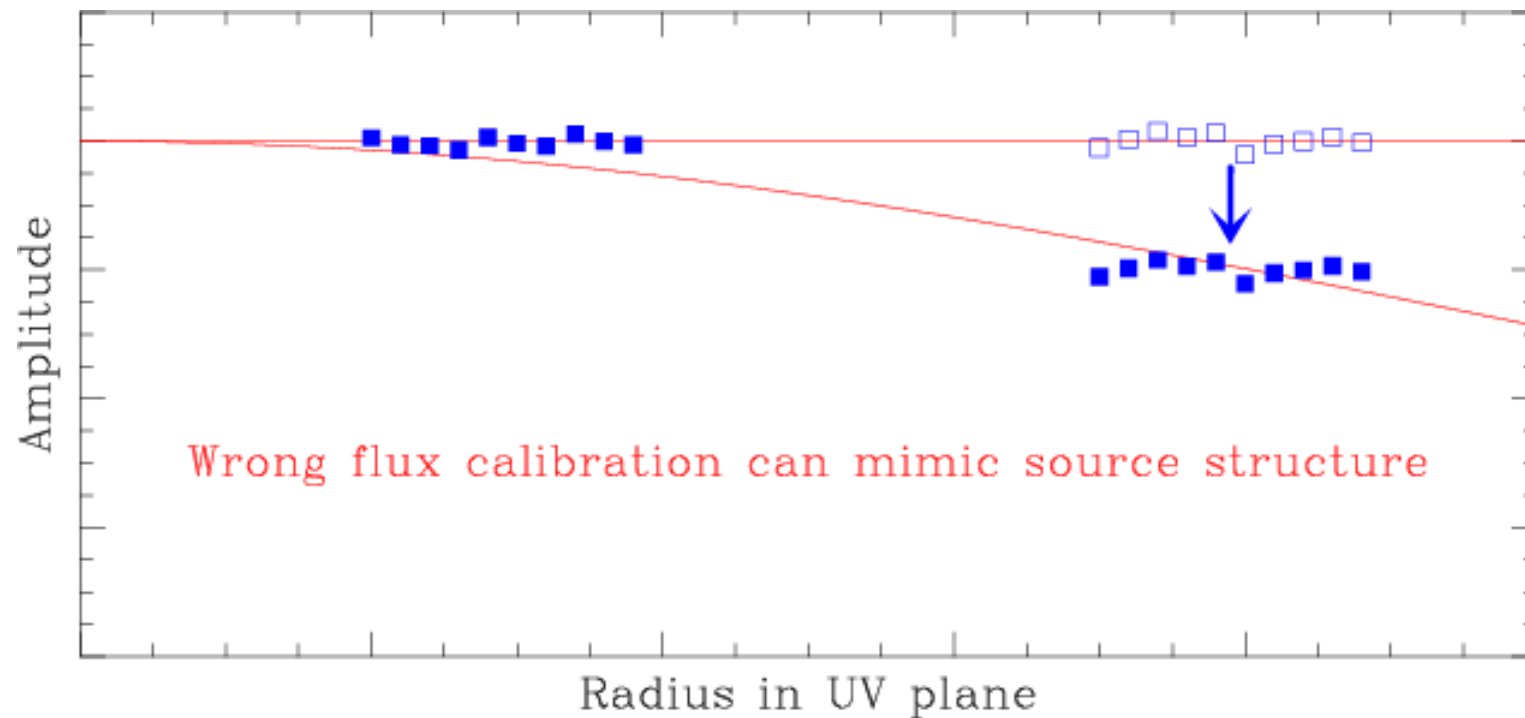
## Not a simple x factor





# Flux calibration

## Not a simple $\times$ factor





# Data calibration

## Conclusions

- All calibrations rely on astronomical observations of quasars = point source, continuum
- **Phase** calibration is the most critical for image quality
- **Flux** calibration is the most difficult in practice

